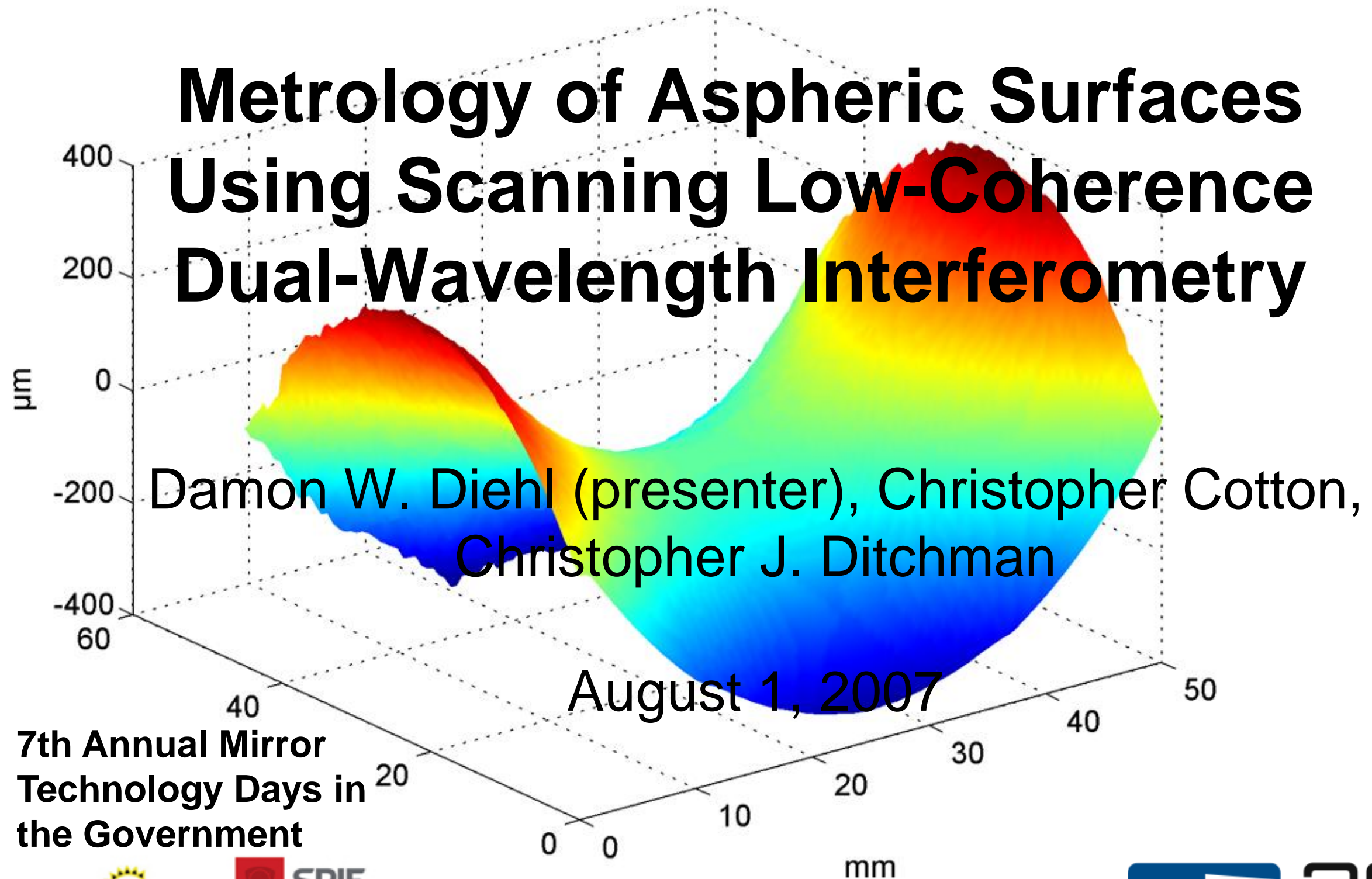


Metrology of Aspheric Surfaces Using Scanning Low-Coherence Dual-Wavelength Interferometry



7th Annual Mirror
Technology Days in
the Government



Acknowledgements

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- A portion of this project was funded by US Army grant W31P4Q-06-C-0185.
- Lumetrics, Inc. provided the OptiGauge dual interferometer used for these measurements.
- Douglas Jacobs-Perkins and Steve Jacobs at the University of Rochester Laboratory for Laser Energetics provided metrology samples.

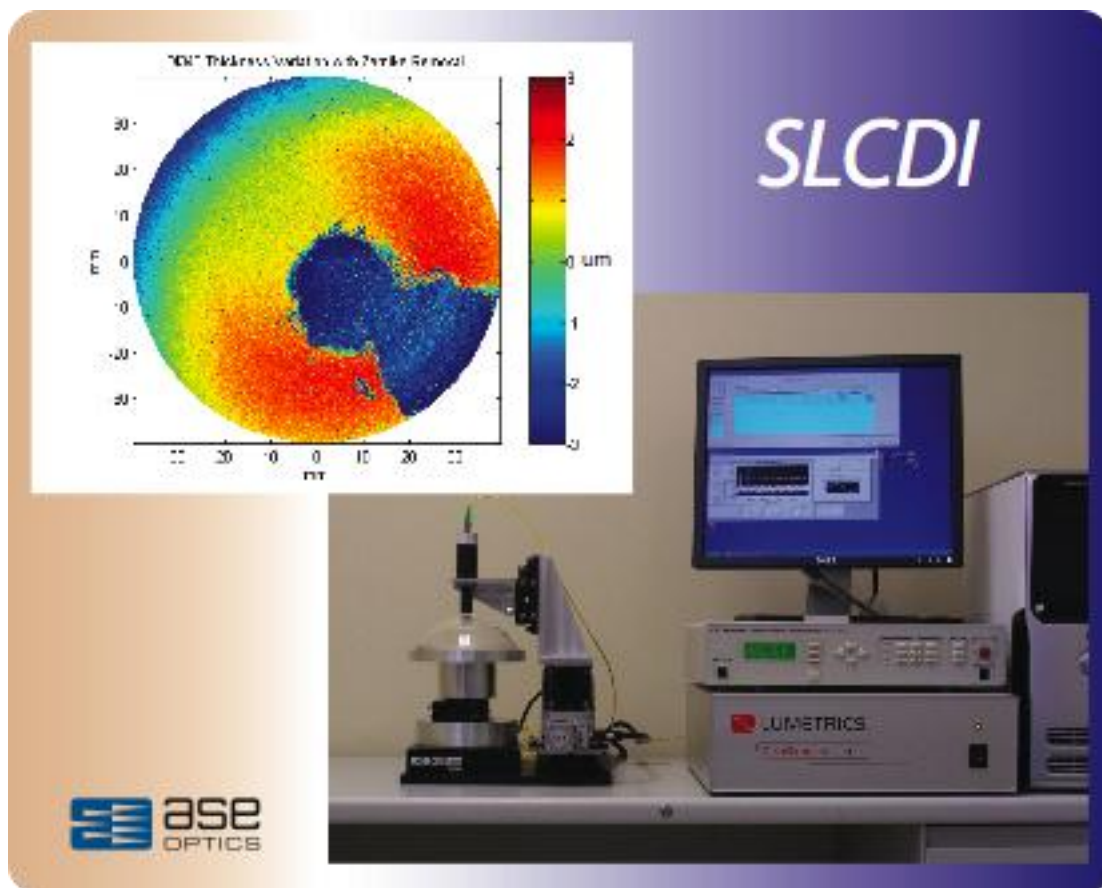
“The Big Picture”

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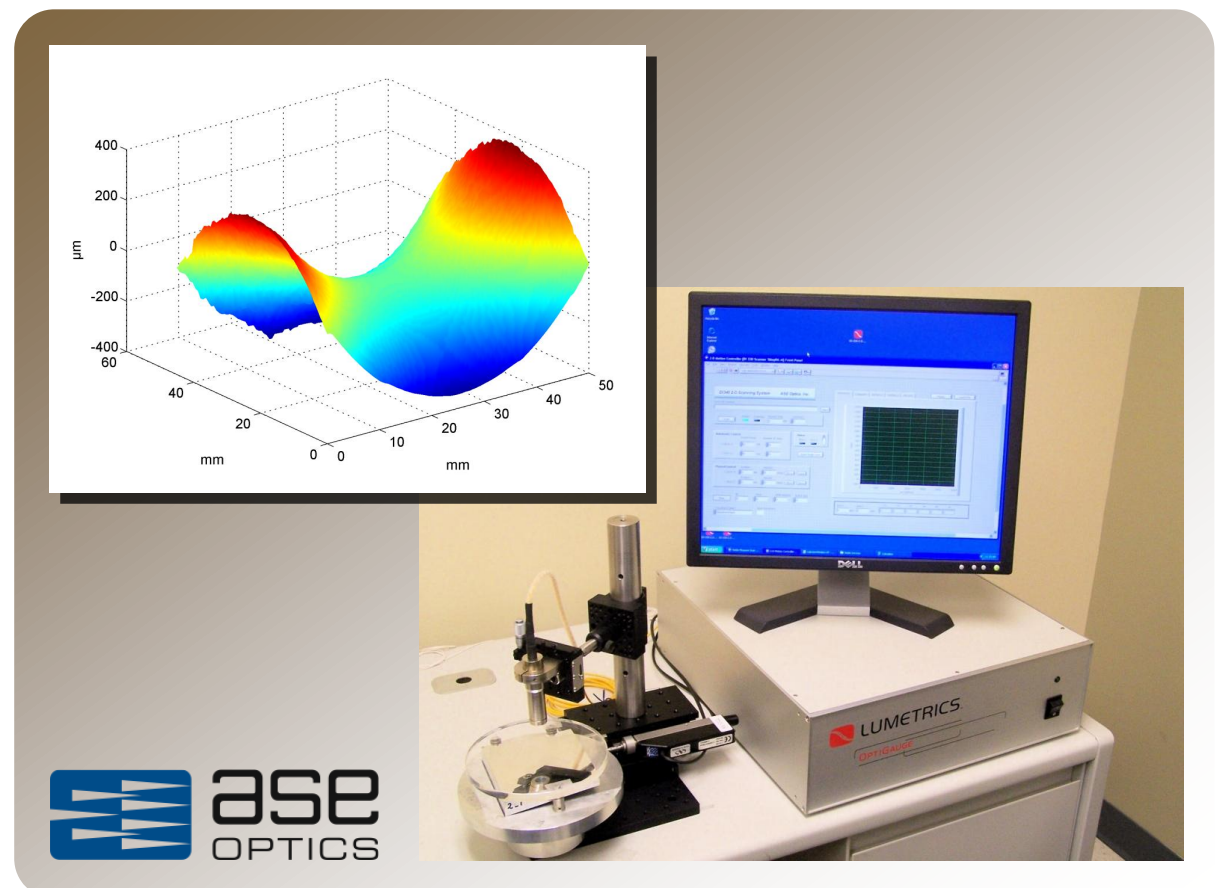


ASE Optics has developed a surface and thickness metrology instrument based upon scanning low-coherence dual-wavelength interferometry (SLCDI).

Thickness Metrology



Surface Metrology



Outline

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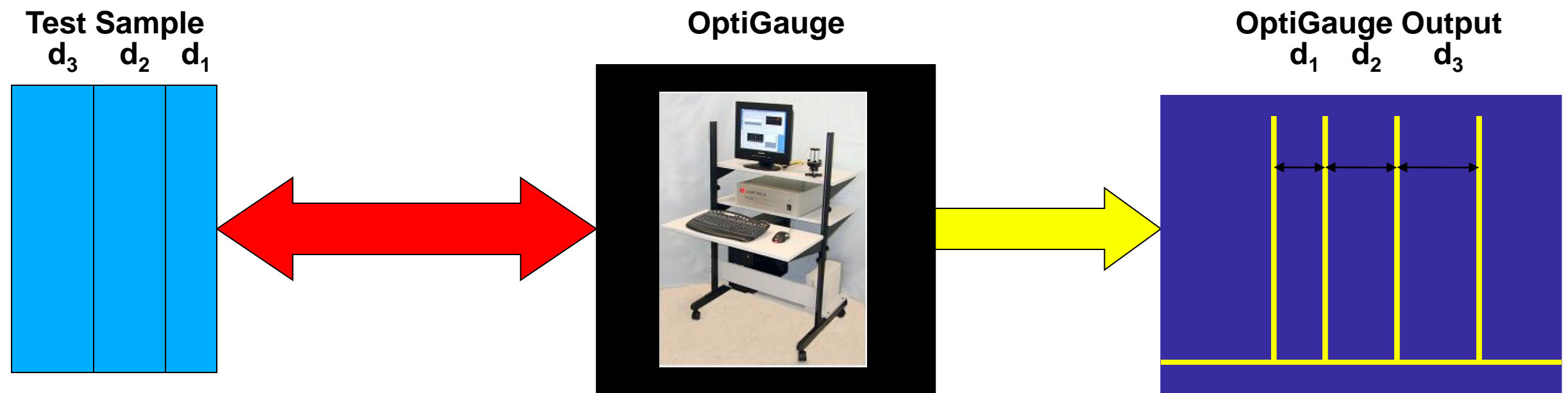


- **Lumetrics DI Overview**
- **Hemispheric dome scanning (Army SBIR)**
- **Aspheric surface scanning (independent research)**



“Black Box” Concept



The OptiGauge uses low-coherence interferometry to simultaneously measure the thickness of each layer within a multilayer material.



- Minimum resolution: 100 nm
- Minimum optical thickness: 12 μm
- Maximum optical thickness: 12 mm

Kodak	<i>Proc. SPIE 3538, 180–191 (1999)</i> <i>Proc. SPIE 3538, 192–203 (1999)</i> <i>Proc. SPIE 4204, 61–70 (2001)</i> <i>Proc. SPIE 4578, 136–144 (2002)</i> <i>Proc. SPIE 5272, 150–156 (2003)</i>
 LUMETRICS	<i>Proc. SPIE 5879, 23–41 (2005)</i>
 ase OPTICS	<i>Proc. SPIE 6545 (2007)</i>

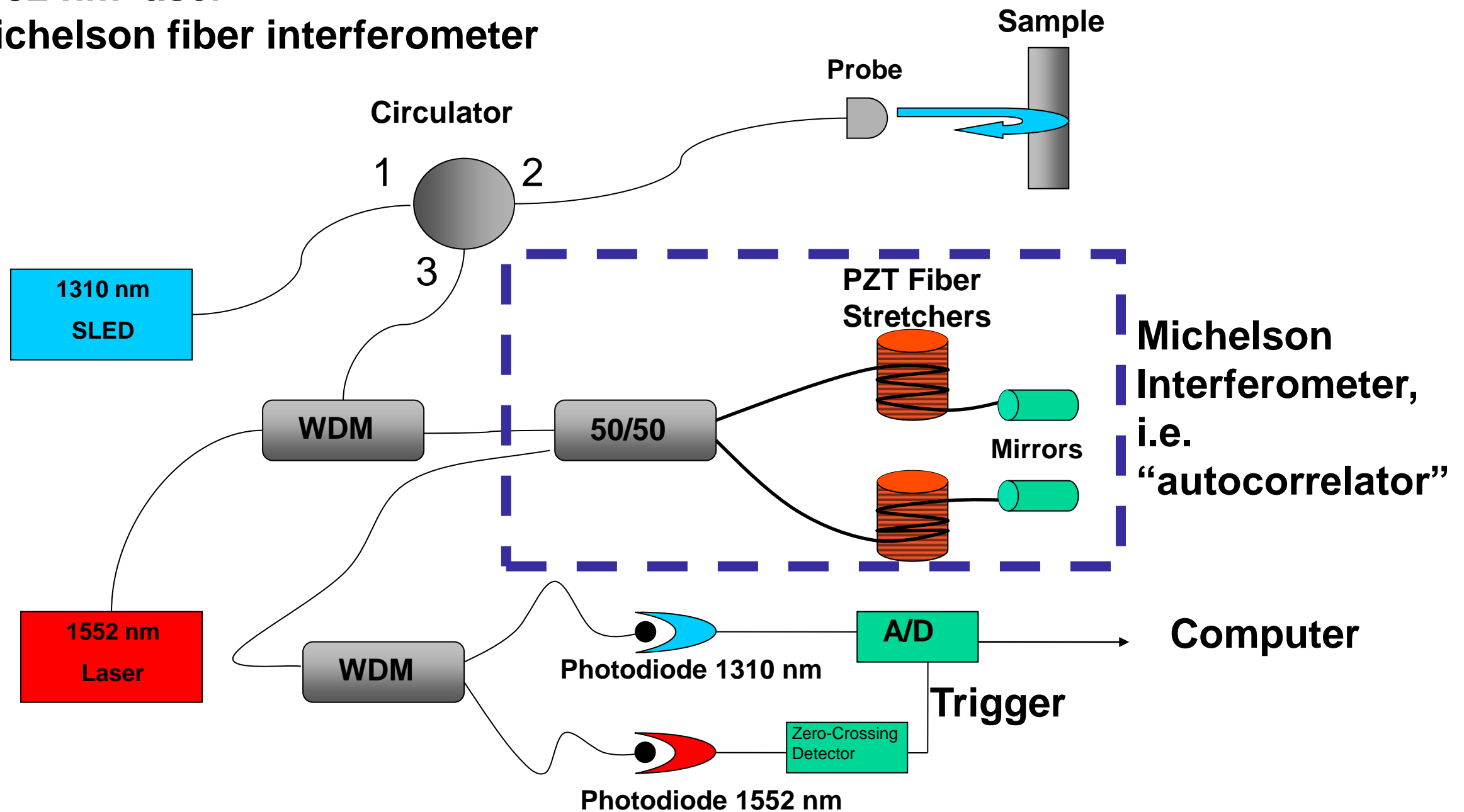
Insided the “Black Box”

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The key components inside the OptiGauge are:

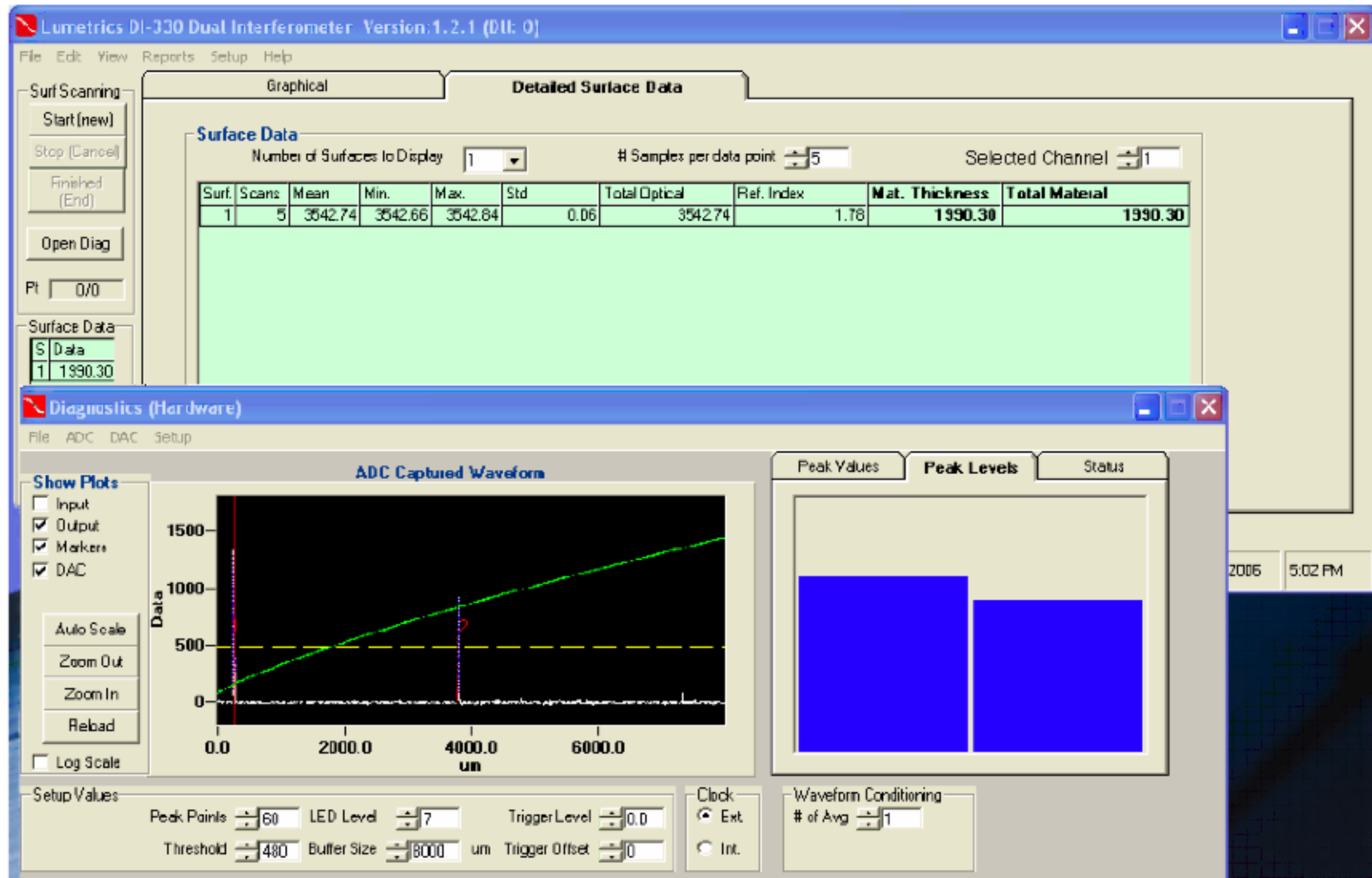
- 1310 nm SLED
- 1552 nm laser
- Michelson fiber interferometer



Lumetrics DI Overview:

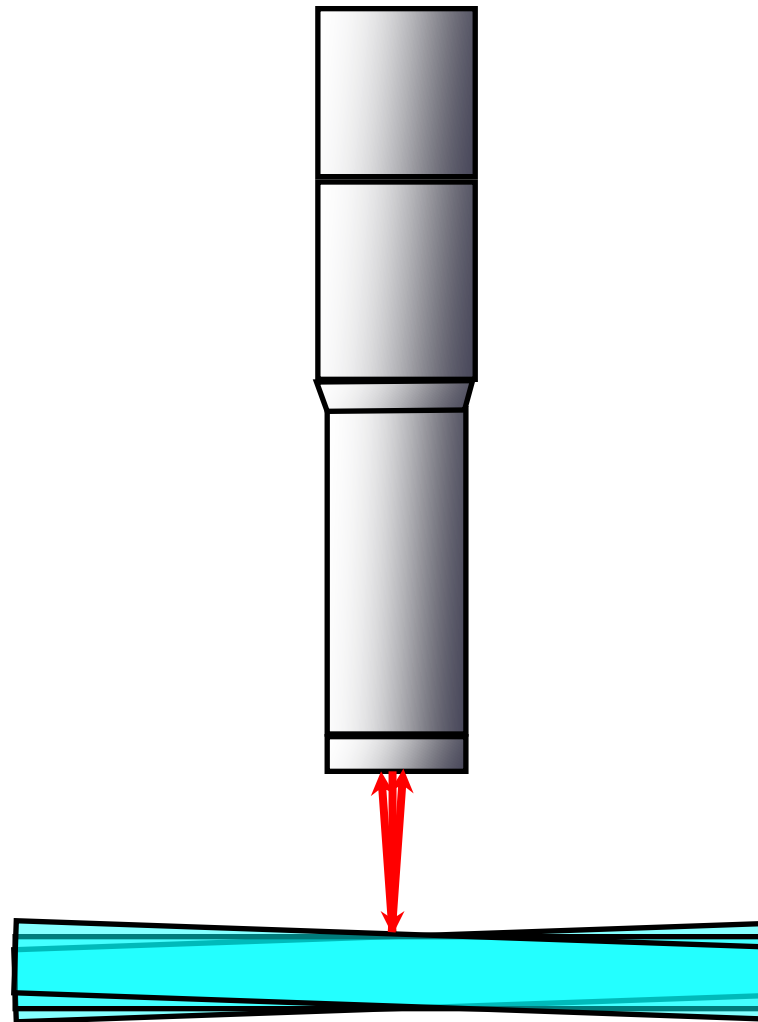
The OptiGauge DI 340 incorporates the data analysis into a simple graphic user interface.

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The OptiGauge probe can tolerate a $\pm 2^\circ$ surface deviation from normal.

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This tolerance allows the system to measure objects that differ significantly from planar or spherical without requiring complex conformal tracing.

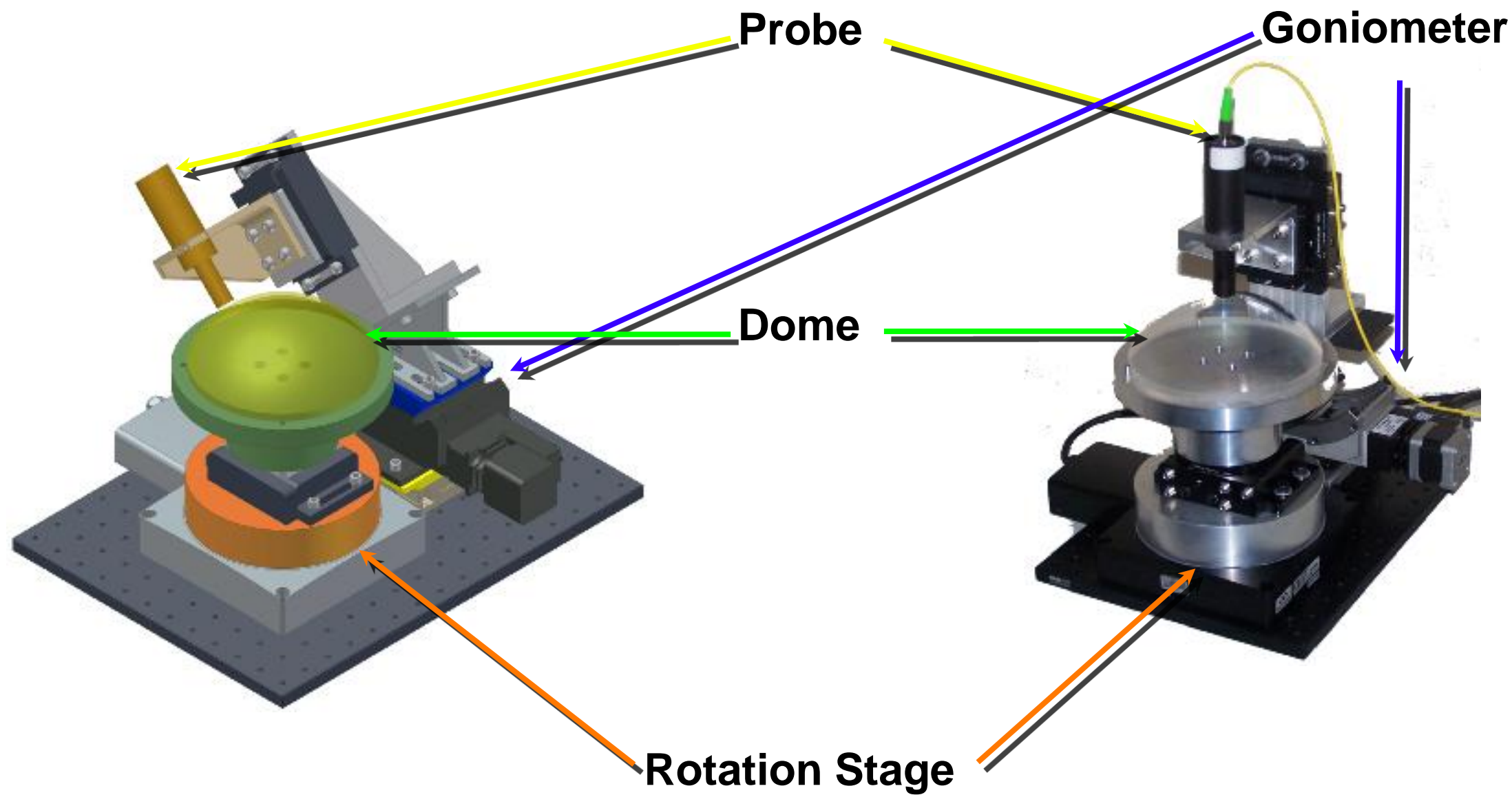
Outline

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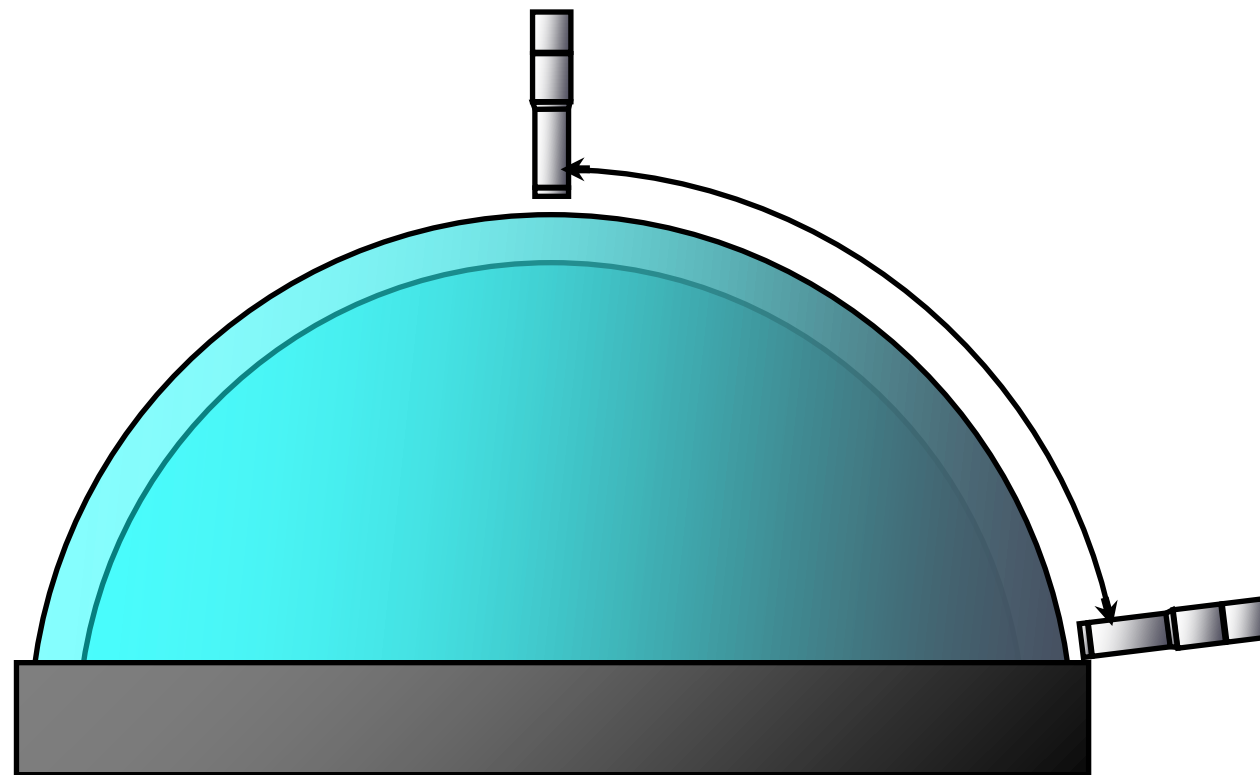
- Lumetrics DI Overview
- **Hemispheric dome scanning (Army SBIR)**
- **Aspheric surface scanning (independent research)**

Scanner Components



The rotation stage and goniometer allow us to scan the dome surface conformally with the probe at normal incidence.

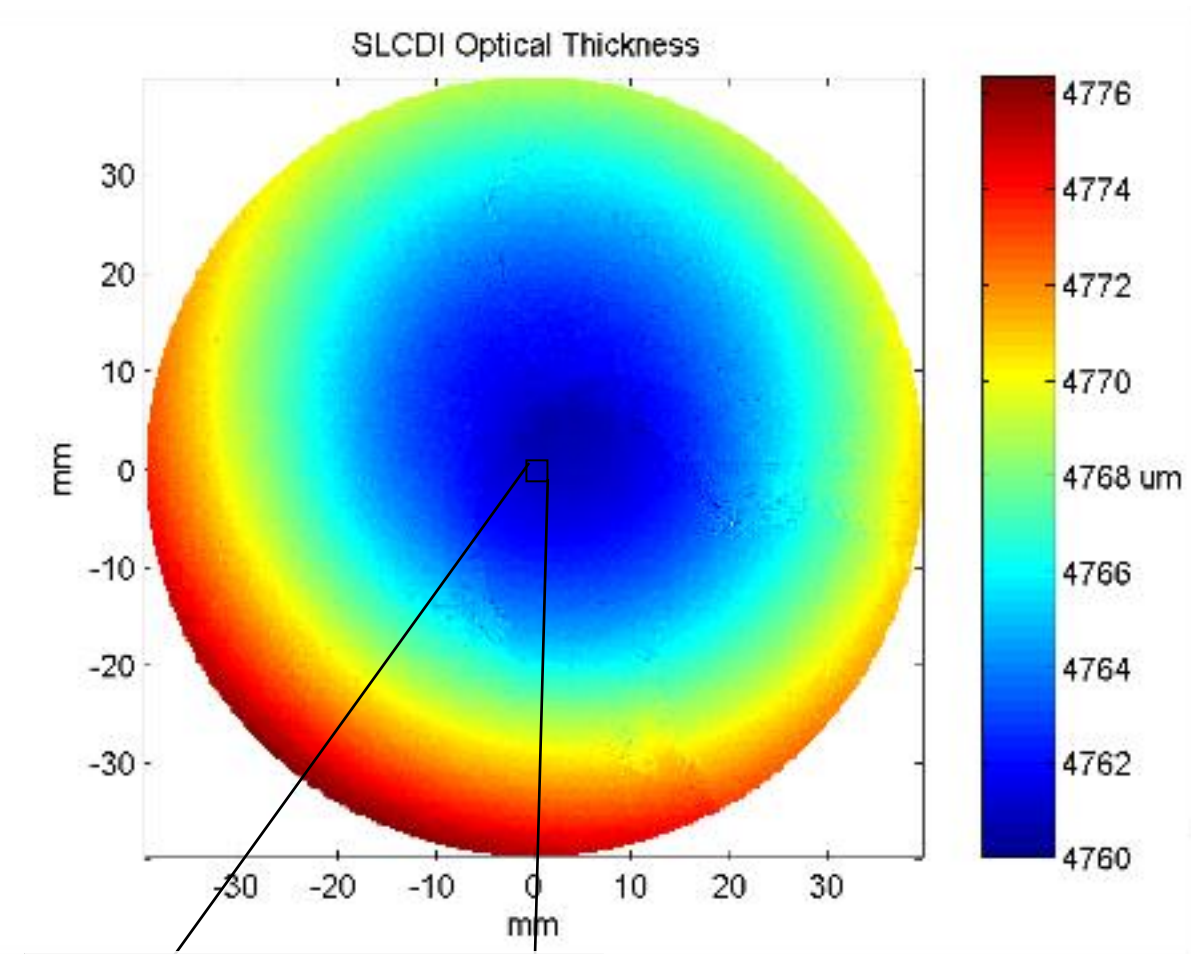
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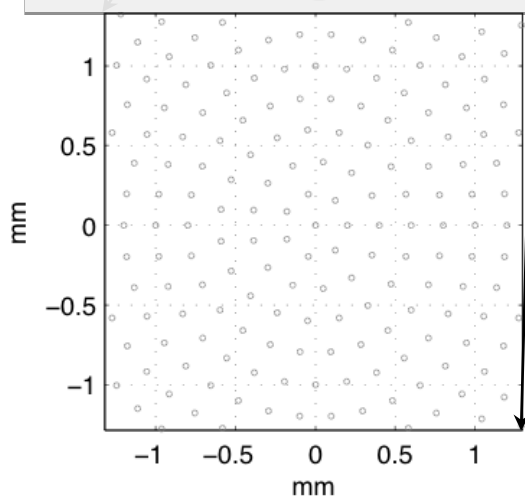
Results:

A 3.5" BK7 domelet was tested using both SLCDI & a Zygo interferometer.

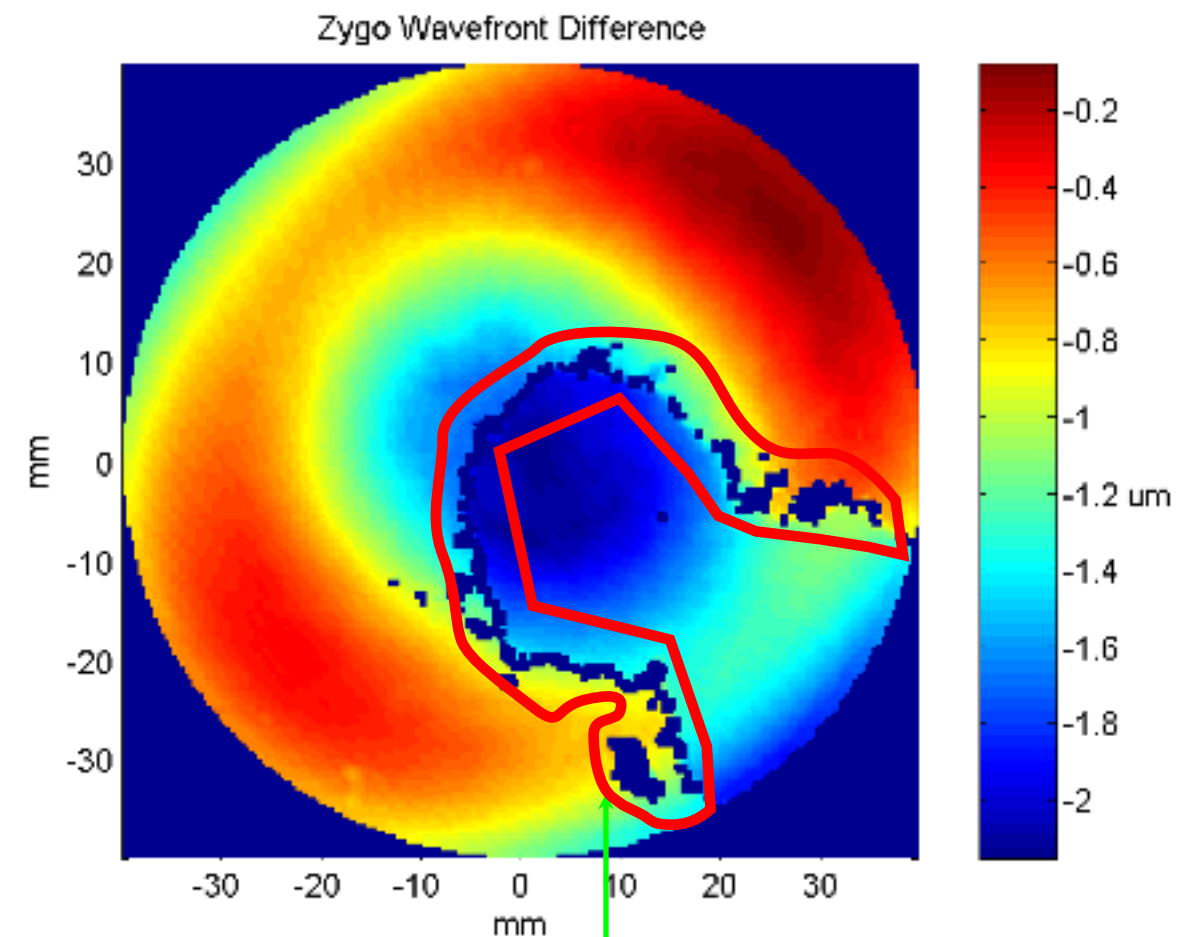
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Sampling Pattern



**Sample Separation:
200 μm**



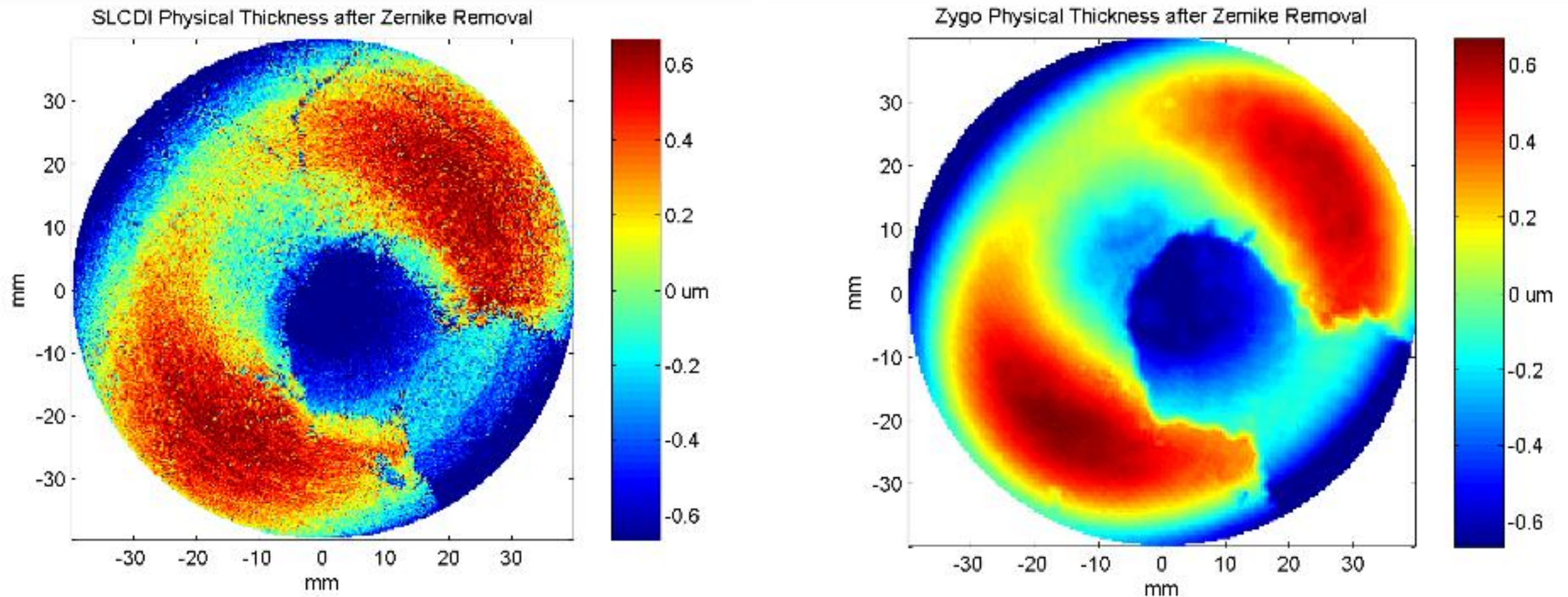
**Phase unwrapping fails at
discontinuities**

**Note: The Zygo system is aligned to
remove tip/tilt and defocus.**

Results:

The images can be compared by converting both maps to physical thickness and remove piston, tip/tilt, and defocus.

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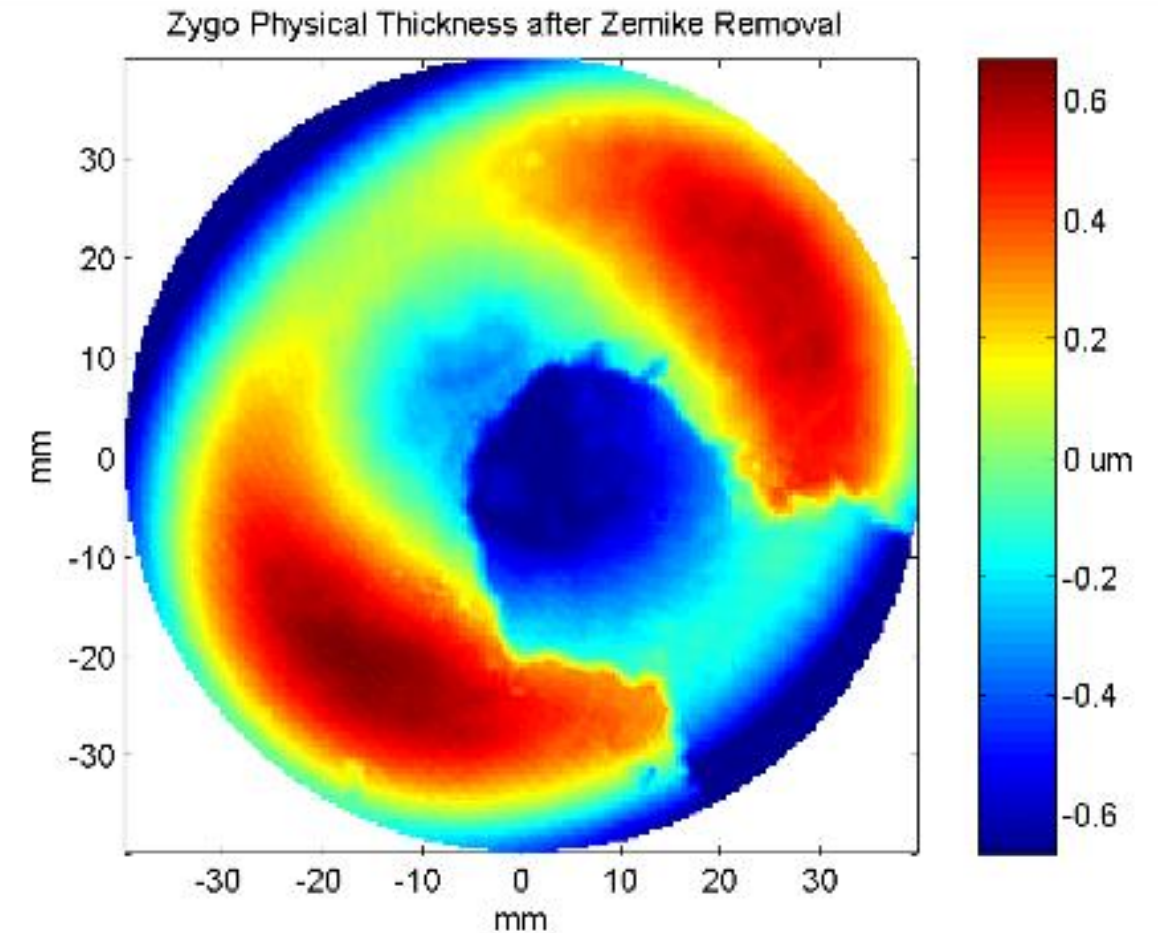
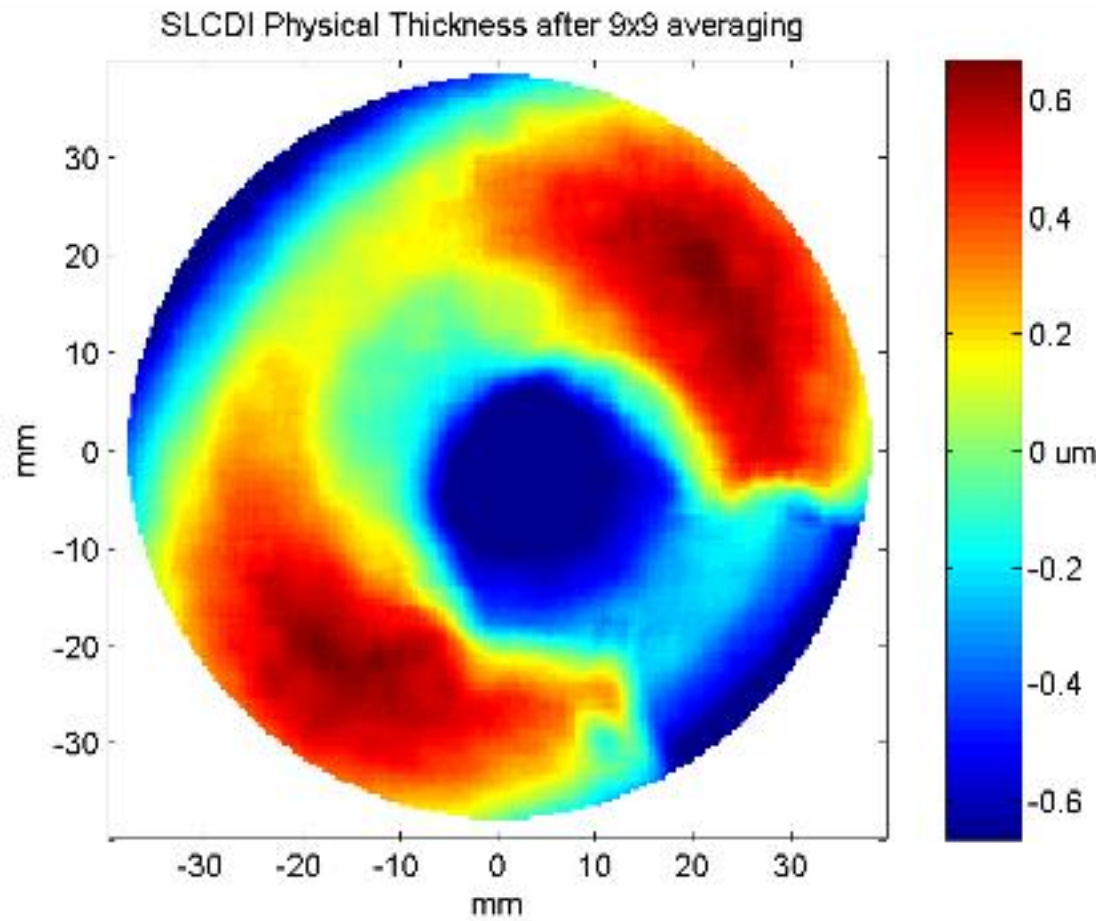


Zernike Order		Fit Coefficients (μm)	
		SLCDI	Zygo
0	Piston	+4811.0	-0.946
1	Tip	-0.4	+0.059
2	Tilt	-0.8	-0.132
3	Defocus	+0.8	+0.284

Results:

Nearest-neighbor averaging reduces the noise in the SLCDI image.

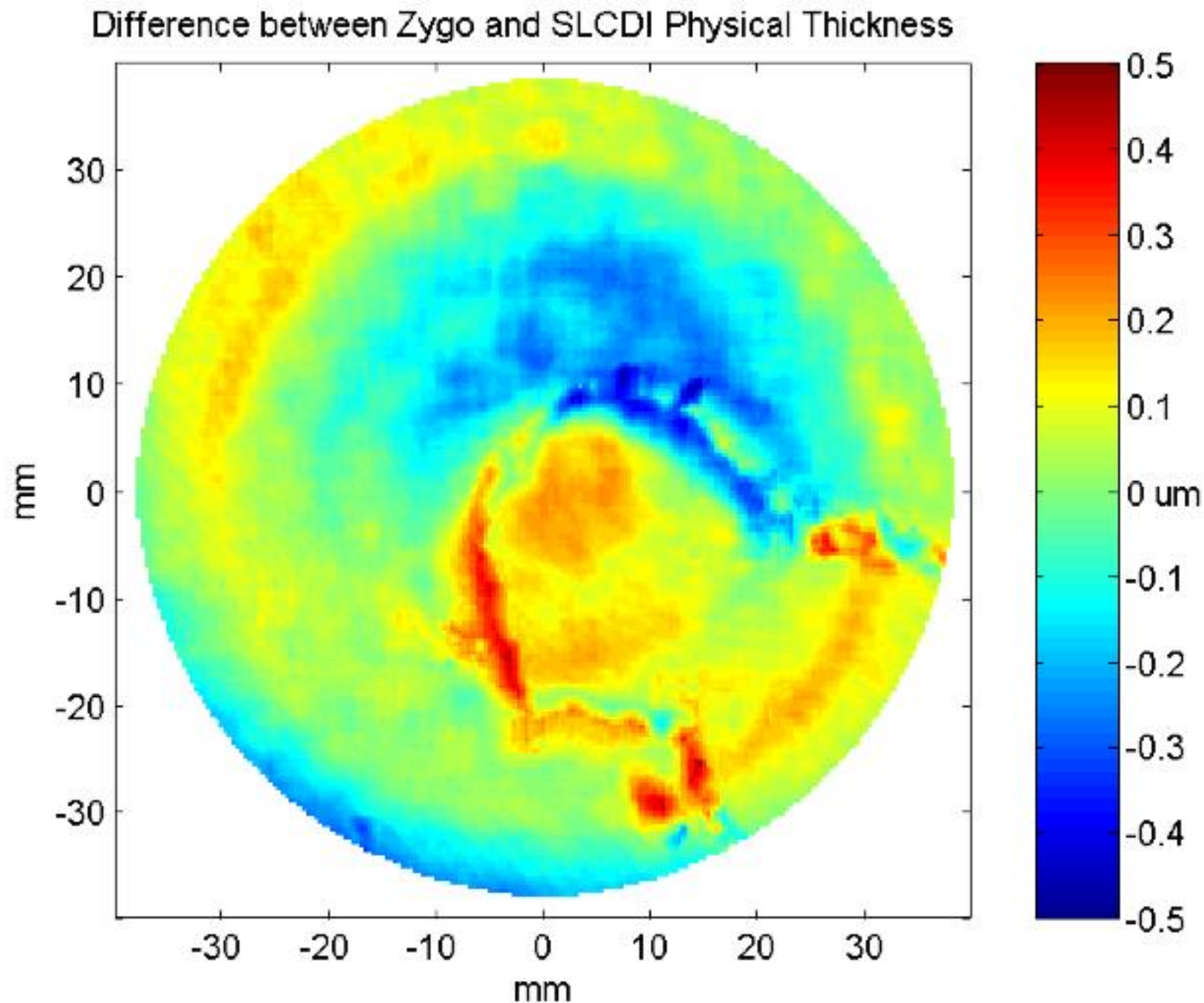
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Results:

The maximum difference between the Zygo and SLCDI data is 200 nm, when disregarding the edge of the coating defect.

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Outline

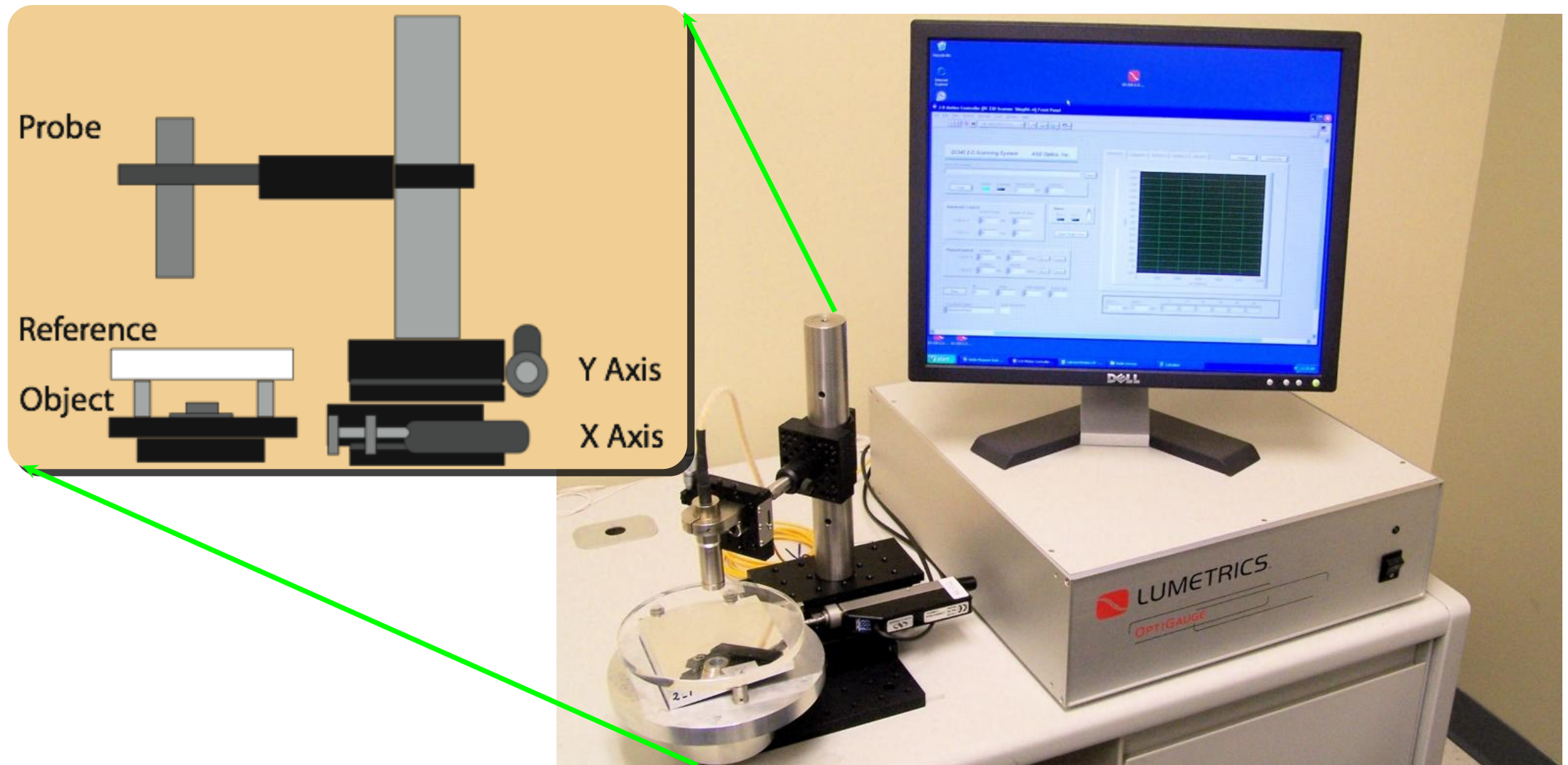
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- Lumetrics DI Overview
- Hemispheric dome scanning (Army SBIR)
- **Aspheric surface scanning (independent research)**

Scanner Components

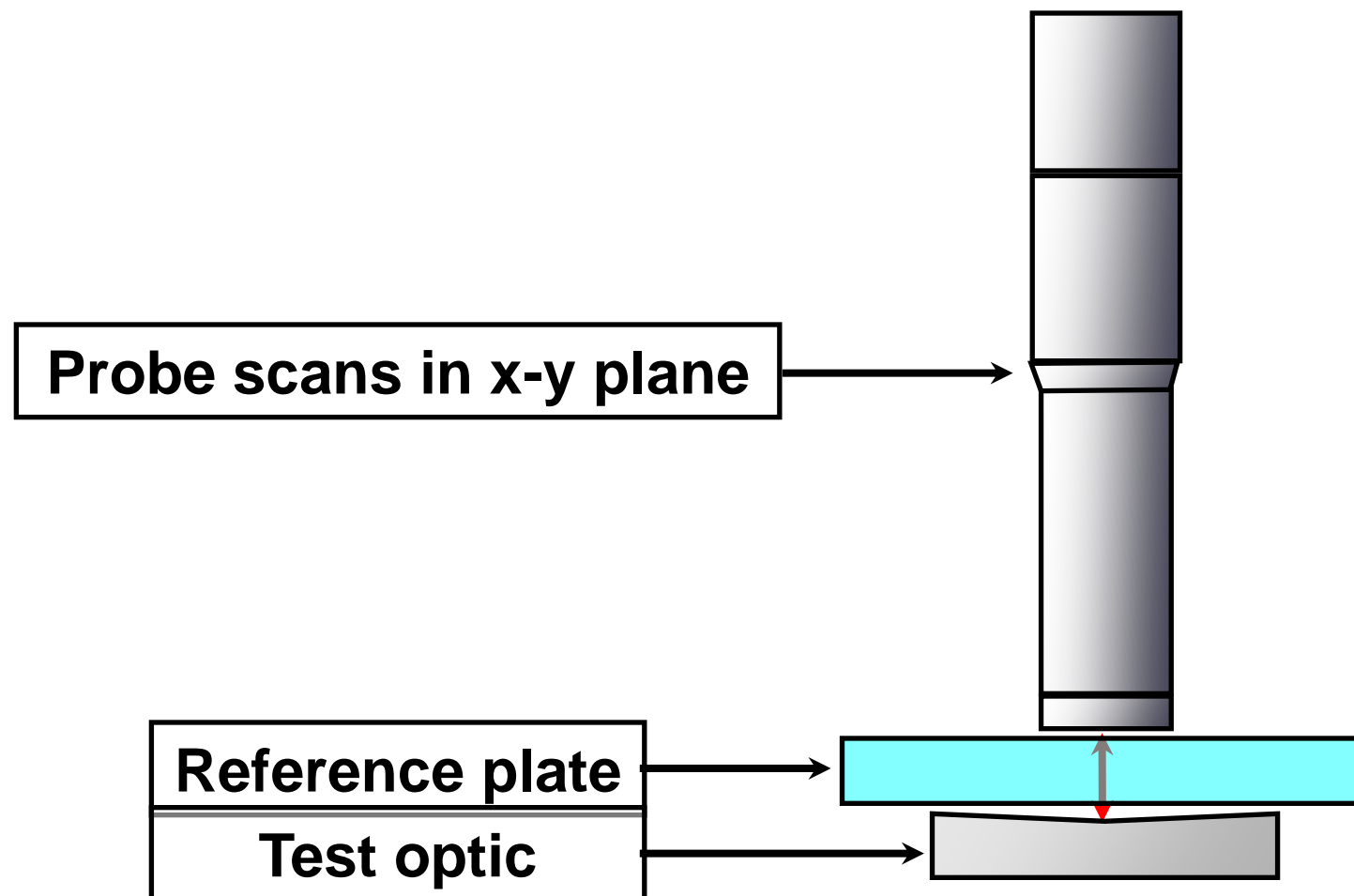
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The scanner incorporates two Newport LTA-HS motorized linear stages with 0.035 μm resolution.

SLCDI measures surface profiles by measuring the airgap between a reference and a test optic.

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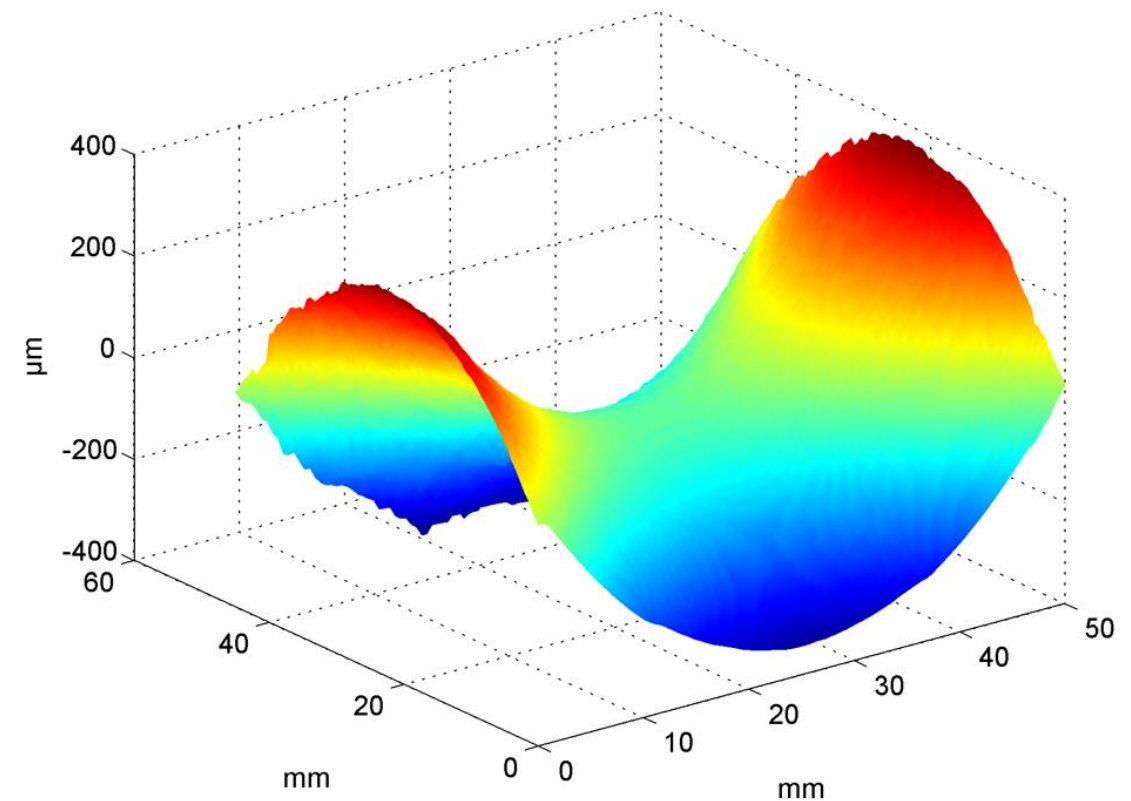
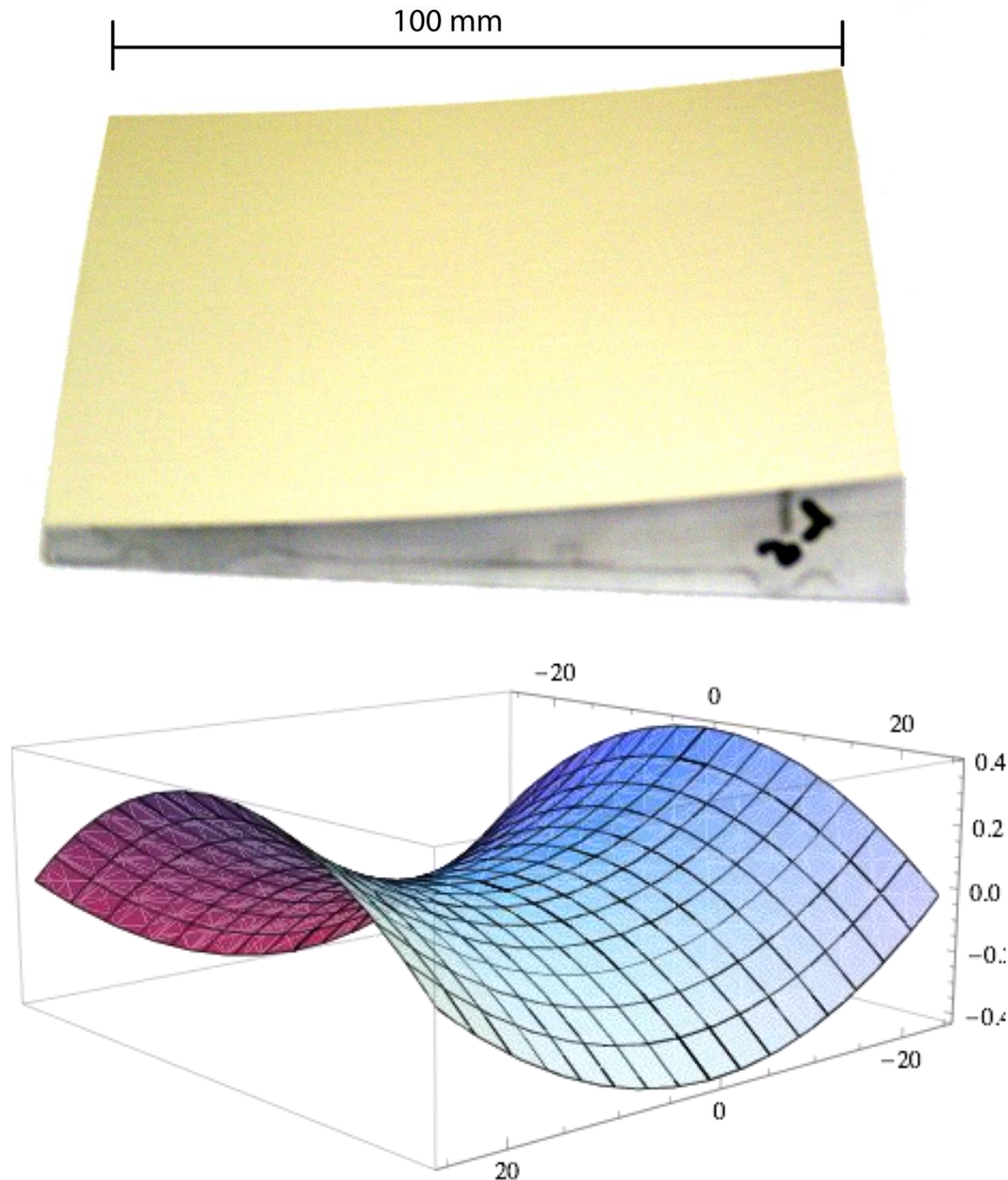
Results:

We measured a 50 mm square portion of a biconic mirror with radii of 799.5 mm and -759.23 mm.

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SLCDI surface profile after removal of tip/tilt

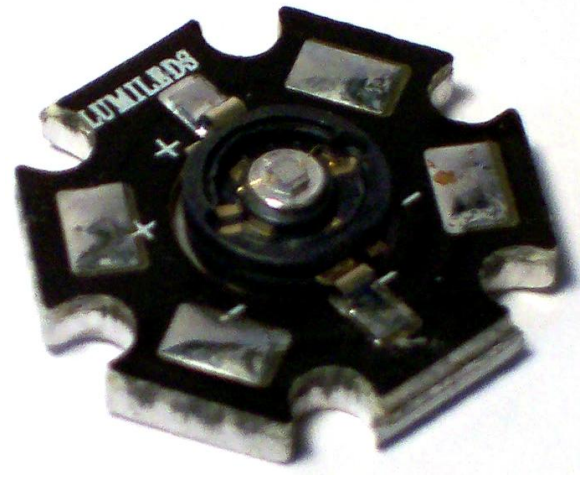


50 μm spatial resolution

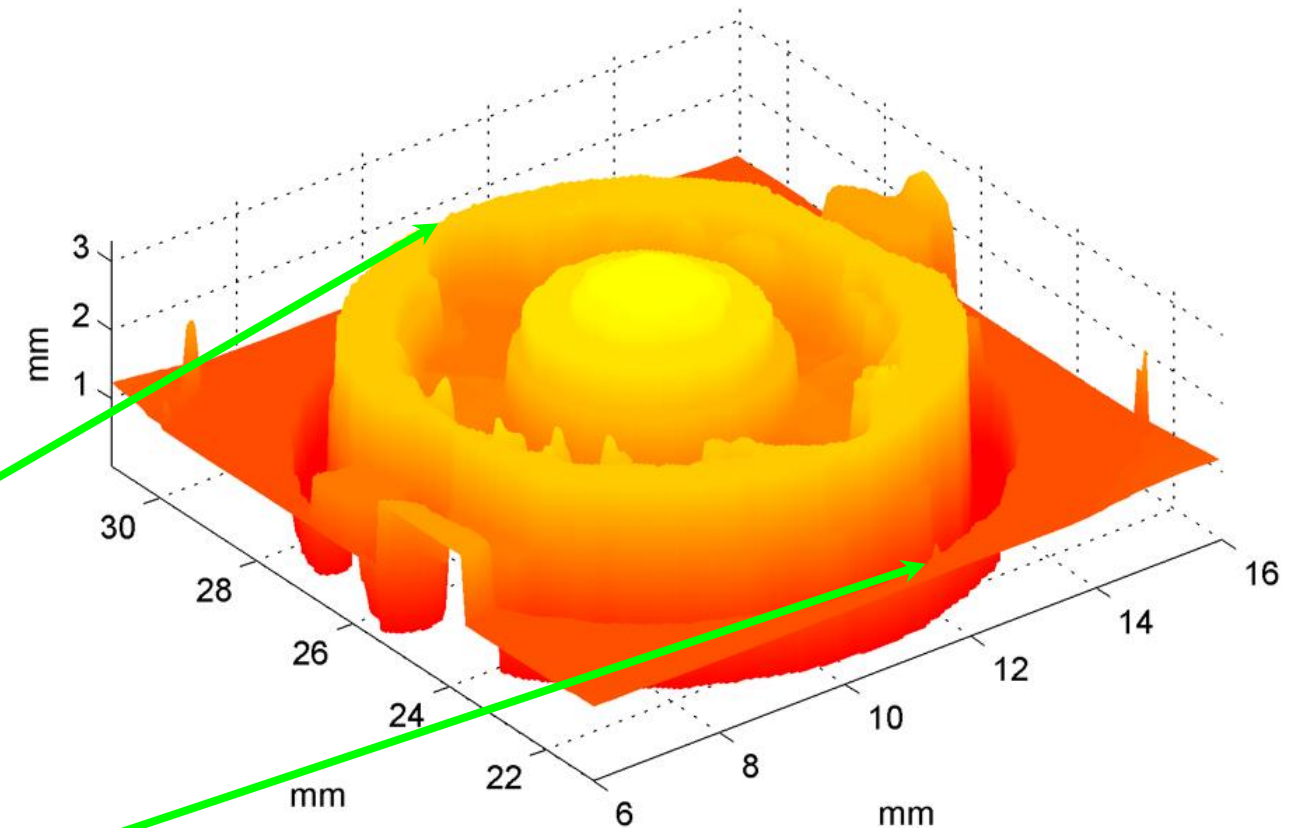
Results:

SLCDI can measure discontinuous surfaces without encountering phase ambiguities.

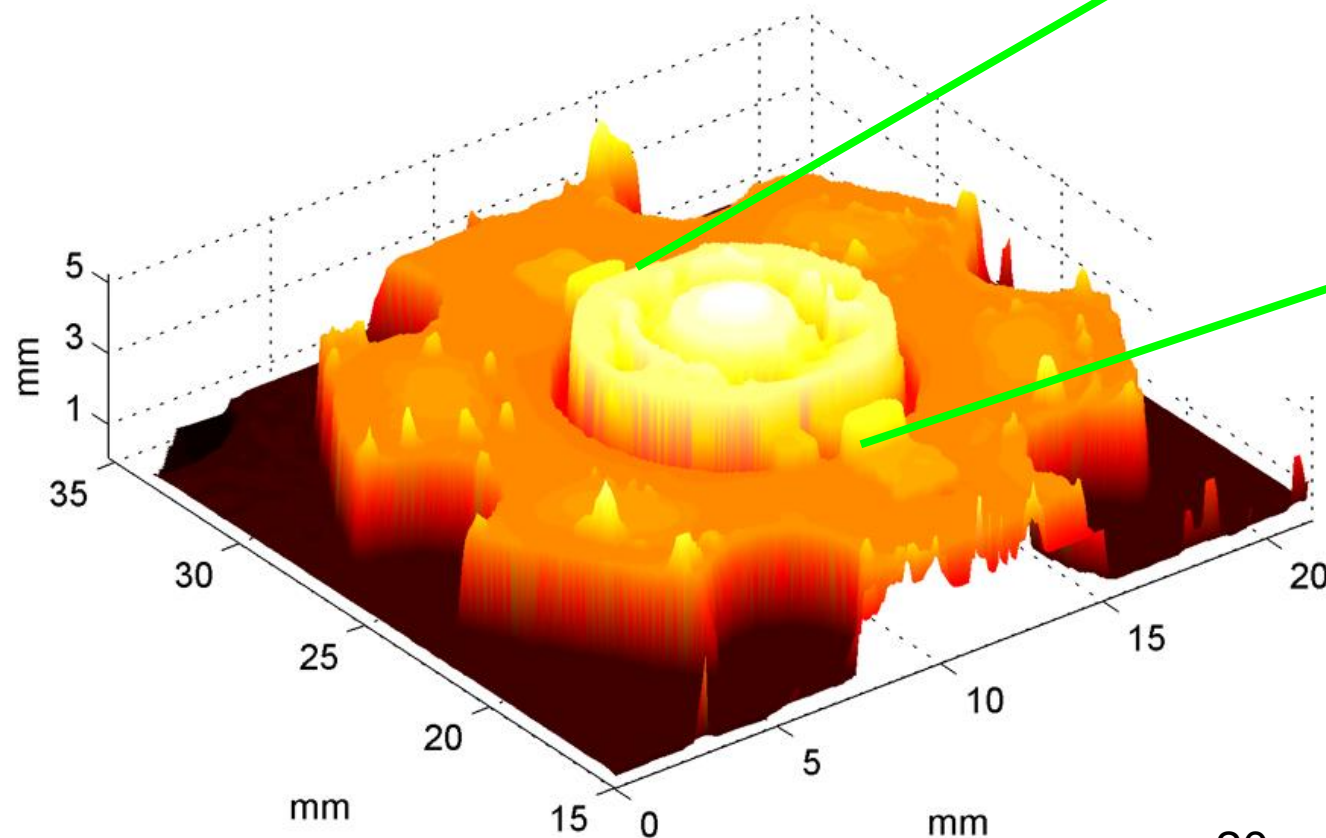
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50 μm spatial resolution



160 μm spatial resolution



Conclusions

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- **SLCDI is a non-contact metrology solution capable of simultaneously measuring both optical thickness and surface profile.**
- **SLCDI yields results that are in agreement with traditional interferometry to within 200 nm.**
- **SLCDI can measure non-traditional shapes, such as saddle mirrors and complex surfaces.**
- **This metrology topic is no longer supported by the US Army. We are seeking new funding sources for this project.**

Backup slides

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All the math...

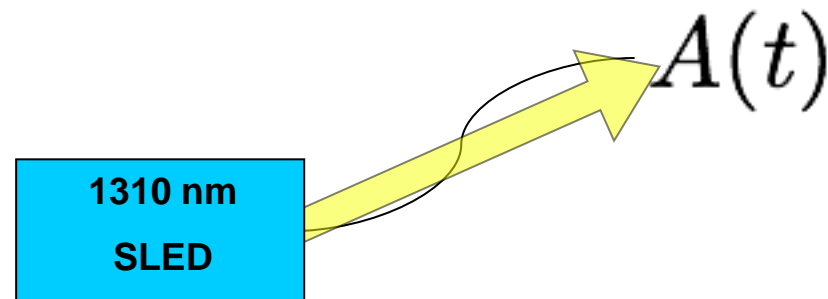
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The Math You Need to Know: Part 1

Autocorrelation

The amplitude of the electric field of the SLED light at a time t is $A(t)$.



The autocorrelation of the field amplitude is the integral of two signals displaced by an increment of time.

$$\Gamma(t, \tau) = \langle A^*(t) A(t + \tau) \rangle = \frac{\int_{-T/2}^{+T/2} A^*(t) A(t + \tau) dt}{T}$$

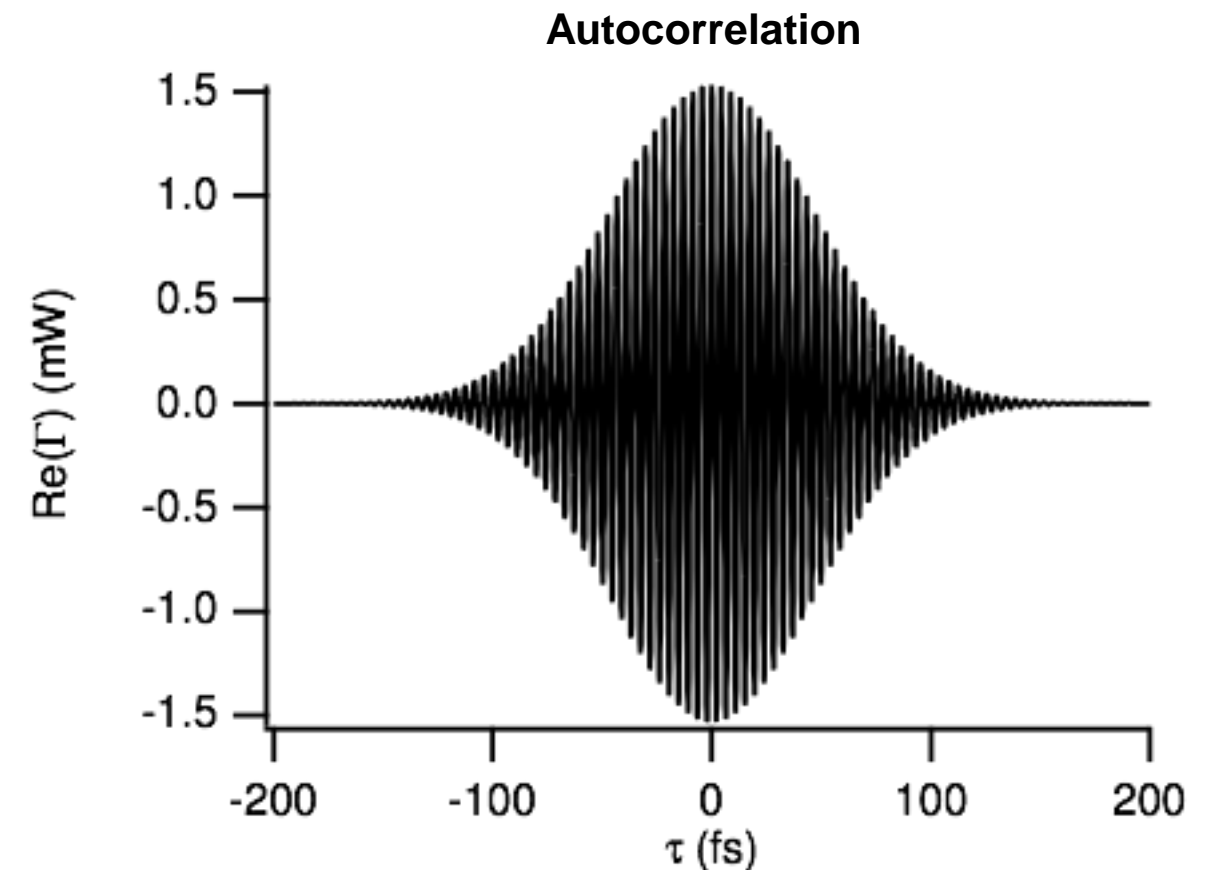
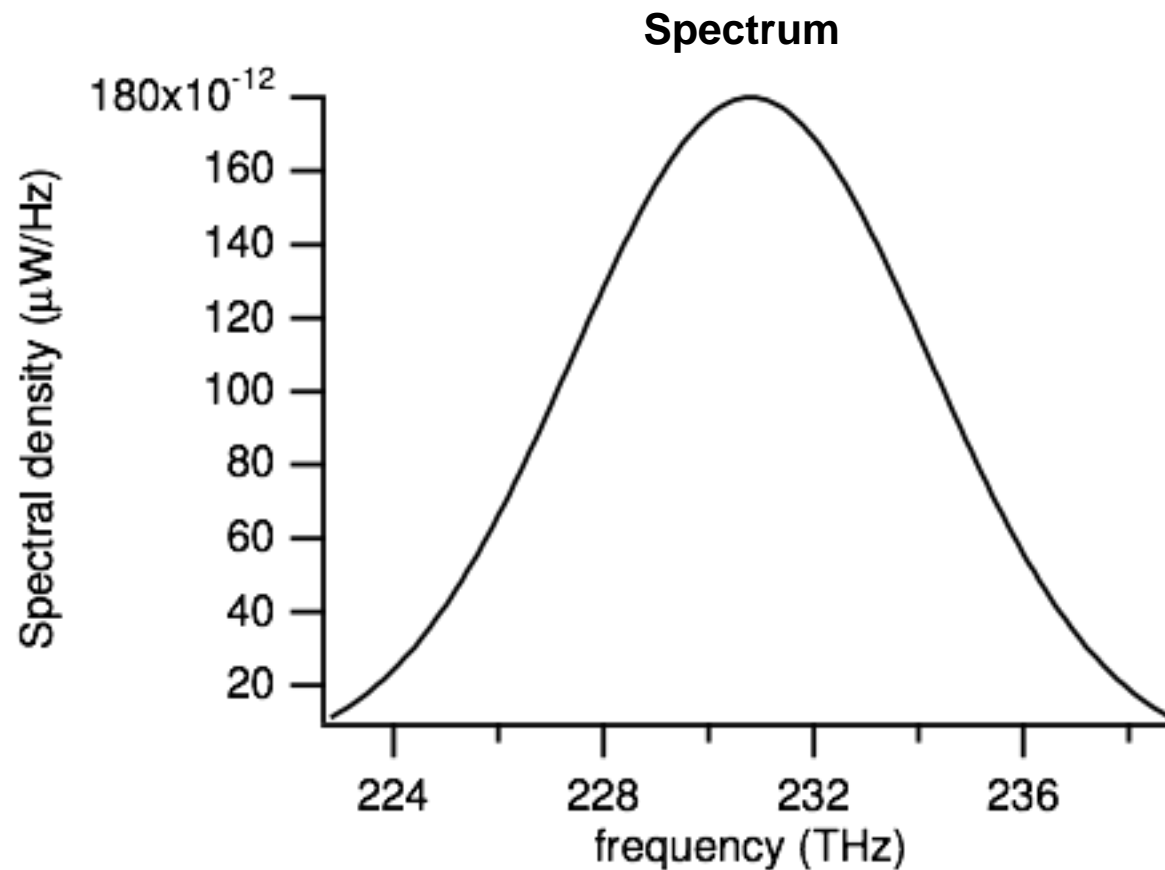
For a stationary random process, the autocorrelation is independent of the time, t , i.e.

$$\Gamma(t, \tau) = \Gamma(\tau)$$

The Math You Need to Know: Part 2

Wiener-Khintchine Theorem

The autocorrelation is the Fourier transform of the SLED spectrum



$$\Gamma(\tau) = \int_{-\infty}^{+\infty} S(\nu) \exp(-i 2\pi \nu \tau) d\nu.$$

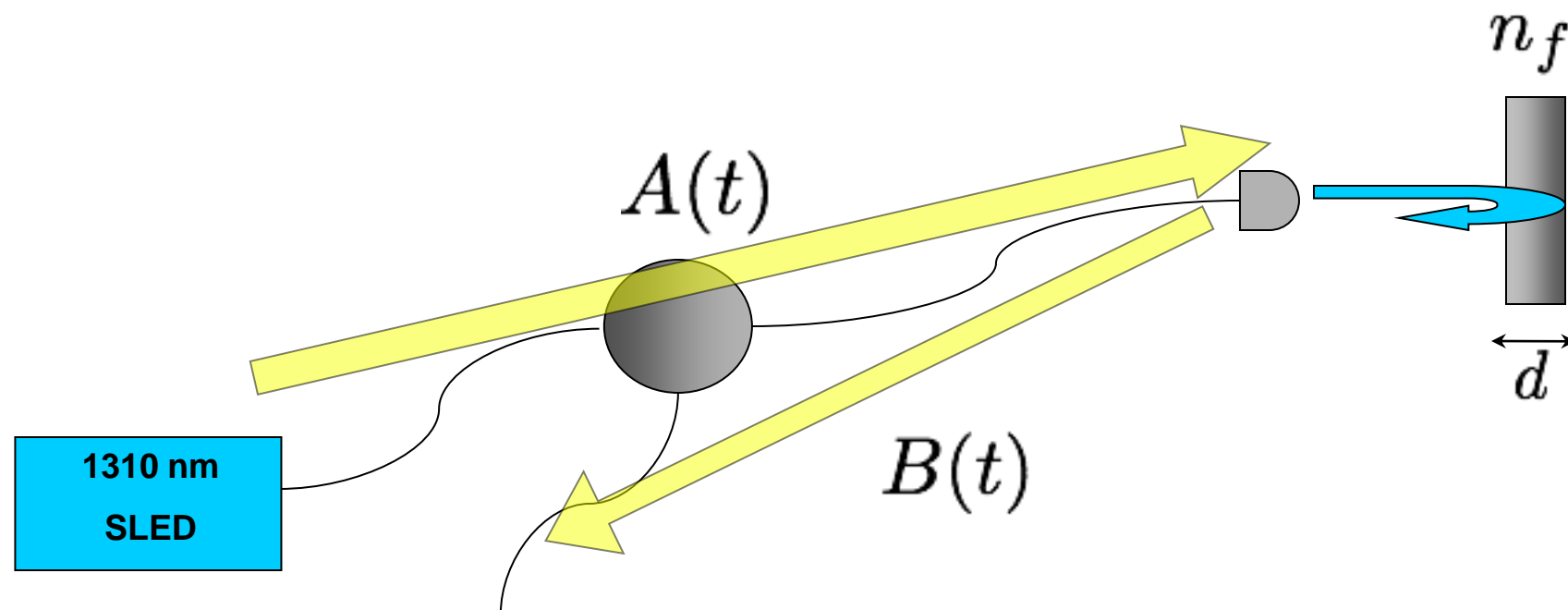
$$S(\nu) = a_0 \exp \left[-4 \ln(2) \left(\frac{\nu - \nu_0}{\Delta\nu} \right)^2 \right]$$

$$\Gamma(\tau) = a_0 \left| \frac{\Delta\nu}{2} \sqrt{\frac{\pi}{\ln(2)}} \right| \exp \left[- \left(\frac{\pi \Delta\nu}{2\sqrt{\ln(2)}} \tau \right)^2 \right] \exp(-i 2\pi \nu_0 \tau).$$

$$S(\nu) = \int_{-\infty}^{+\infty} \Gamma(\tau) \exp(+i 2\pi \nu \tau) d\tau$$

Theory of Operation: Field Propagation, Pt. 1

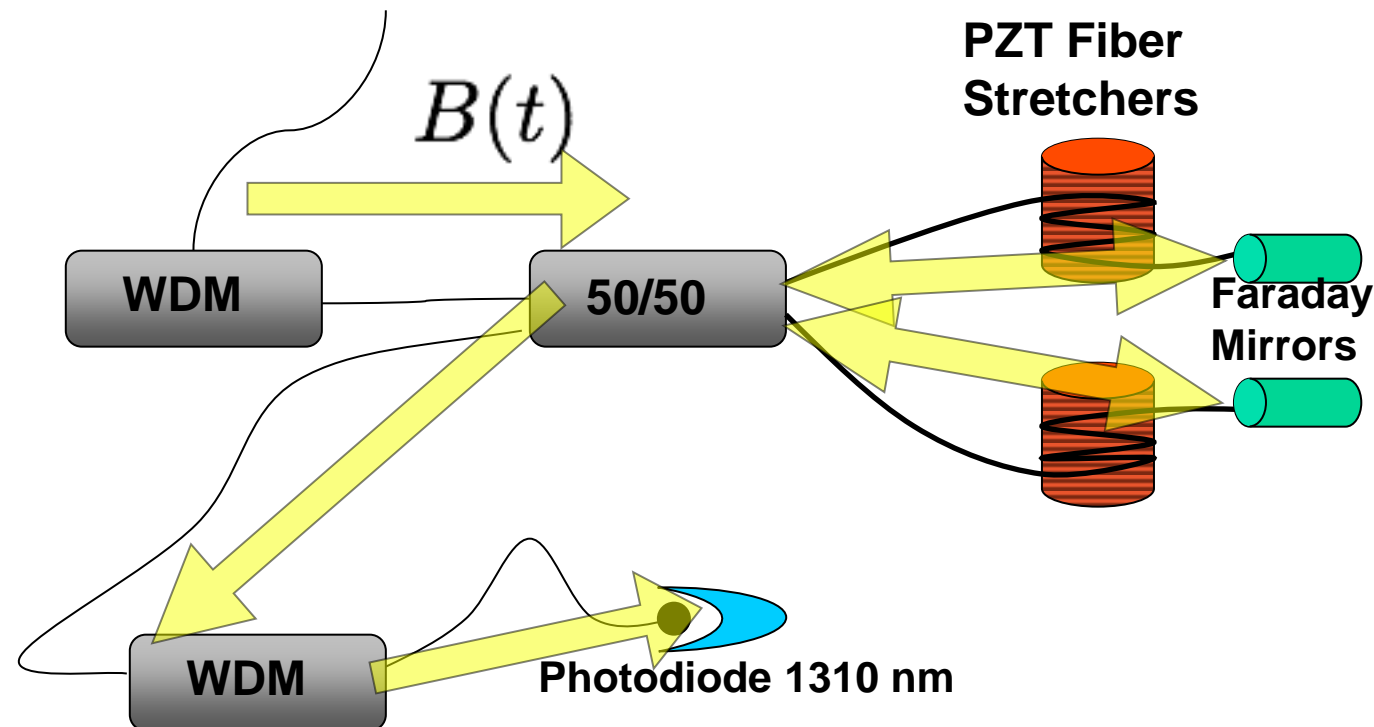
The light collected by the probe is the sum of the fields reflected from each surface.



$$B(t) = r_1 A(t) + r_2 A(t - 2n_f d/c)$$

Theory of Operation: Field Propagation, Pt. 2

The light enters the fiber Michelson interferometer, and each returns a reflection displaced in time. The photodiode reads the intensity of the light.



$$\begin{aligned}
 I(d_1, d_2) &= \langle |B(t + 2n_i d_1/c) + B(t + 2n_i d_2/c)|^2 \rangle \\
 &= \langle [B^*(t + 2n_i d_1/c) + B^*(t + 2n_i d_2/c)] [B(t + 2n_i d_1/c) + B(t + 2n_i d_2/c)] \rangle \\
 &= \langle B^*(t + 2n_i d_1/c) B(t + 2n_i d_1/c) \rangle \cdots \\
 &\quad \cdots + \langle B^*(t + 2n_i d_1/c) B(t + 2n_i d_2/c) \rangle \cdots \\
 &\quad \cdots + \langle B^*(t + 2n_i d_2/c) B(t + 2n_i d_1/c) \rangle \cdots \\
 &\quad \cdots + \langle B^*(t + 2n_i d_2/c) B(t + 2n_i d_2/c) \rangle .
 \end{aligned}$$

Theory of operation: The Meaning, Pt. 1

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The intensity expression becomes surprisingly simple when the B terms are expanded in terms of A, and then written as autocorrelations.

$$\begin{aligned}
 I(\tau) = & 4 \operatorname{Re}[r_1^* r_2 \Gamma(-2n_f d/c)] \cdots \\
 & \cdots + 2(|r_1|^2 + |r_2|^2) \{ \Gamma(0) + \operatorname{Re}[\Gamma(\tau)] \} \cdots \\
 & \cdots + 2 \operatorname{Re}[r_1^* r_2 \Gamma(\tau - 2n_f d/c)] \cdots \\
 & \cdots + 2 \operatorname{Re}[r_1 r_2^* \Gamma(\tau + 2n_f d/c)].
 \end{aligned}$$

small constant terms

peak at 0

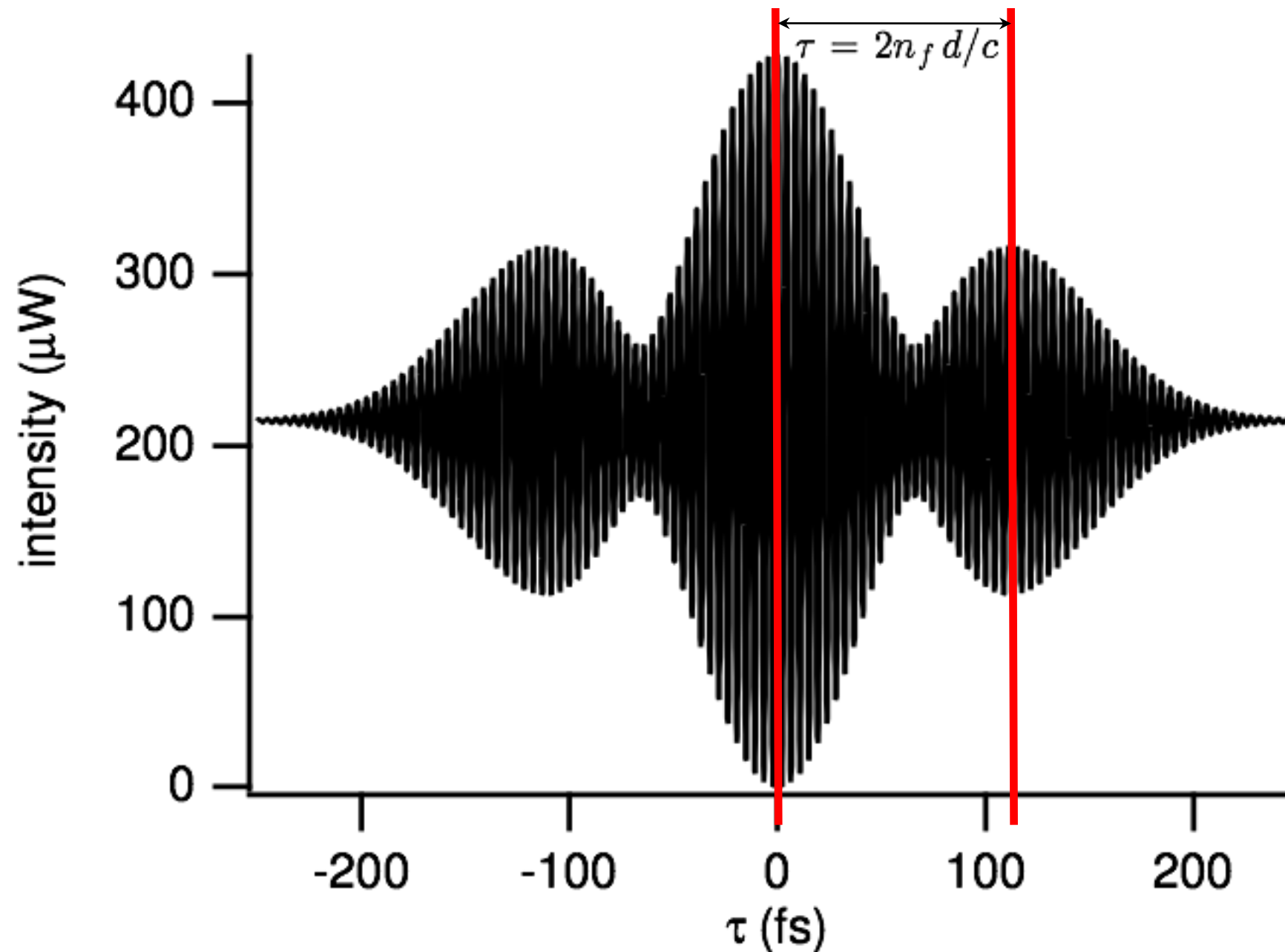
peak at +2n_fd/c

peak at -2n_fd/c

where $\tau = 2(d_2 - d_1)n_i/c$,

Theory of operation: The Meaning, Pt. 2

The distance from the side peak to the center peak is proportional to the optical thickness of the sample.



Scanner Overview:

The scanning software was created in LabVIEW.

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