

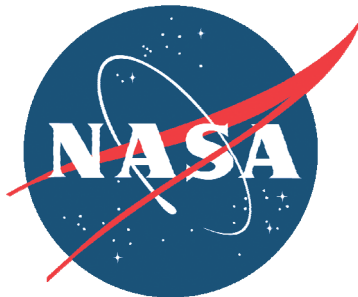
# Figure Verification of a Precision Ultra-Lightweight Mirror: Techniques and Results

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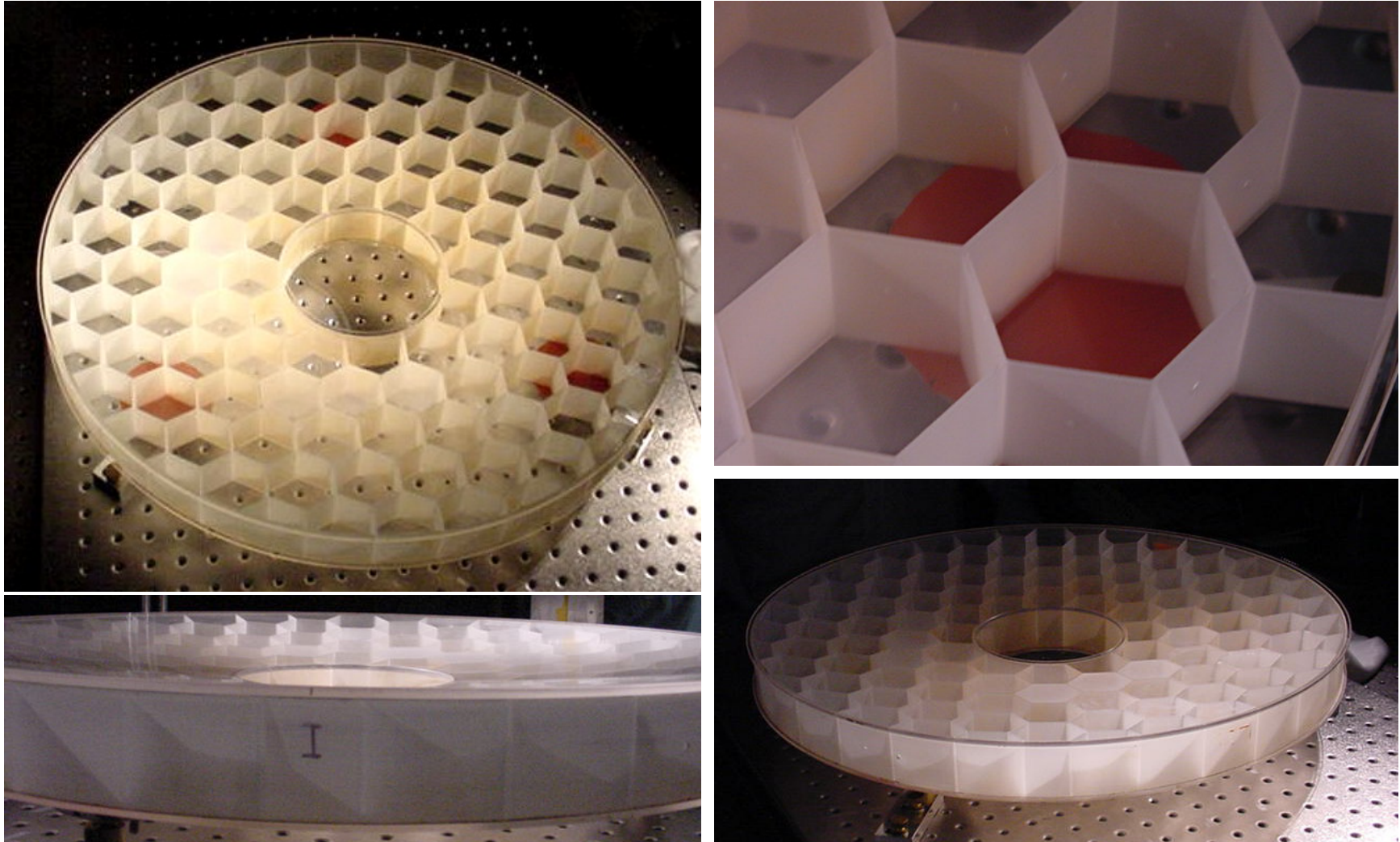
# Ultra-Lightweight Mirror Technology R&D:

Developing and testing the methodologies required to incorporate cutting-edge lightweight mirror technology in spaceflight missions.

- NASA/Goddard has dedicated internal research and development resources to advance methods of verifying and utilizing ultra-lightweight mirror technologies for spaceflight use.
- To test the feasibility of using ITT Space System's ultra-lightweight ULE architecture for diffraction limited applications in the EUV ( $\sim 120\text{nm}$ ), a demonstrator mirror was fabricated, polished, and furnished to GSFC.
- At GSFC the mirror was: coated, measured, mounted, and vibration tested

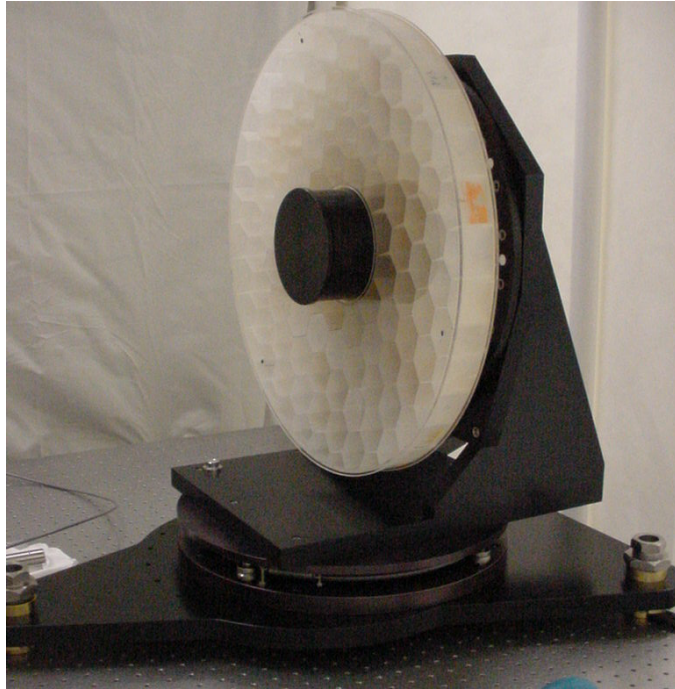


# Mirror Received in June 2003

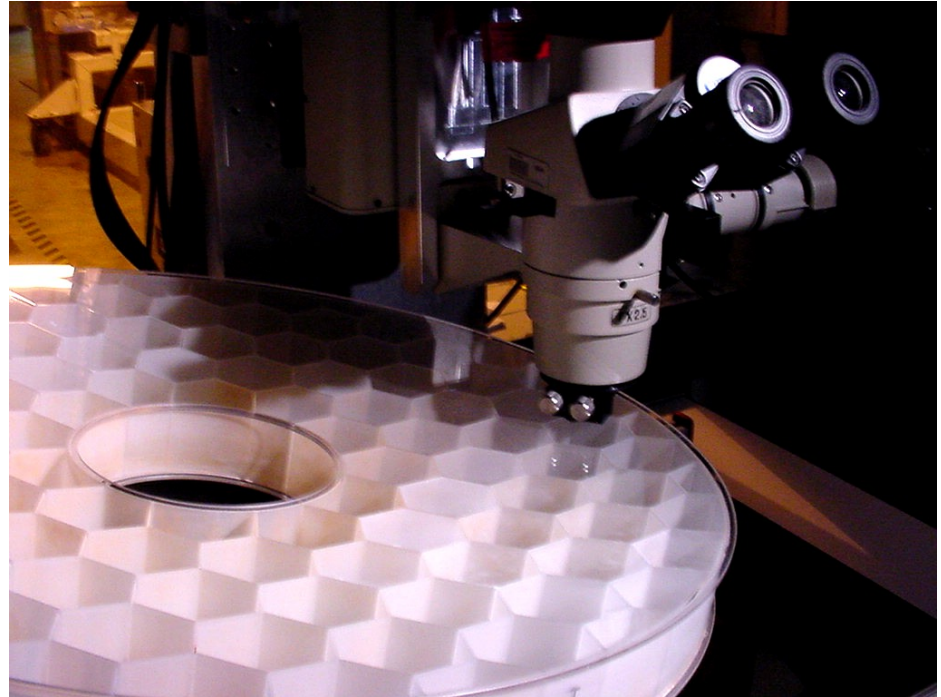


*Mirror during initial inspection. Starting at upper-left and moving clockwise: (a) from above, showing overall cell pattern and mount pad locations; (b) close up of one mount pad looking through front face; (c) foreshortened view looking across flat-flat symmetry line; (d) side view showing clocking marks*

# Fixturing and Initial Measurements



uncoated mirror in  
horizontal test fixture

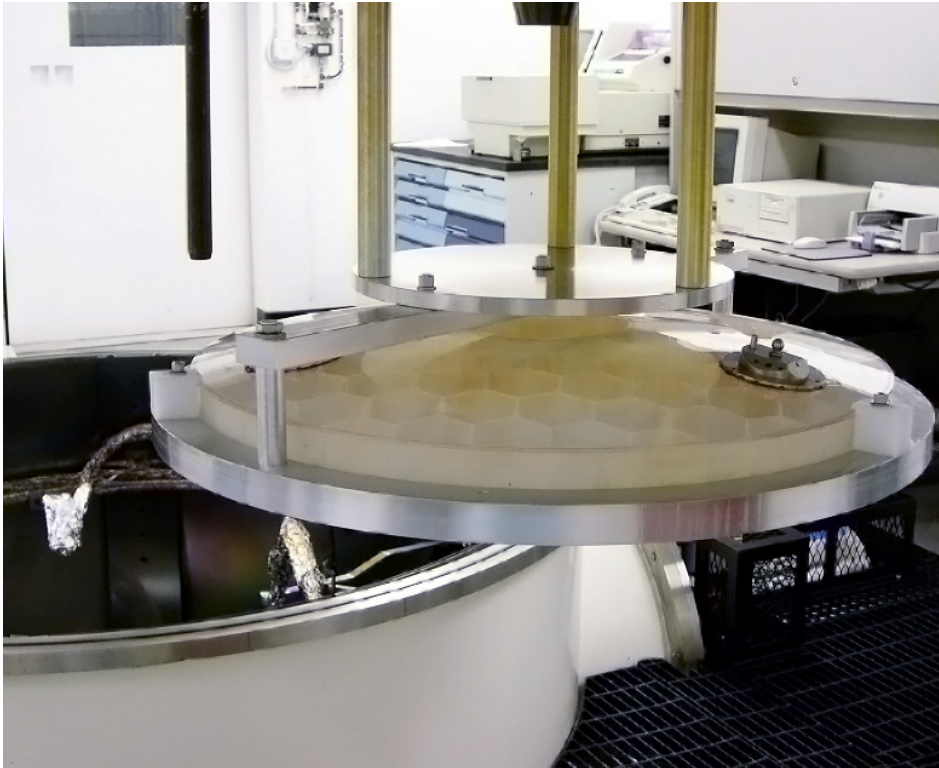


roughness measurements  
(*Topo2D Micro-interferometer*)



# Coating at Goddard

$\text{AlMgF}_2$  and  $\text{AlSiO}_2$

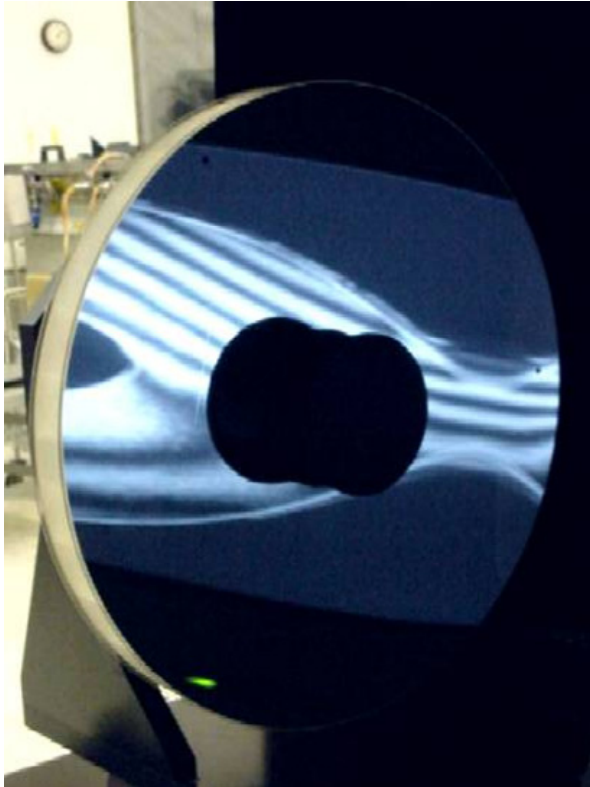


Mirror being loaded into  
Goddard's 2m coating chamber.

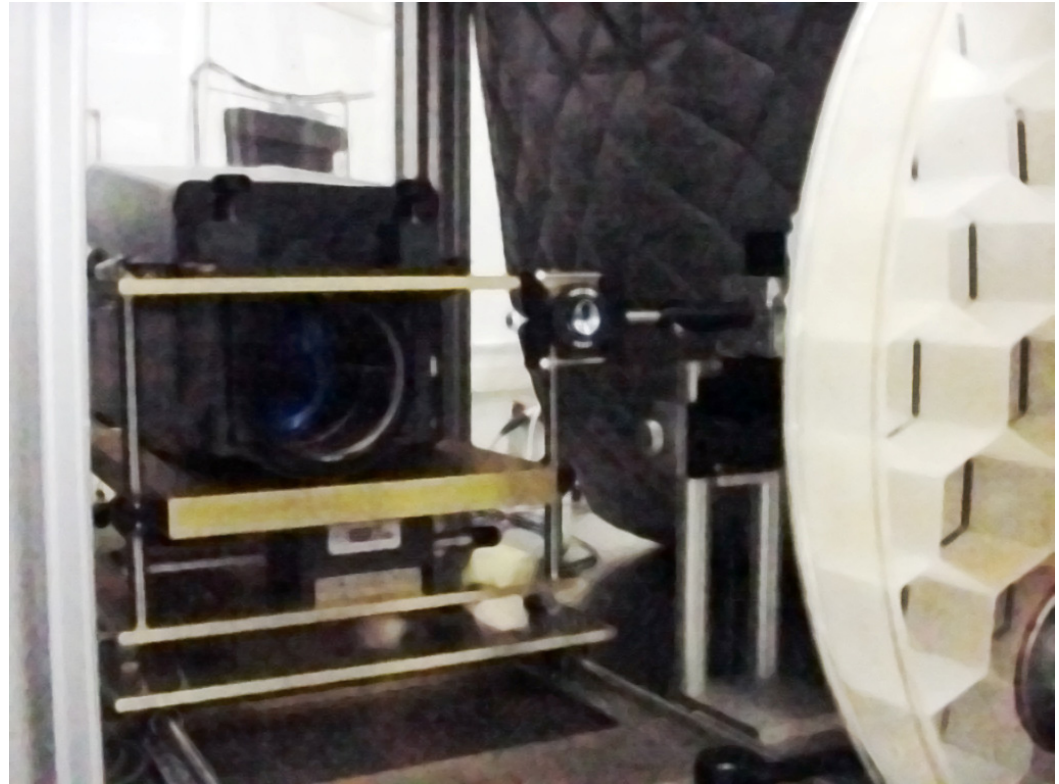


Looking up into the chamber at  
the mirror just before coating

# Horizontal Figure Metrology



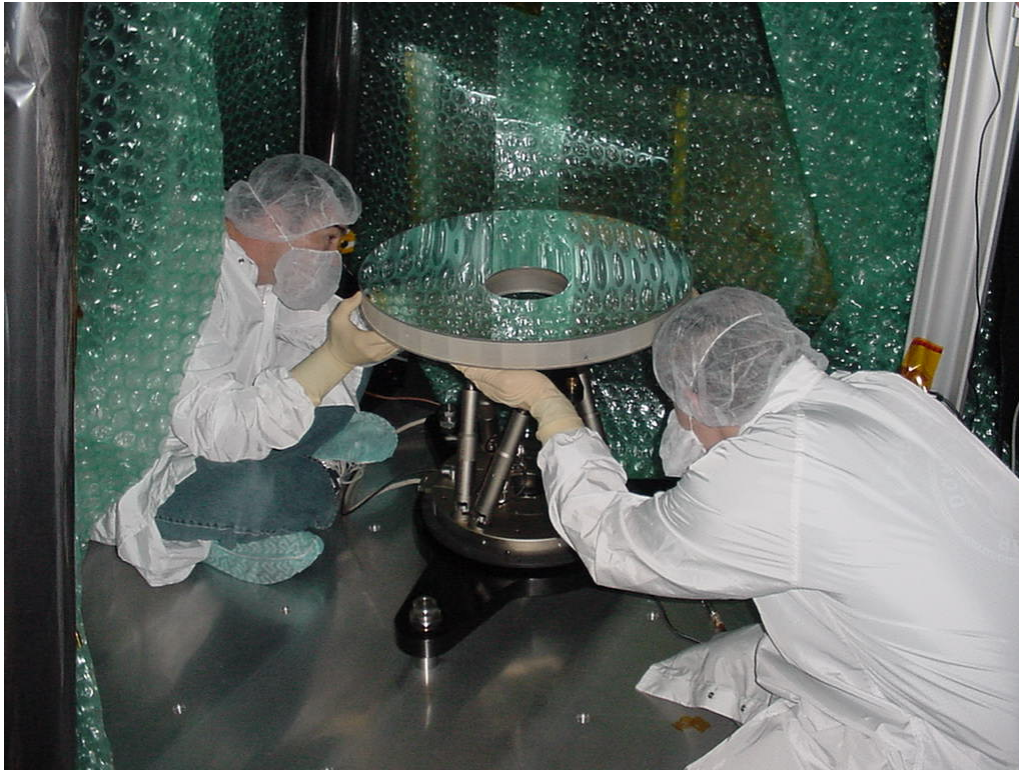
full aperture test



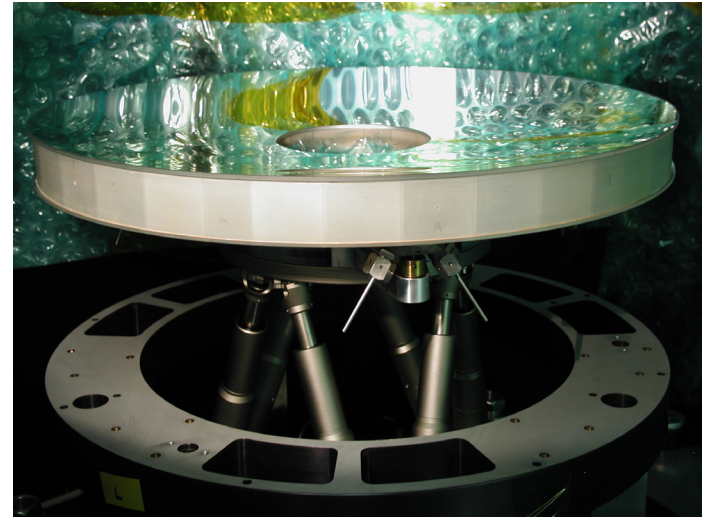
sub-aperture test



# Vertical Metrology and Mount Prep.



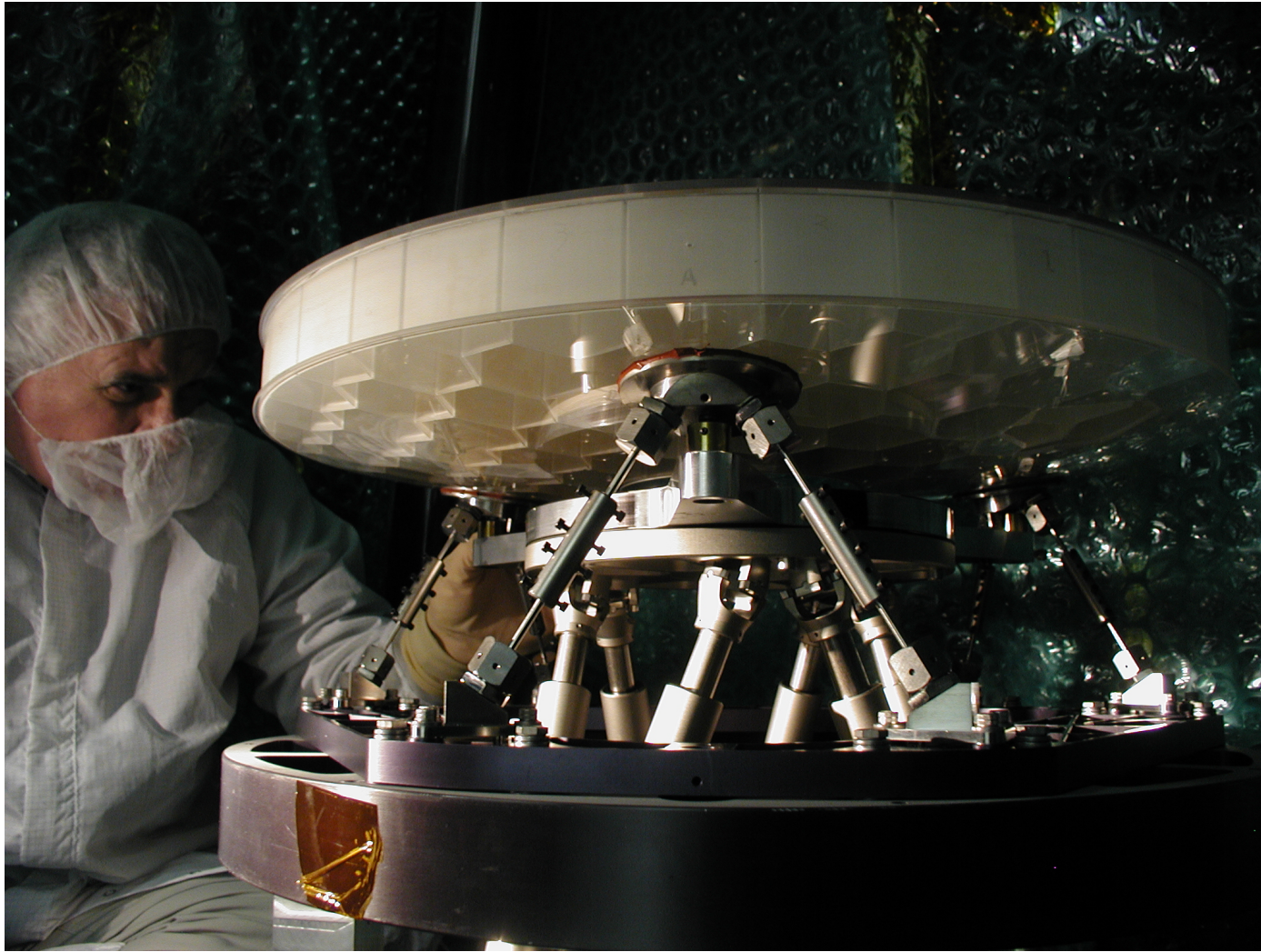
kinematic mount and hexapod  
positioner for vertical test



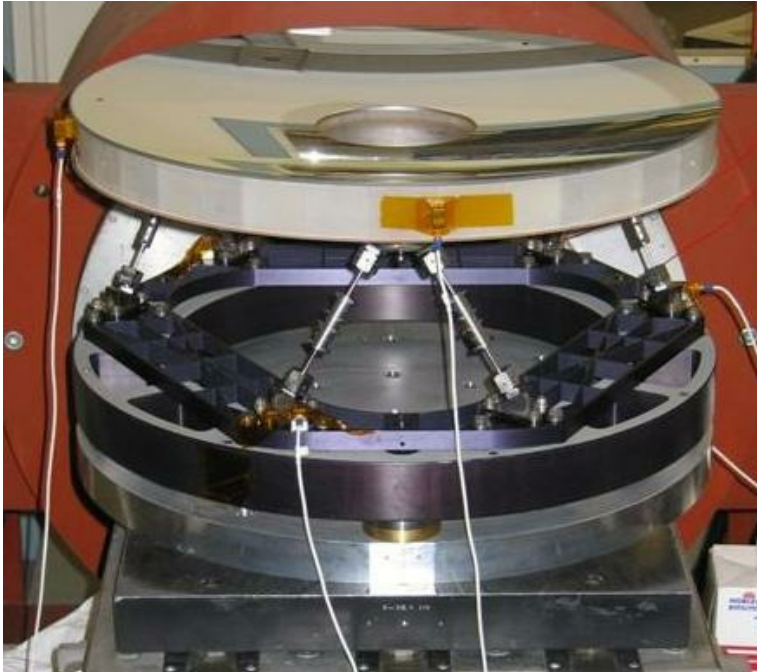
initial mounting steps



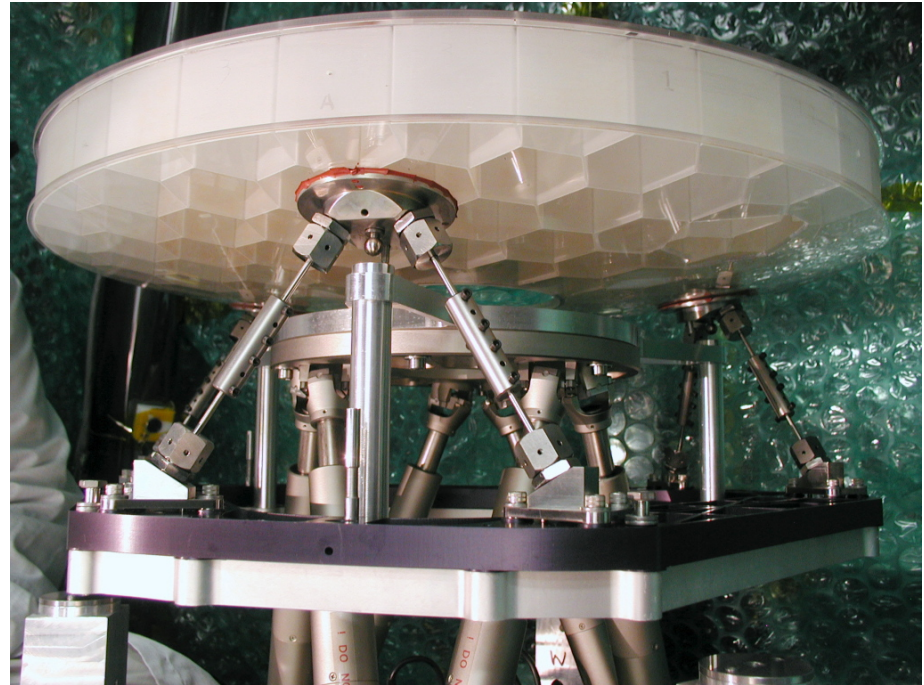
# Mounting and *in situ* Testing



# Qualification Tests



vibration tests at  
Goddard's Wallops  
Flight Facility



fixturing configuration for  
post-mount and post-vibe  
figure measurements

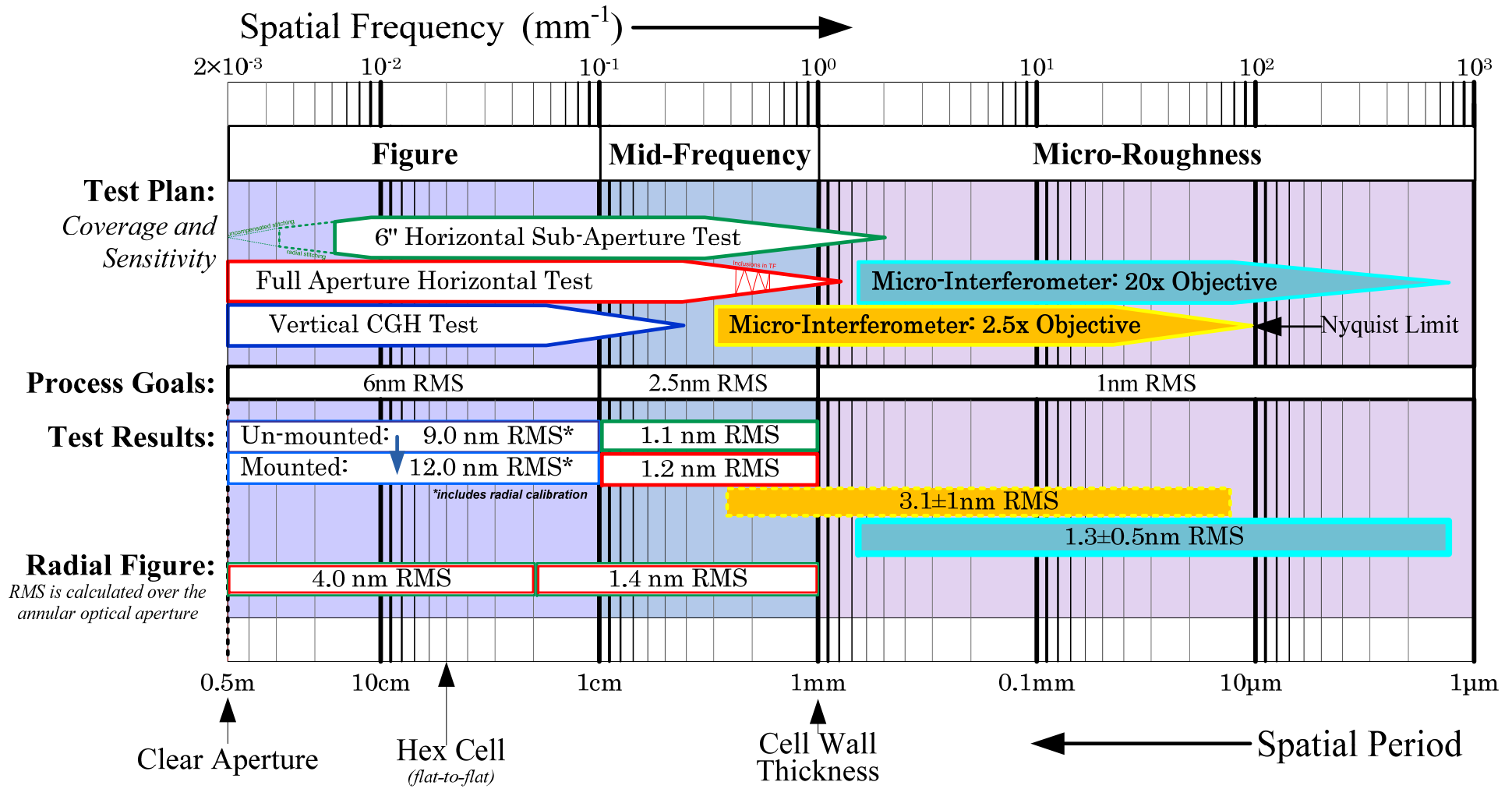
# Metrology Tactics

- Divide and conquer for “absolute” asphere testing
  - n-position test + independent radial test  $\approx$  “absolute”
  - test in vertical and horizontal orientations
  - test with an aspheric CGH null and by auto-collimation
- Split spatial frequency test requirements between separate test configurations
  - Capture mid-spatial frequencies ( $0.1\text{-}1\text{mm}^{-1}$ ) with a sub-aperture test
- Recovery: when good mirrors go bad
  - “forensic interferometry”

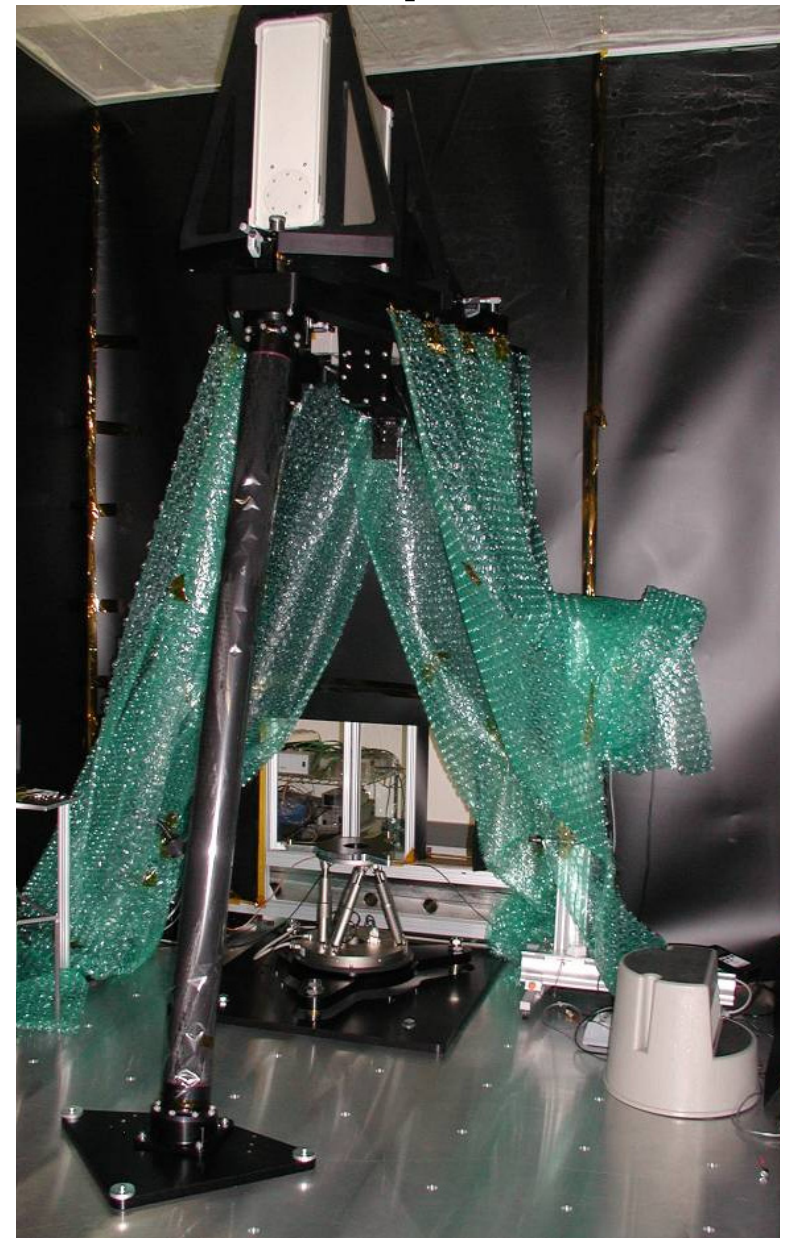
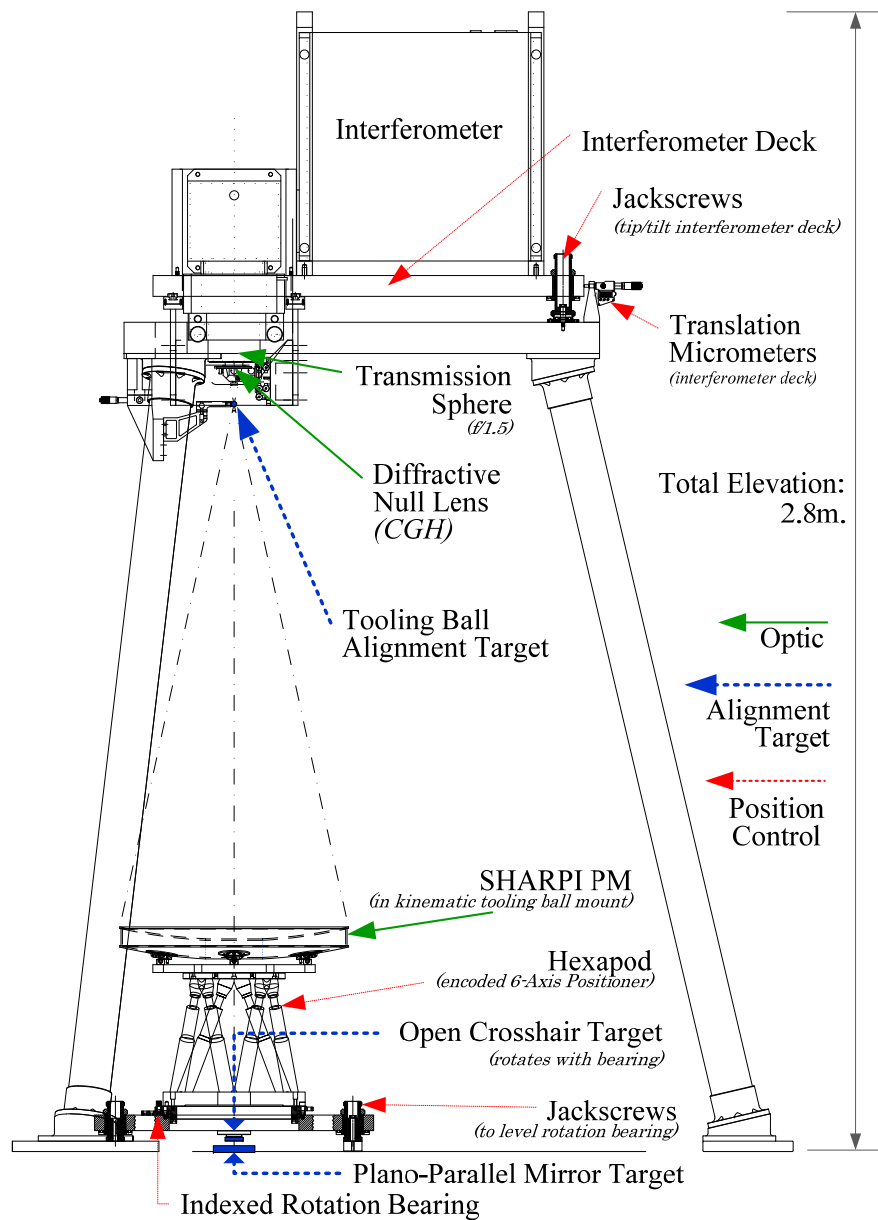


# Test Coverage and Results:

## Figure, Mid-Frequency, and Micro-roughness Errors

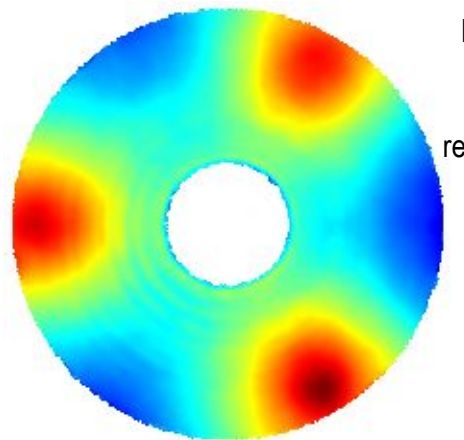


# Vertical Test Tower Setup



# Overview of Data Reduction: averaging, n-position rotations, and gravity backout

# Initial Figure Analysis & Decomposition



**Figure Measurement (1g)**

**RMS:71.5nm±2nm**

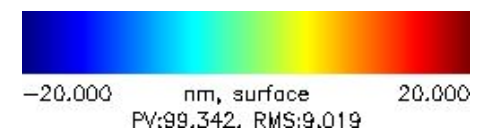
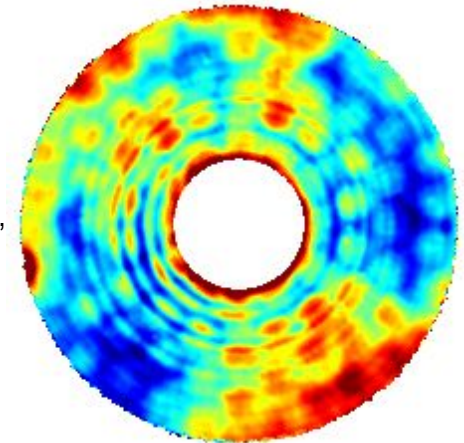
Corrections applied:  
reference wavefront, pupil distortion



**Figure Measurement (0g)**

**RMS:9.0nm±2nm**

Corrections applied:  
NASTRAN predicted 1g deformation,  
CGH null radial profile calibration



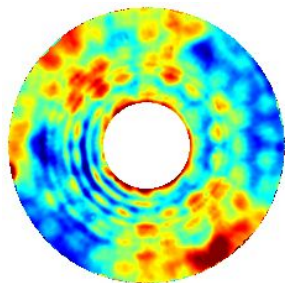
## Measuring 0g Mirror Figure

*Measuring precise lightweight mirrors in the presence of large gravity deformations*

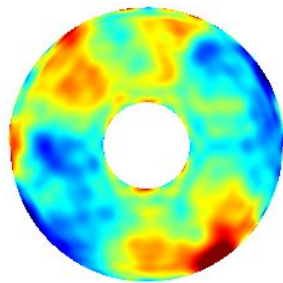
scale magnification: x10

## Error Analysis & Decomposition

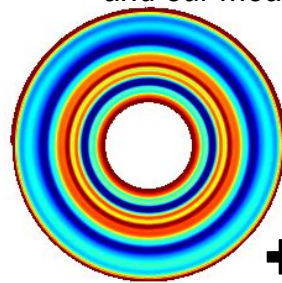
*Understanding the magnitude and character of the mirror figure error and our measurement uncertainty.*



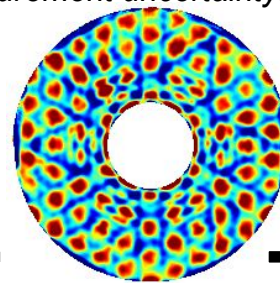
**Total 0g Error**  
**RMS:9.0nm±2nm**



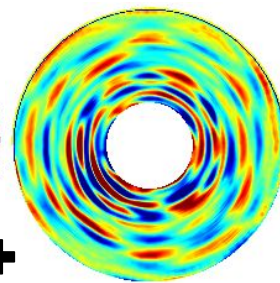
**Asymmetric Figure Error**  
**RMS:7.3nm±1nm**



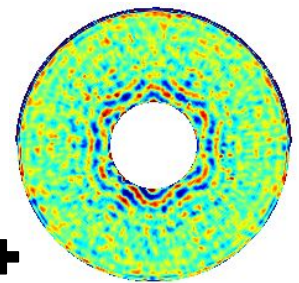
**Symmetric Radial Error**  
**RMS:4.0nm±0.2nm**



**"Quilting" Error**  
**RMS:2.3nm±0.4nm**



**Semi-Symmetric Error**  
**RMS:1.9nm±0.2nm**



**Residual**  
**RMS:1.1nm±0.2nm**



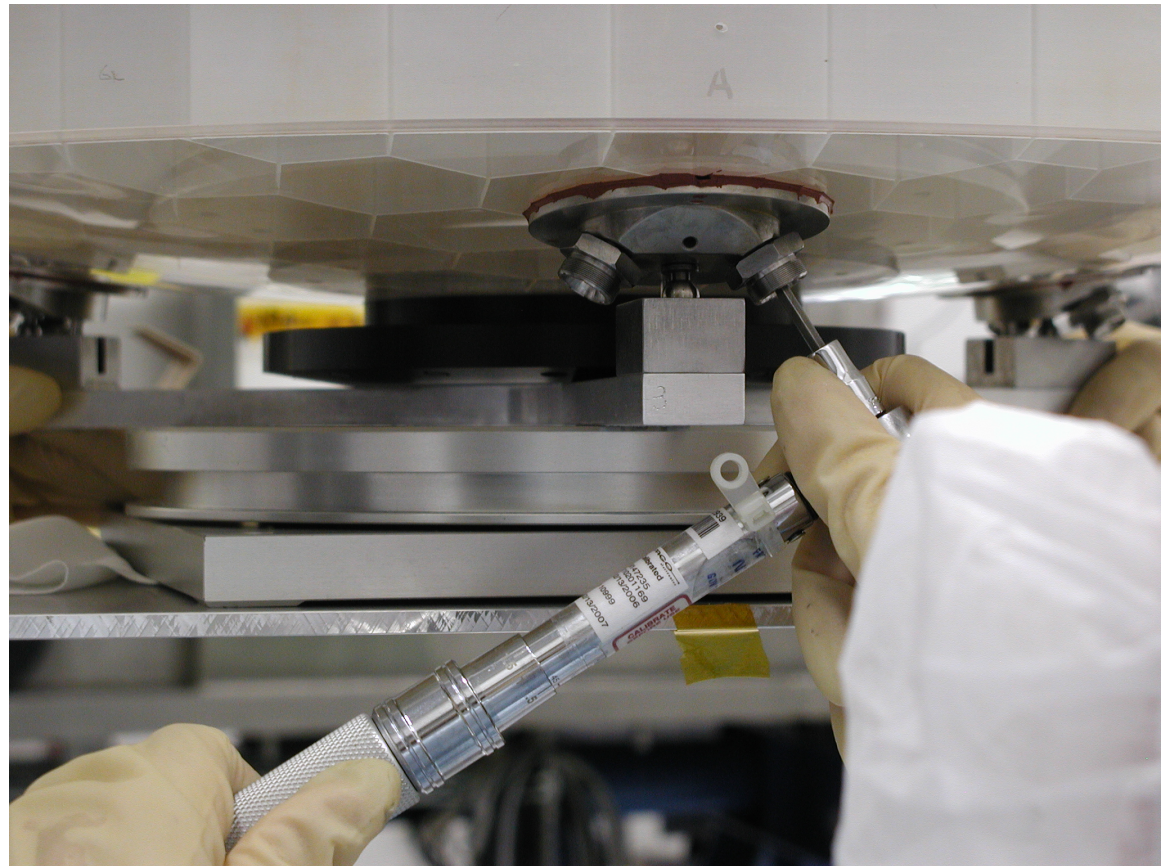
scale magnification: x5





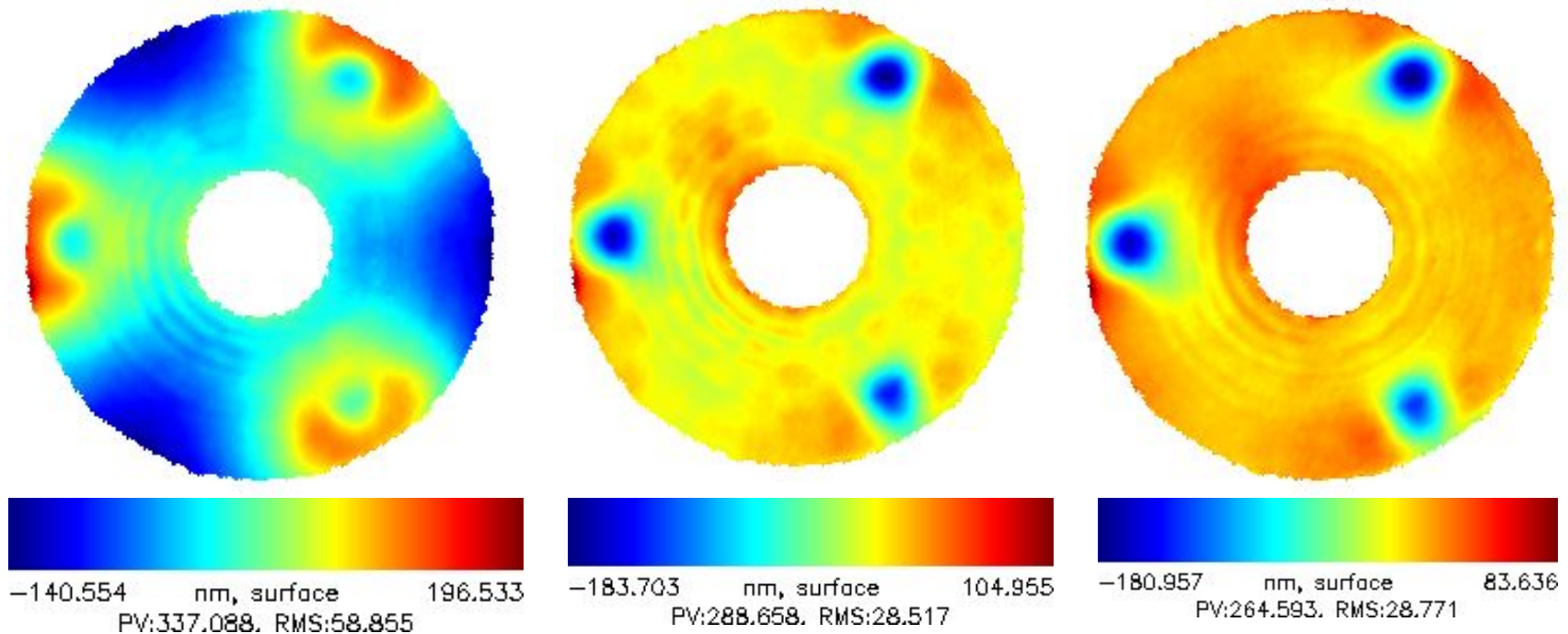
# Mounting with Metrology

Mirror figure measurements taken during the mounting process immediately became an essential source of feedback.



The first pieces of mount hardware attached to the mount pads were coupling sockets...

... and the mirror distorted.  
*from 9 nm RMS to 29 nm RMS!*



Averaged 1g

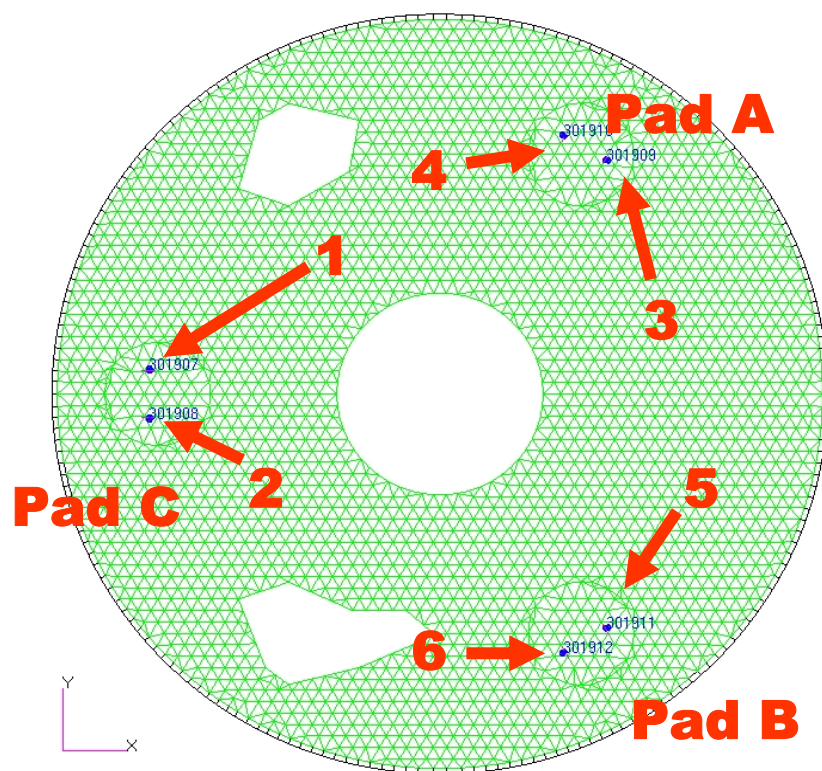
Averaged 0g

*data projected onto the XY plane*

ΔFigure from  
Initial 0g

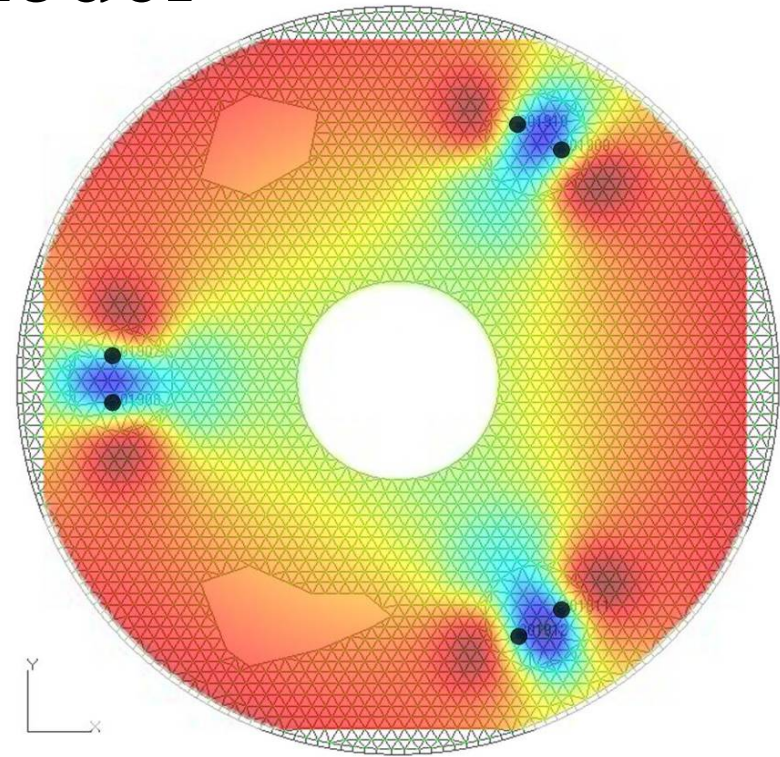


# Fastener stresses were added to the finite element model –



FEM Model

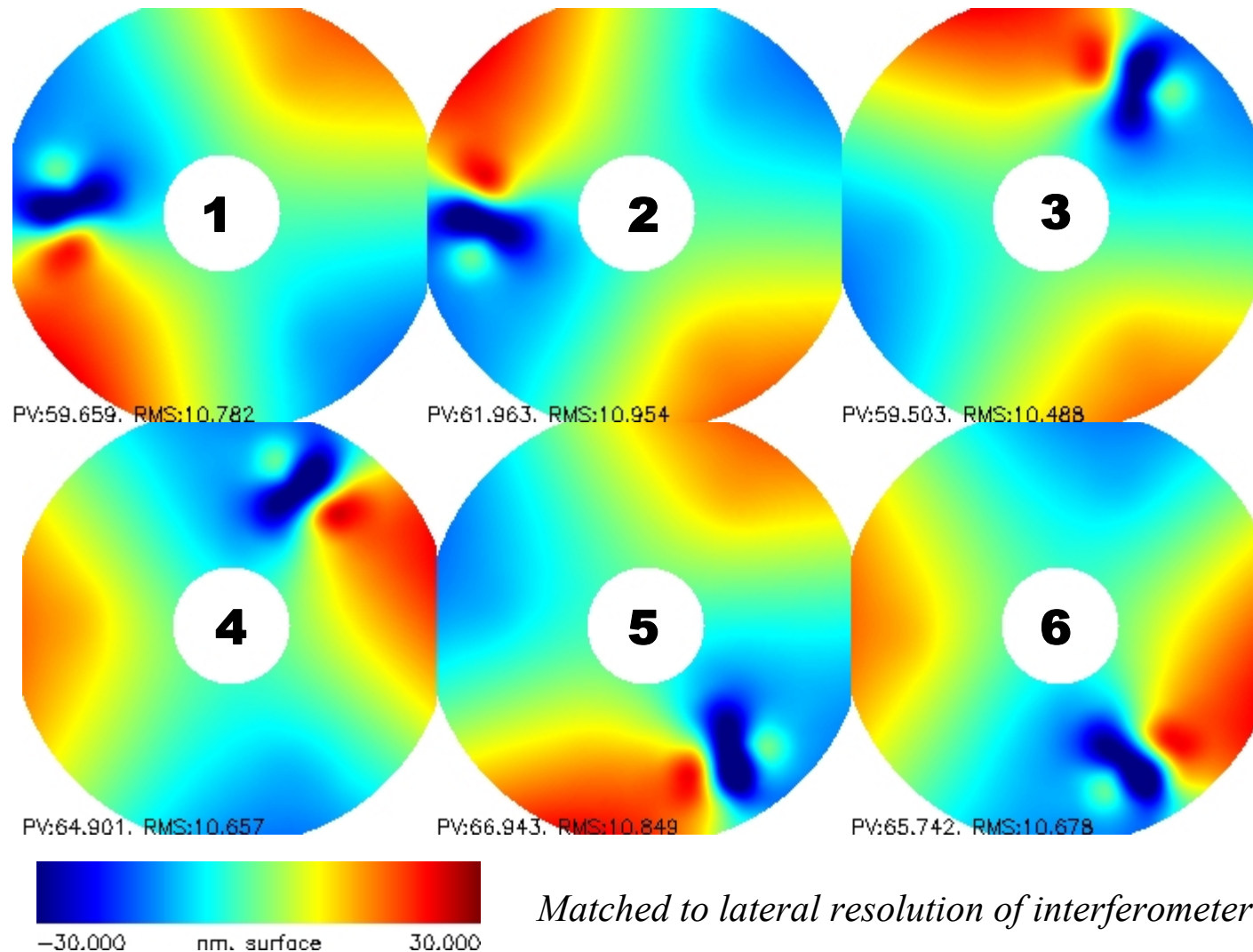
A 1000lbF preload was modeled at nodes corresponding to the location of each screws pair in each mount pad.



-75.097      nm, surface      29.312  
PV:104.409. RMS:16.766

Distortion Prediction  
(rigid body motion subtracted)

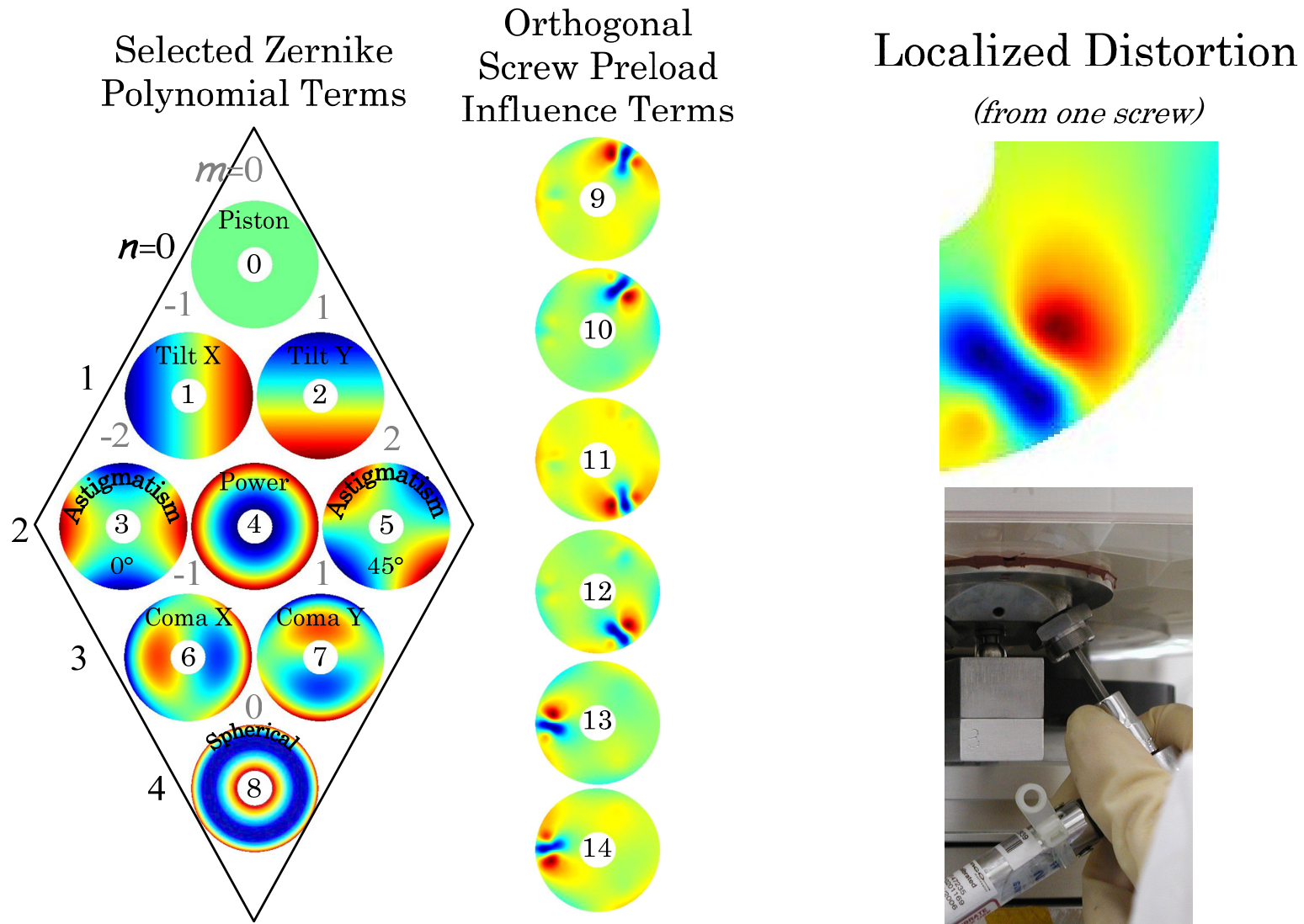
Considering each screw preloads separately,  
there are six “influence functions”:



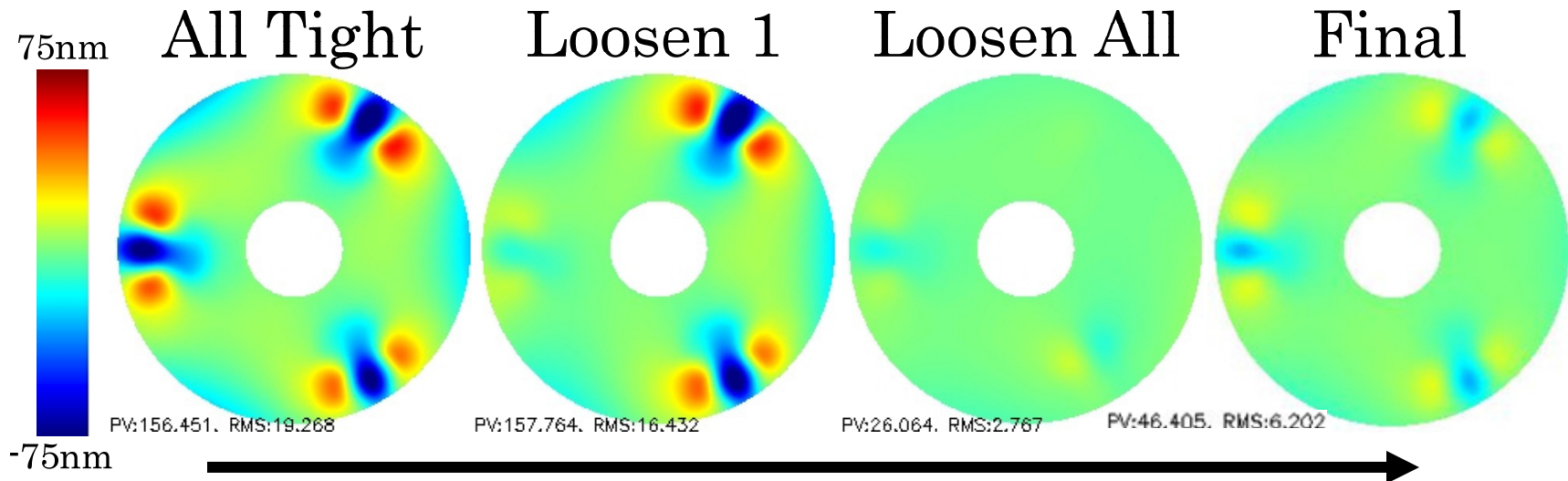


# An Orthonormal “Screw” Basis:

The FEM influence functions are orthonormalized with standard Zernike terms to produce an analysis tool that correlates wavefront shape to mechanical conditions.



# Using the FEM Basis for Visualization and Prediction

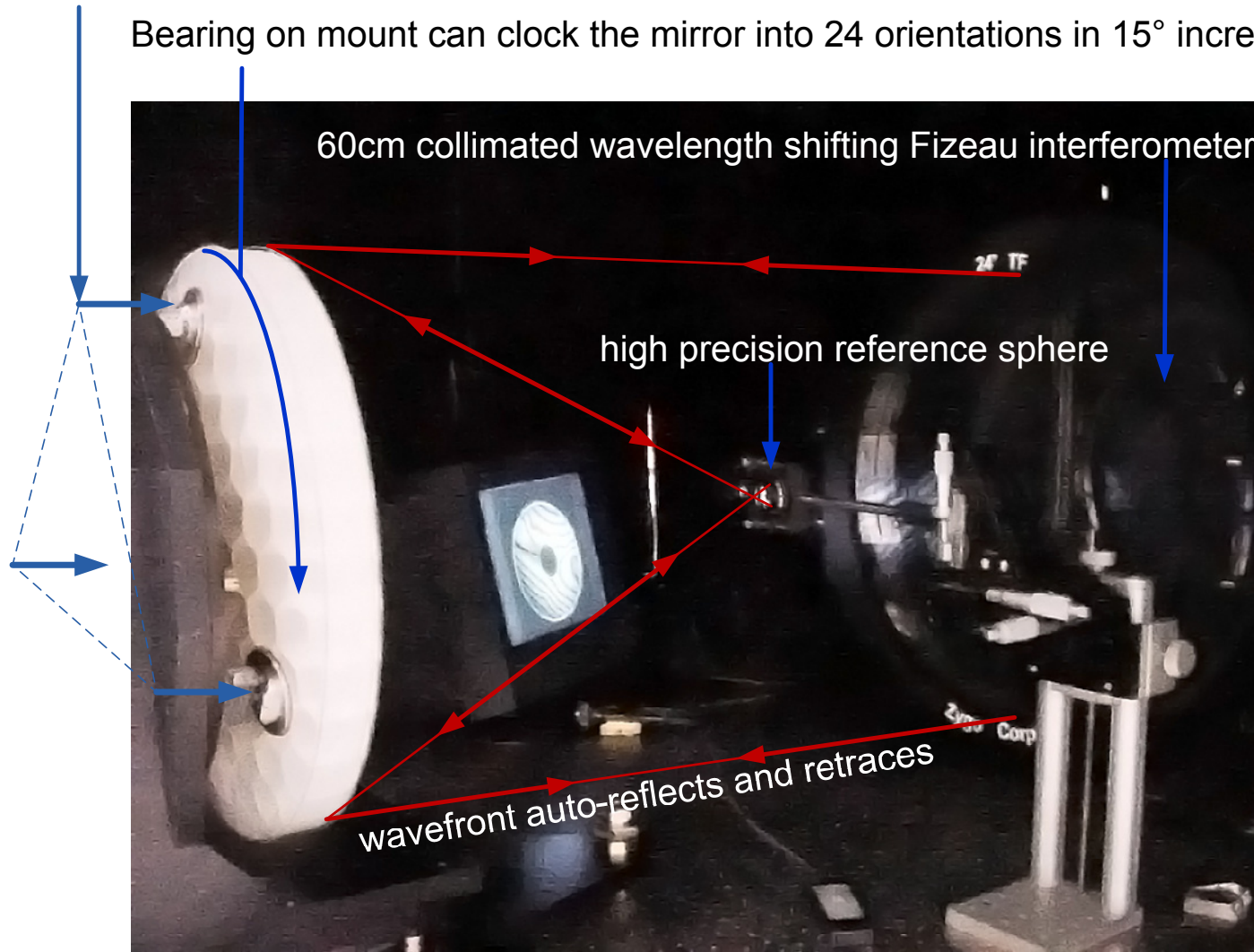


Using this FEM decomposition, the basis coefficients corresponding to screw-induced distortions show a linear dependence on the torque preload. With a few calibrated steps, it was possible to empirically determine the coupling and derive an acceptable torque value along with a prediction of the final surface figure. Over these FEM basis coefficients, the predicted distortion matched the final distortion within 1nm RMS

# Horizontal Full-Aperture Testing

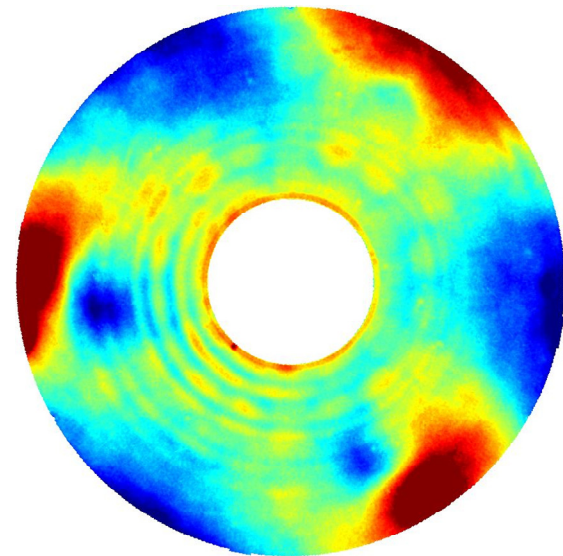
Three mount to tooling ball interfaces

Bearing on mount can clock the mirror into 24 orientations in  $15^\circ$  increments



# ... another case for forensics

- The process of capturing the mirror in the horizontal fixture captured an unknown strain and resulted in a significant amount of mirror distortion during horizontal testing
- Vertical test data confirmed the horizontal mount was the culprit, but horizontal metrology was our only planned independent measurement of radial figure.
- Using a similar FEM-basis analysis, it was possible to separate the mount-induced distortion from mirror figure and confidently determine the radial figure.

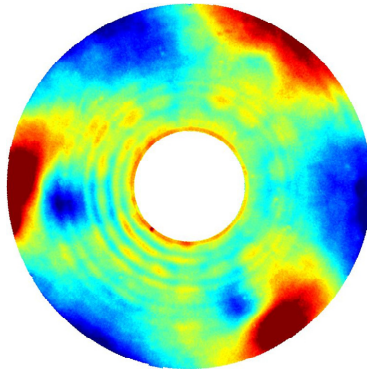


22.2nm RMS

24x15° n-position test, averaged,  
and 1g backout applied



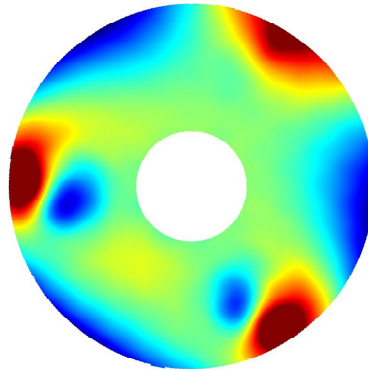
Horizontal  
Measurement\*



22.2nm RMS  
\*reduced, averaged, and  
1g compensated

=

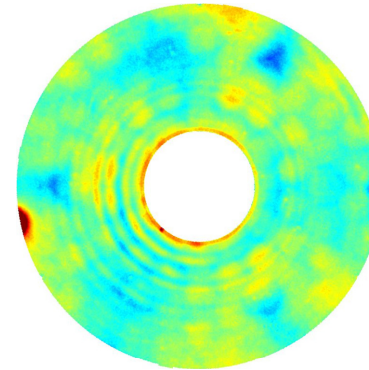
Distortion Solution



20.5nm RMS

+

Residual:  
*0g Figure*



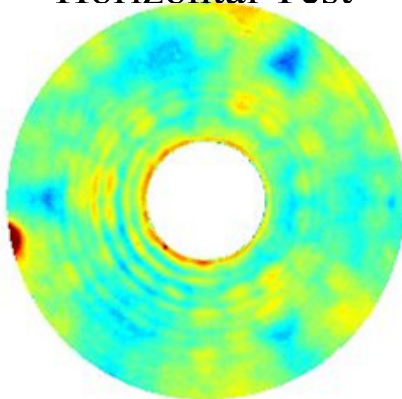
8.1nm RMS

50nm



-50nm

0g Figure Result:  
Horizontal Test

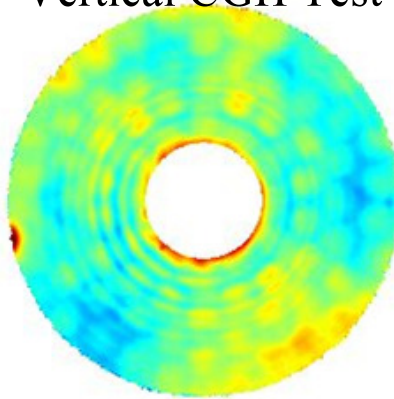


8.2nm RMS

(as calculated from distortion solution,  
transformed into vertical CGH dataspace)

-

0g Figure Result:  
Vertical CGH Test

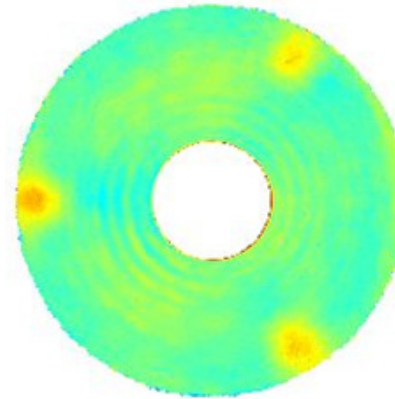


9.0nm RMS

(most accurate 0g figure measurement, data  
corrected for axi-symmetric errors)

=

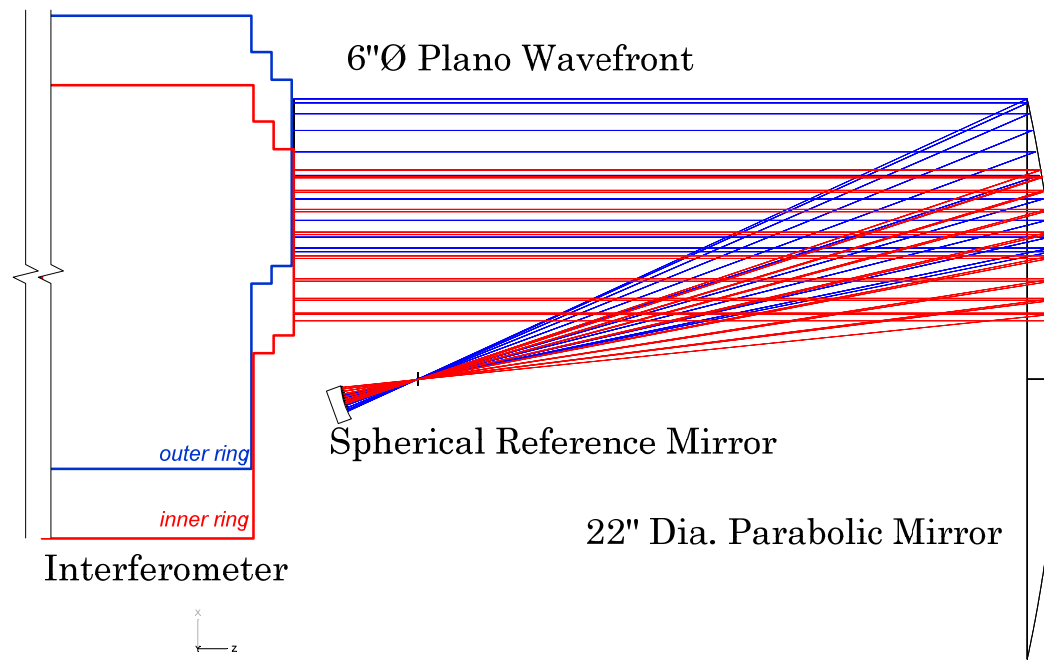
Residual:



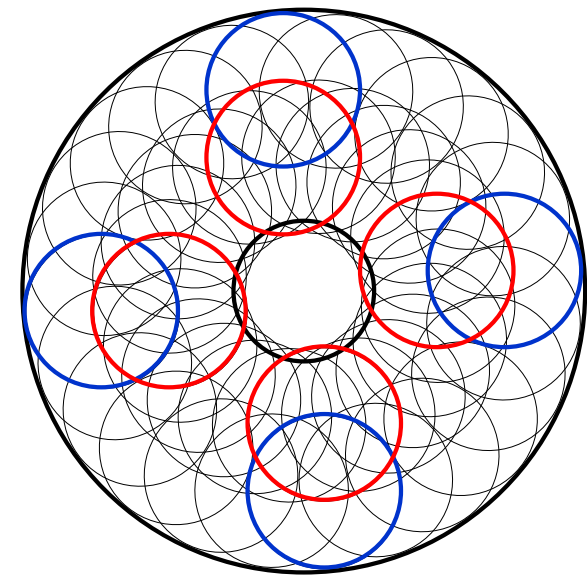
4.9nm RMS

# Horizontal Sub-Aperture Tests

- Measurement of mid-spatial frequency errors
- Higher resolution radial figure measurement, overlap with full-aperture result



Layout



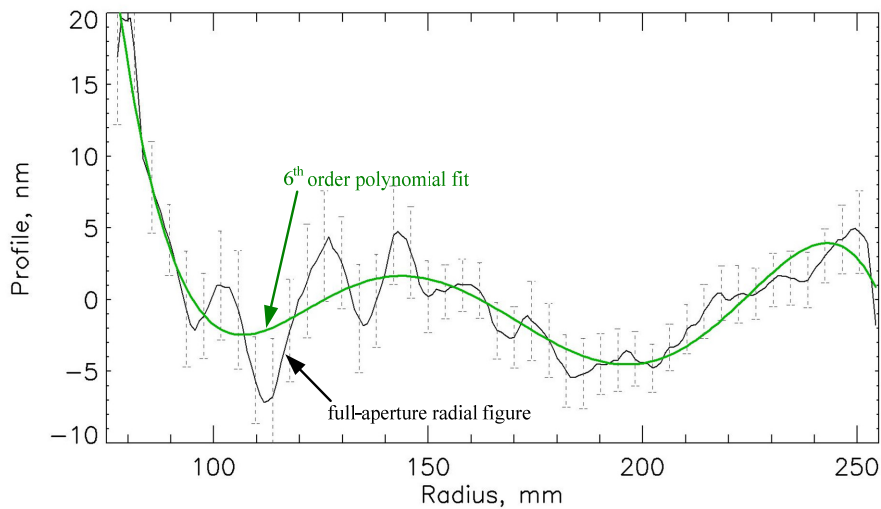
Sub-Aperture Coverage

Sub-Apertures Total: 48

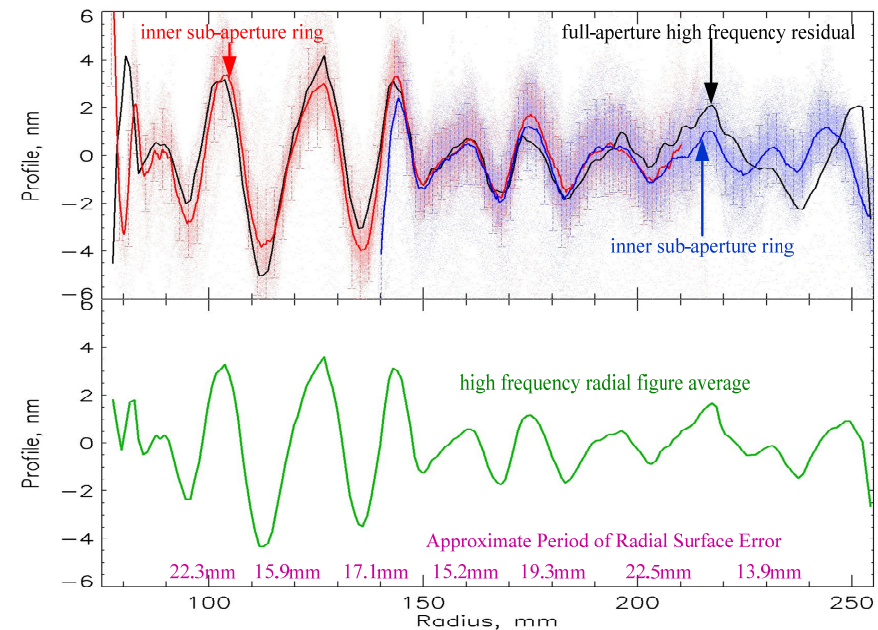
24 measurements on **inner (red)** and **outer (blue)** ring in 15° increments about the parent vertex

# Total Radial Profile Derived from the Low Frequency Radial Figure and the High Frequency Radial Figure

Low Frequency Radial Figure  
*from the full-aperture horizontal test*

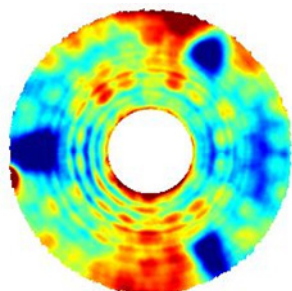


High Frequency Radial Figure



Full-aperture horizontal test data and sub-aperture test data are combined to give an independent measurement of the radial figure over a large spatial frequency range.

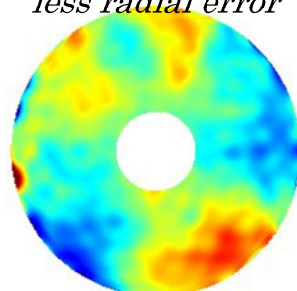
**Final Figure:**  
Mounted &  
Vibe Tested



170nm P-V,  
12.5nm RMS

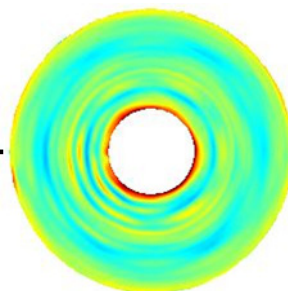


**Figuring Error**  
*less radial error*



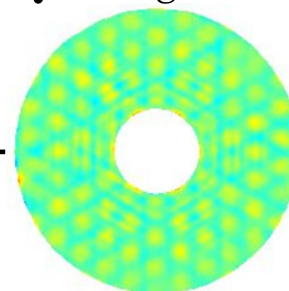
86.1nm P-V,  
7.3nm RMS

**Radial Error**



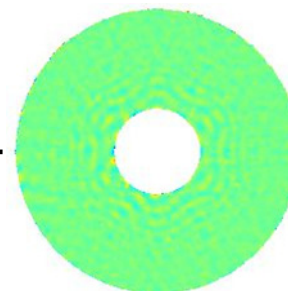
47.3 nm P-V,  
4.4 nm RMS

**Quilting Error**



22.5 nm P-V,  
2.3 nm RMS

**Residual**

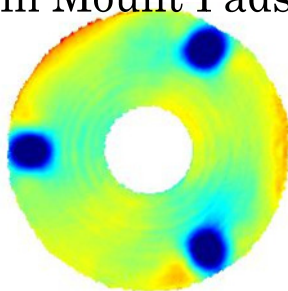


34.1 nm P-V,  
1.1 nm RMS

**Initial Figure Error**

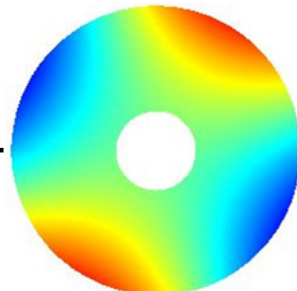
**+**

$\Delta$ Figure from  
Fasteners  
in Mount Pads



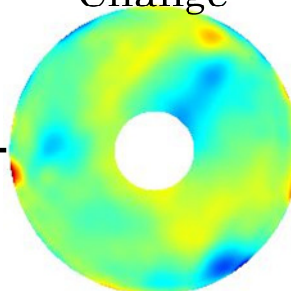
72.4 nm P-V,  
8.8 nm RMS

$\Delta$ Astigmatism



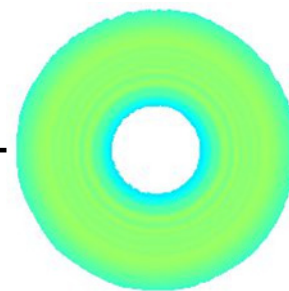
34.5 nm P-V,  
7.3 nm RMS

Residual  
Global Figure  
Change



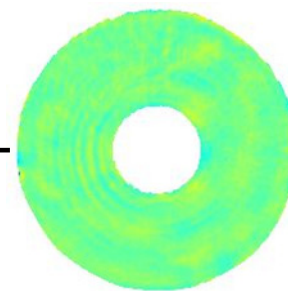
50.8nm P-V,  
4.0nm RMS

Radial  
Change



8.9 nm P-V,  
1.9 nm RMS

Residual  
Change



25.1 nm P-V,  
1.2 nm RMS

**Changes Through Mount and Vibe**



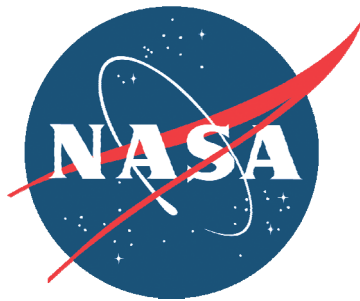
# Accomplishments:

- Successfully adapted existing capabilities and facilities
  - coating, roughness metrology, fixture design and fabrication
- Performed an absolute 0g figure test on an ultra-lightweighted aspheric mirror with ~2nm RMS accuracy.
  - Addressed aspheric null certification, gravity back-out verification, and much more...
- Mounted mirror to a flight interface without inducing significant distortion, passed component vibration testing, and maintained surface figure through vibe

# *Thanks...*

- Our success would not have been possible without the dedicated efforts of: David Content, Doug Rabin, Thomas Wallace, Shane Wake, Jeff Bolognese, Sandra Irish, Craig Stevens, Jeff Gum, and many more...
- Funding provided by NASA/Goddard Space Flight Center IRAD program. Telescope I&T funds provided through PICTURE sounding rocket project, managed through Boston University.
- Questions?
  - I would be happy to answer additional questions by email:
    - [Scott.Antonille@nasa.gov](mailto:Scott.Antonille@nasa.gov)

# Backup Slides...



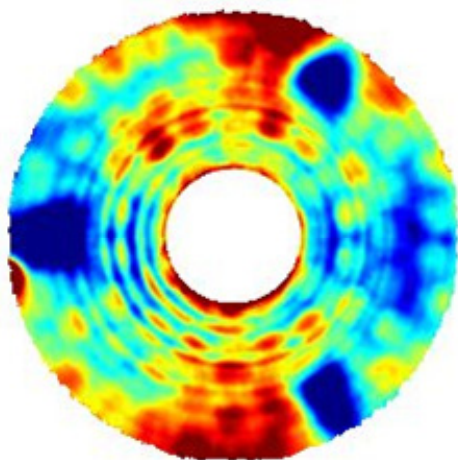
**Scott Antonille**  
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National Aeronautics and Space Administration  
Goddard Space Flight Center  
Optics Branch

Scott.Antonille@nasa.gov  
301.286.5669  
Fax: 301.286.0204

# Total Figure Change:

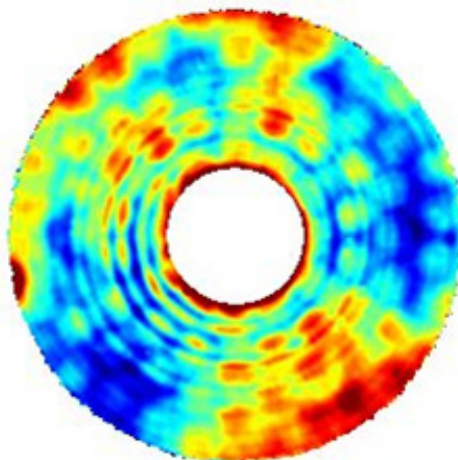
Mounted,  
Vibr. Tested



12.5nm RMS

-

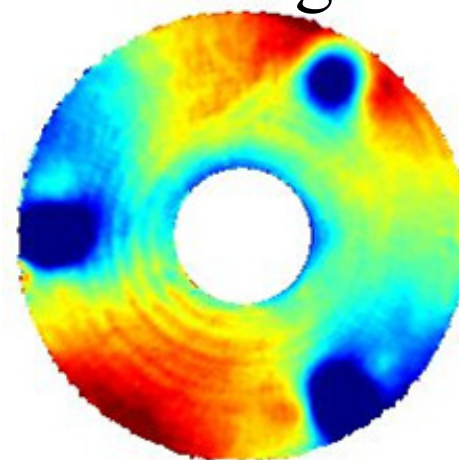
Un-Mounted



8.9nm RMS

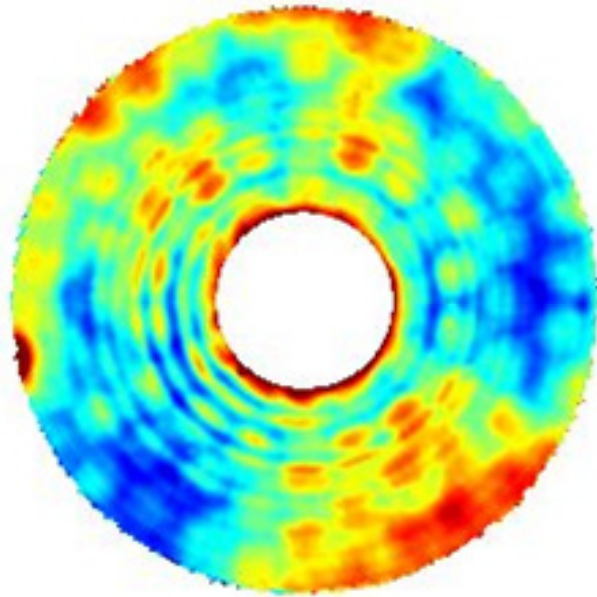
=

Measured Figure  
Change



11.8nm RMS

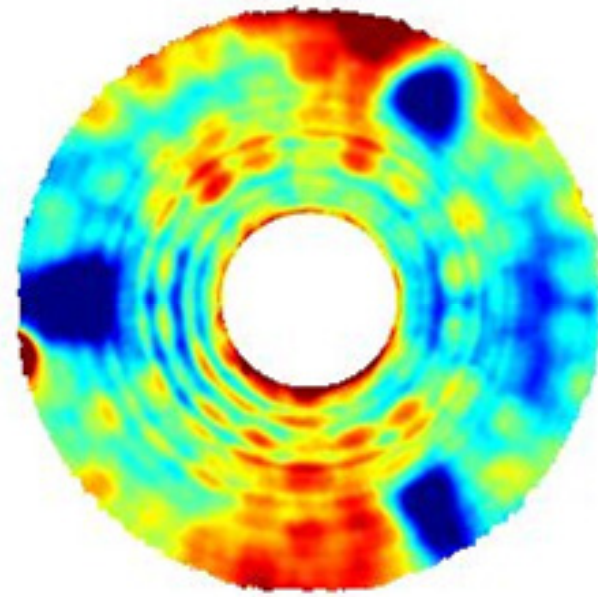
# Initial



95.1 nm P-V,  
8.9nm RMS



# Final



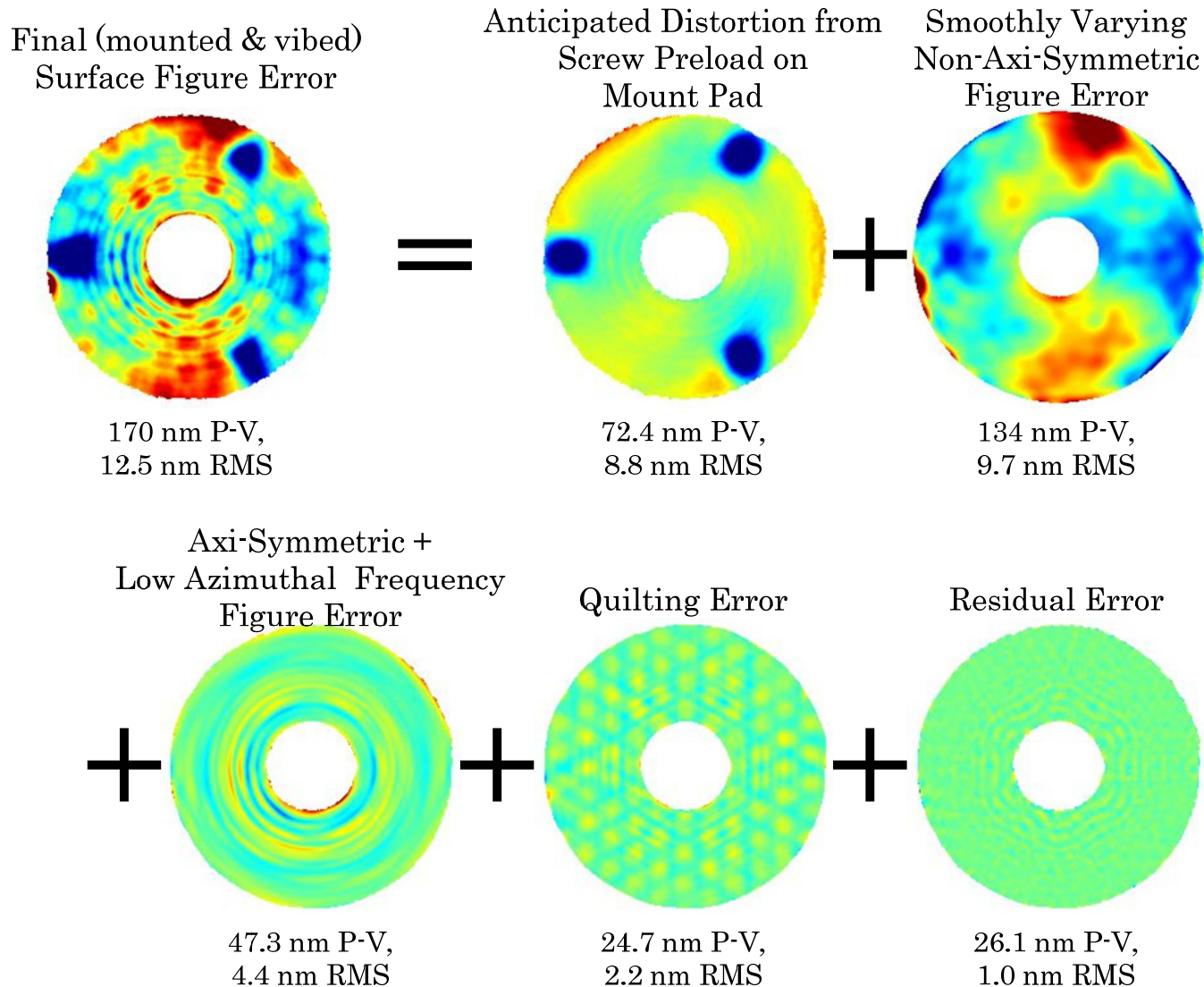
170 nm P-V,  
12.5 nm RMS



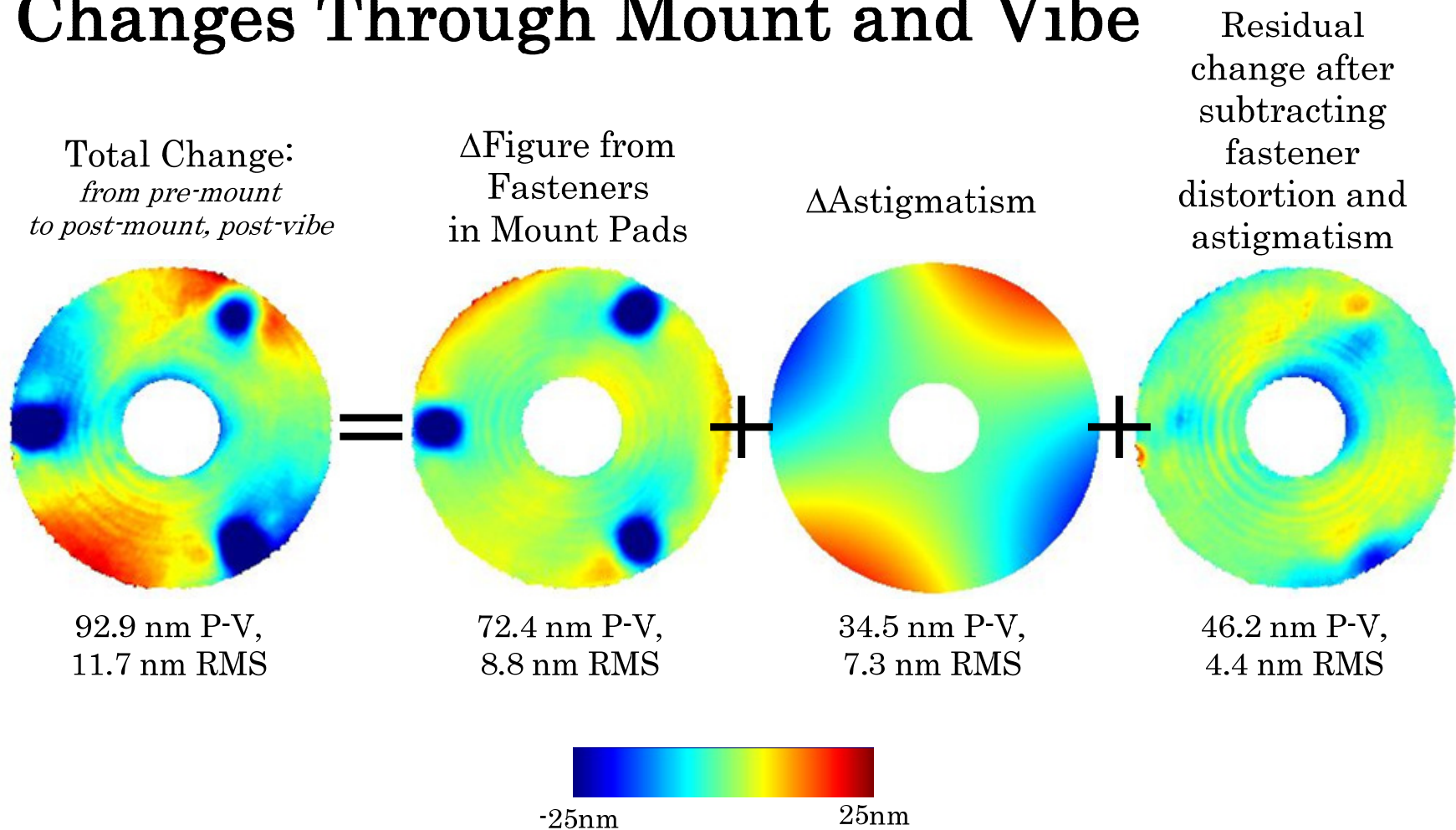
- Initial Vertical CGH measurement.
- Gravity sag subtracted.
- Radial CGH figure correction applied.
- Data has been transformed into the final measurement coordinate system, and therefore there are minor changes in RMS and PV from the initial measurements as reported in their initial coordinate frame
- This result includes all error terms except rigid body motion and the Zernike power term as normalized over the discretely sampled annular aperture.

- Post-Mount, Post-Vibe Test Vertical CGH measurement.
- Gravity sag subtracted.
- Radial CGH figure transformed into final data space and applied. Result includes any changes in radial figure.
- This result includes all error terms except rigid body motion and the Zernike power term as normalized over the discretely sampled annular aperture.

# Decomposition of Final Surface Figure



# Changes Through Mount and Vibe





# Horizontal Full-Aperture Test

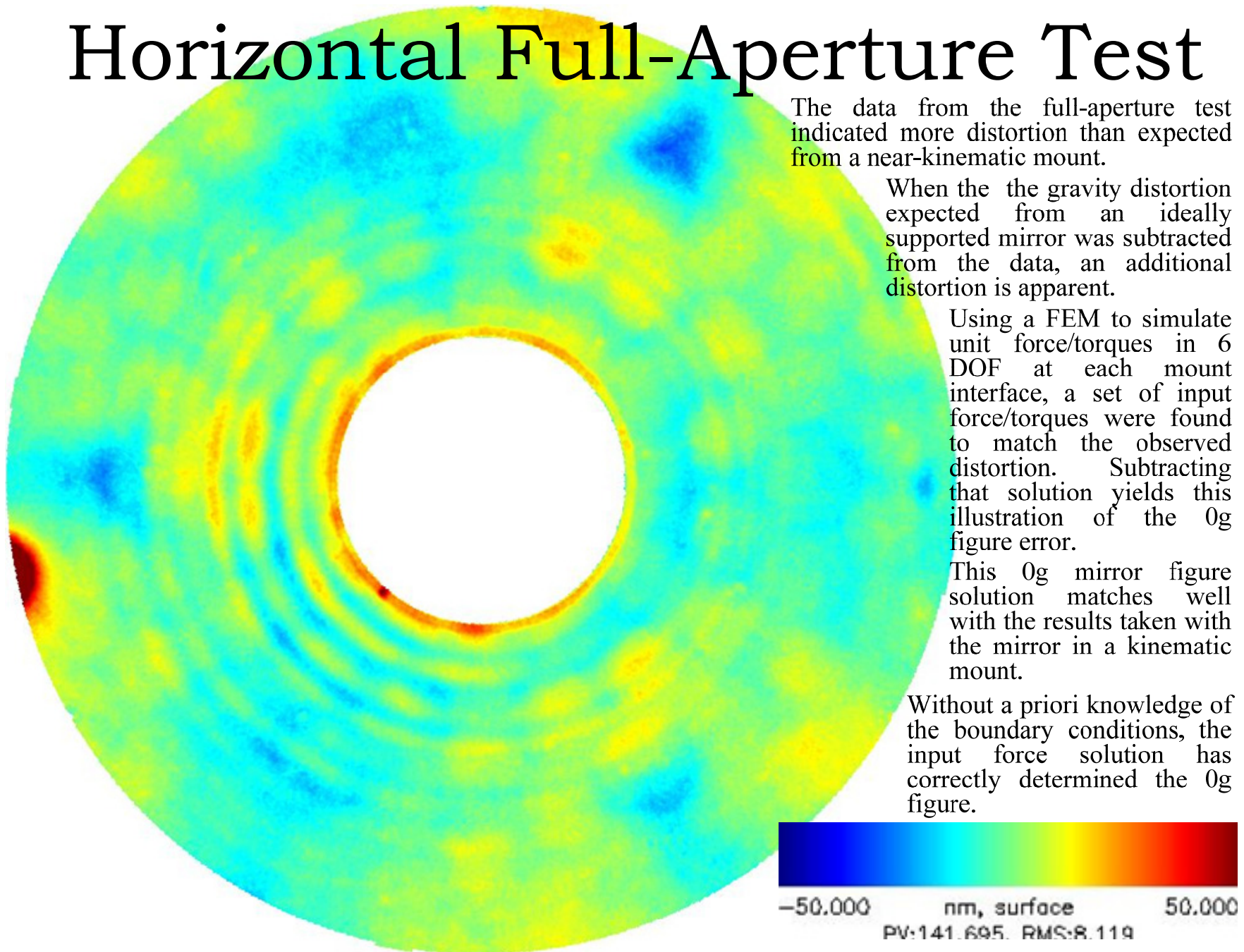
The data from the full-aperture test indicated more distortion than expected from a near-kinematic mount.

When the the gravity distortion expected from an ideally supported mirror was subtracted from the data, an additional distortion is apparent.

Using a FEM to simulate unit force/torques in 6 DOF at each mount interface, a set of input force/torques were found to match the observed distortion. Subtracting that solution yields this illustration of the 0g figure error.

This 0g mirror figure solution matches well with the results taken with the mirror in a kinematic mount.

Without a priori knowledge of the boundary conditions, the input force solution has correctly determined the 0g figure.



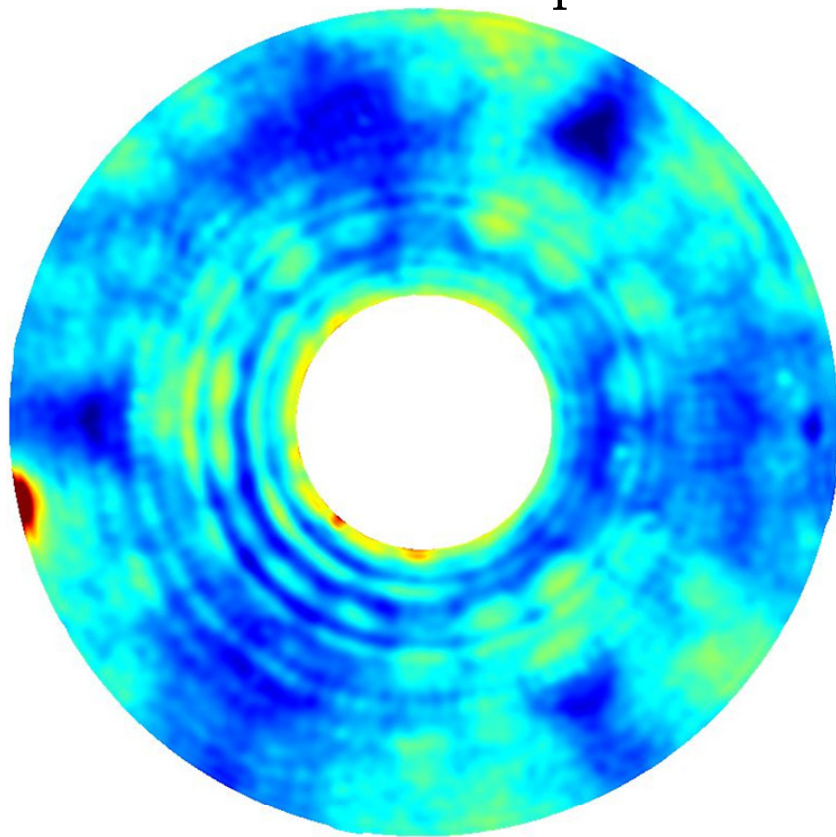
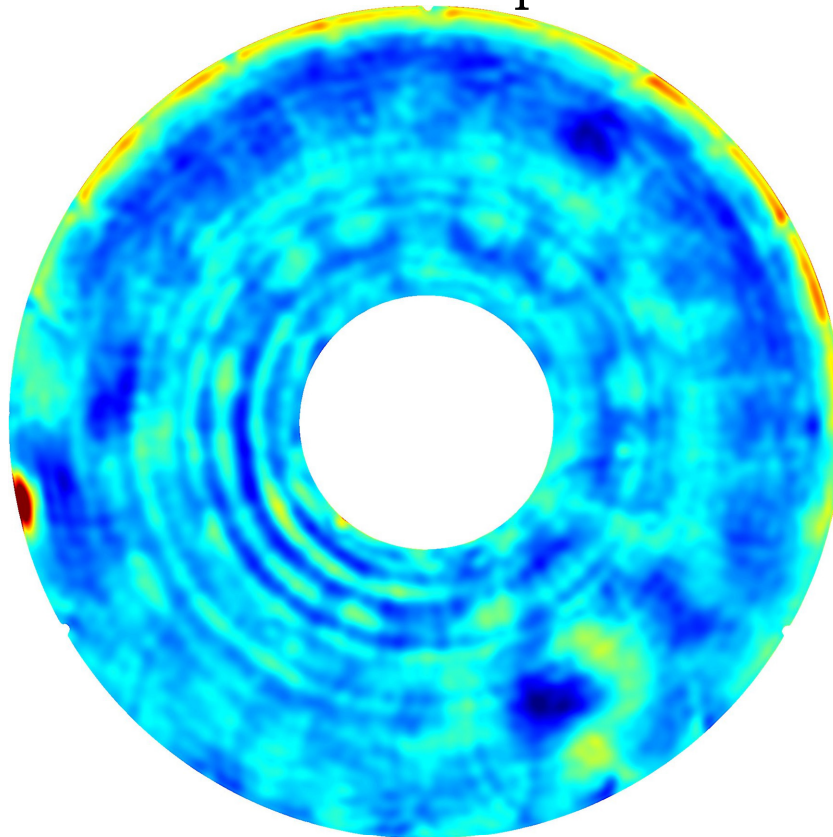


# Low-Frequency Error

(lowpass filter >10mm)

Stitched Sub-Apertures

Horizontal Full-Aperture

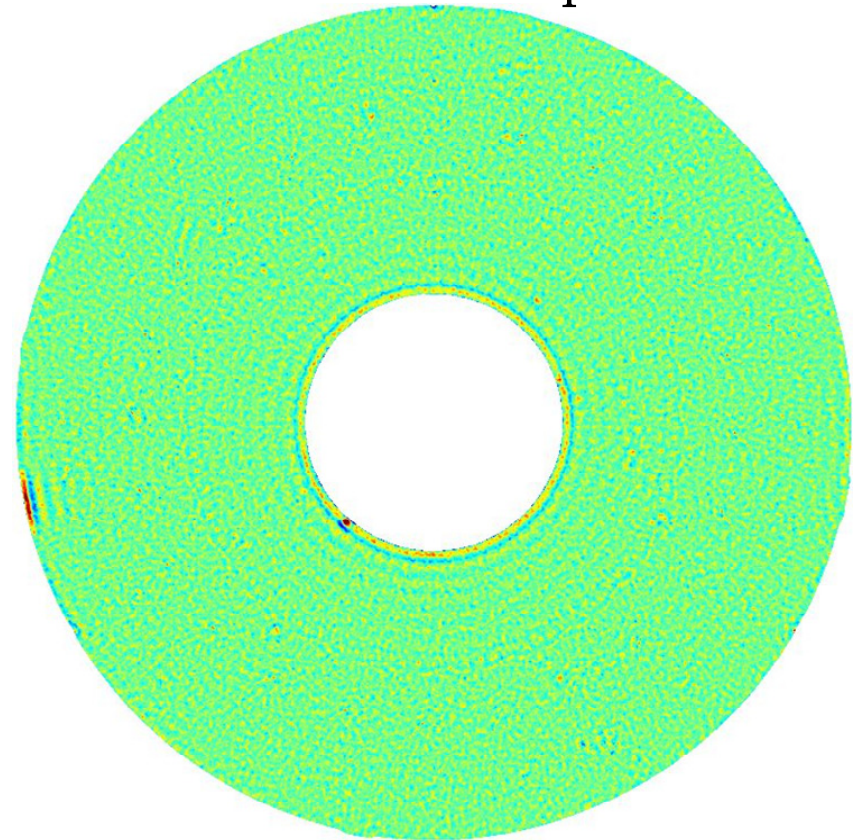
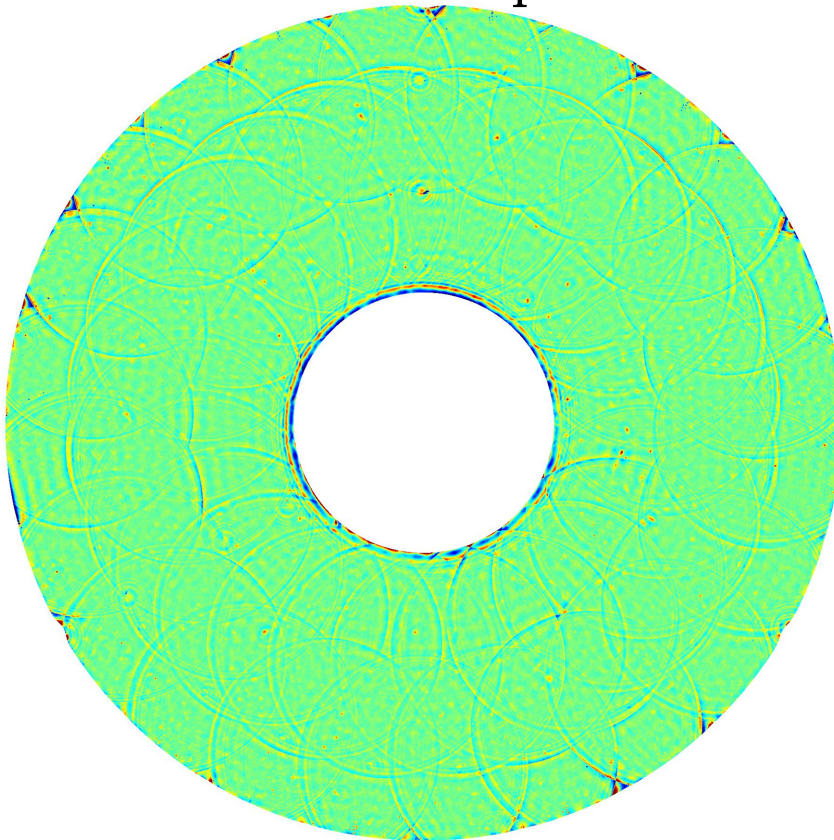


# Mid-Frequency Error

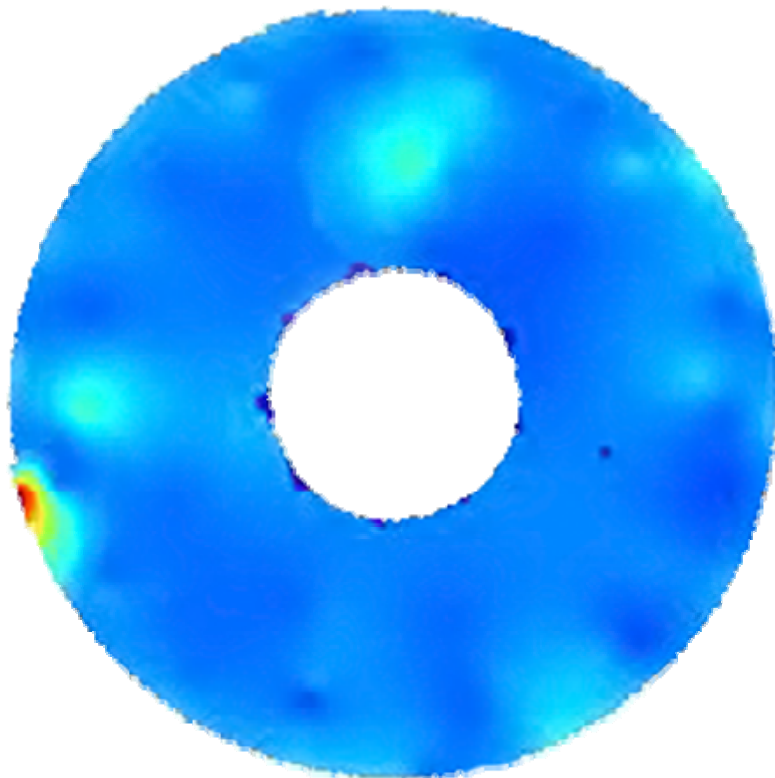
(bandpass filter 1-10mm)

Stitched Sub-Apertures

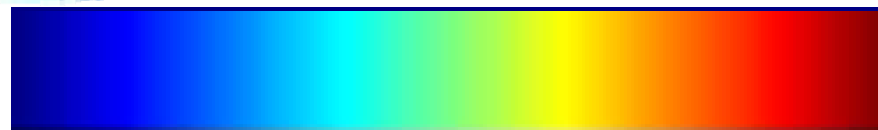
Horizontal Full-Aperture



# Roughness Distribution:



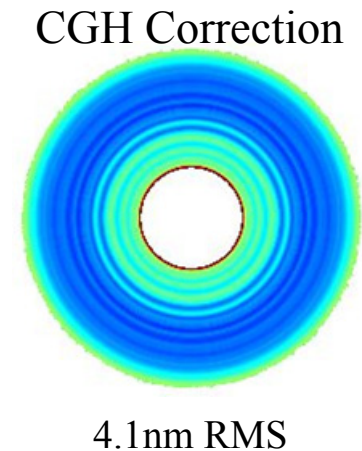
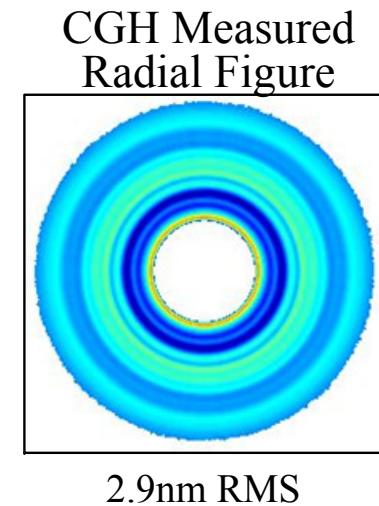
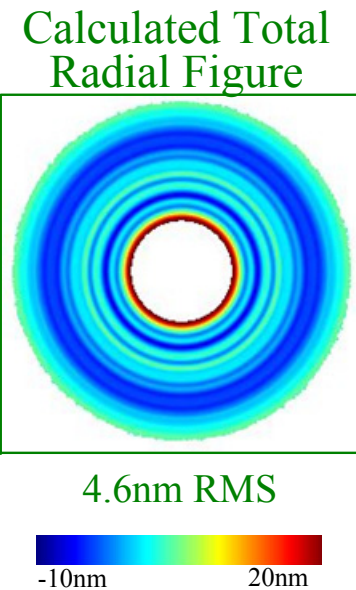
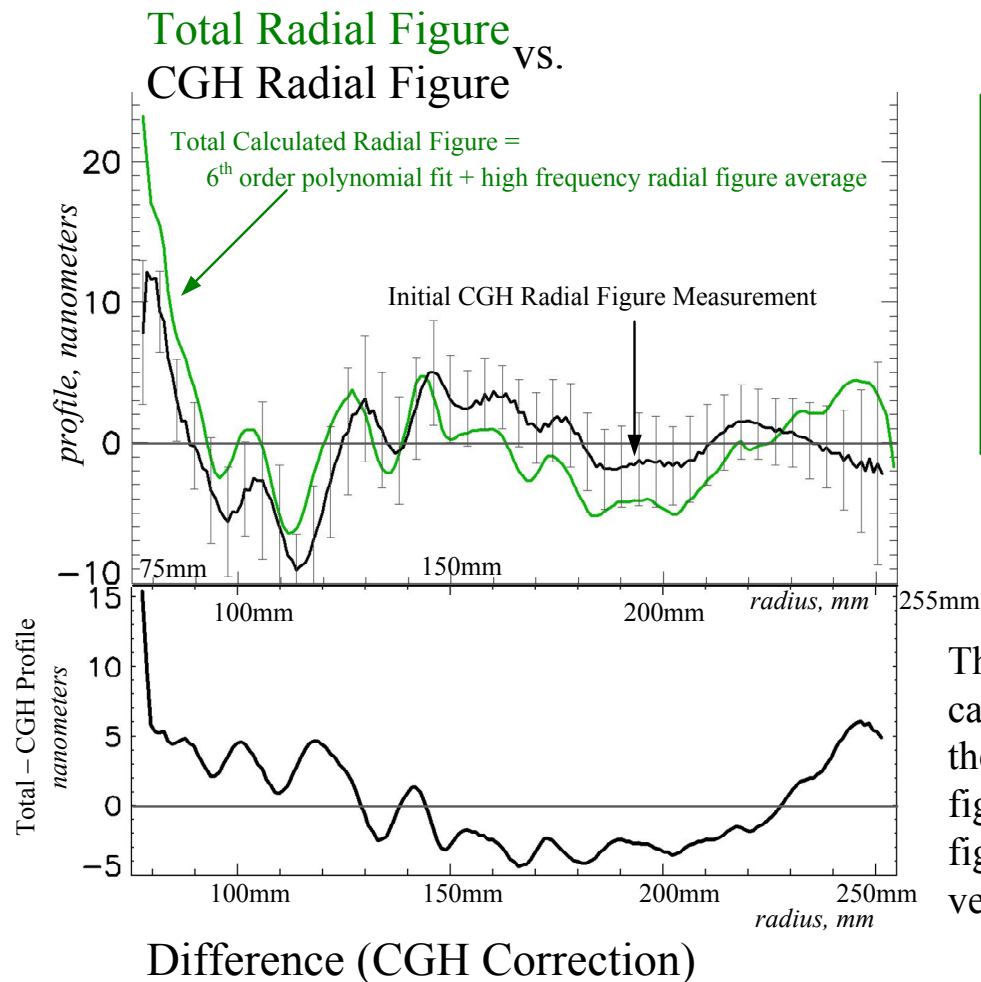
Map of RMS  
Roughness from  
20x Objective  
Topo2D Micro-  
Interferometer



0.40000 nm RMS Roughness 3.40000  
PV:2.970 RMS:0.13346



# CGH Radial Figure Correction using the Total Radial Figure

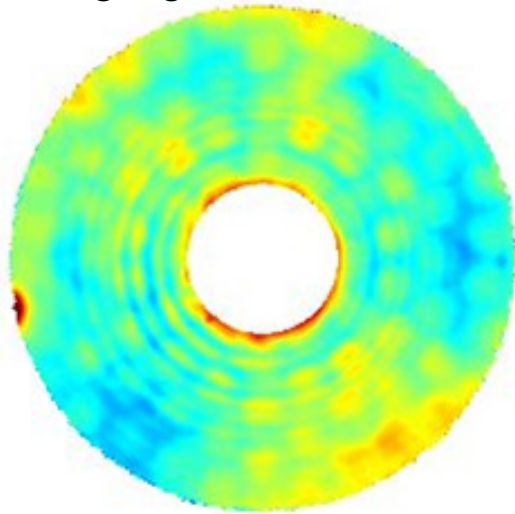


The difference between the calculated radial figure and the CGH measured radial figure results in a radial figure correction for the vertical CGH test.



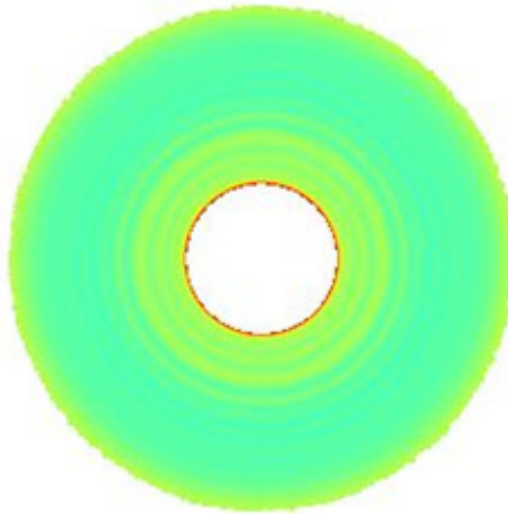
## Addition of Radial Figure Correction to CGH Measured Figure Error

Initial Vertical (CGH null)  
0g Figure Measurement



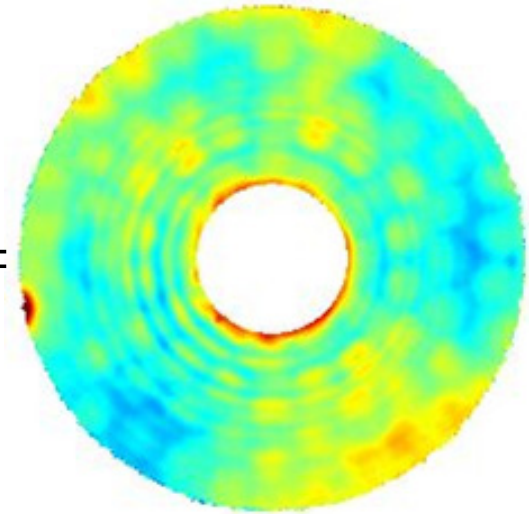
8.4nm RMS

Radial Correction from  
Horizontal Measurements



4.1nm RMS

Final Corrected 0g Figure



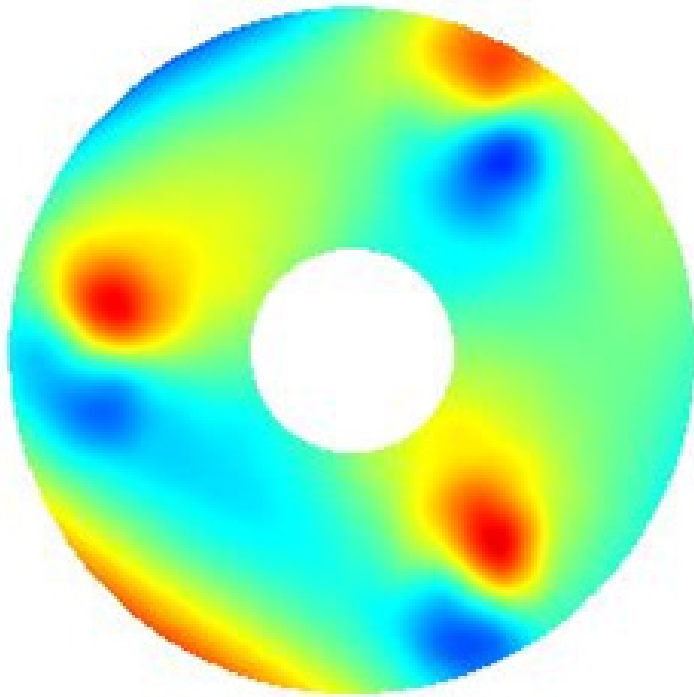
9.0nm RMS

The independent measurement of the radial figure is required to fill the blindspot in the n-position asphere test.

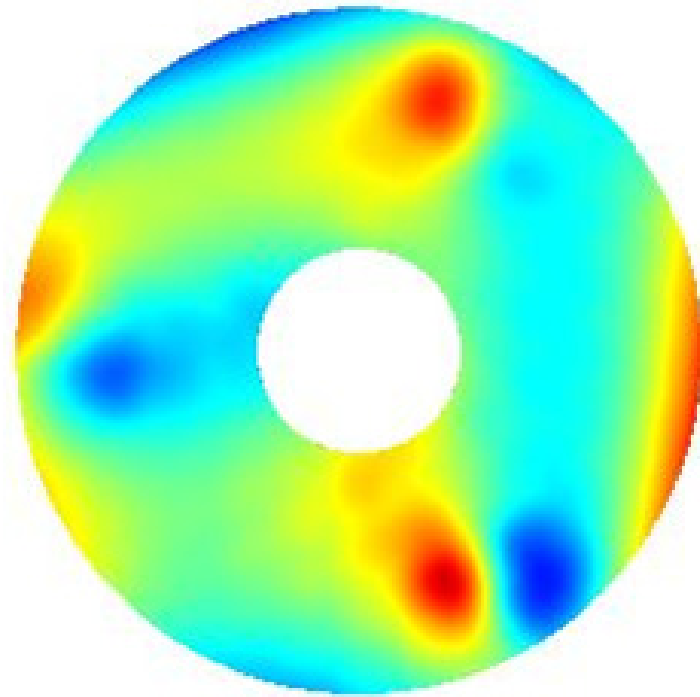
# Mounting in Vertical Test Tower

- Tower configuration allowed for *in situ* measurements of mirror figure during the rigidization of the bipod mount.
- Figure data was analyzed with finite element model predictions to help understand process errors.
- Rather than using set boundary conditions to predict a mirror figure distortion, 6DOF forces/torques were applied at mount-mirror interface points, generating an array of potential distortions.
- With some care, orthonormal influence functions were generated out of these FEM test cases and then combined with low order Zernike functions correlated with misalignment.
- Fit coefficients to these influence functions were monitored during the mounting process.
- During mounting, variations in the FEM-basis coefficients were concentrated in only two influence functions

# Orthonormal Functions: FEM #1/2



FEM Influence Function #1

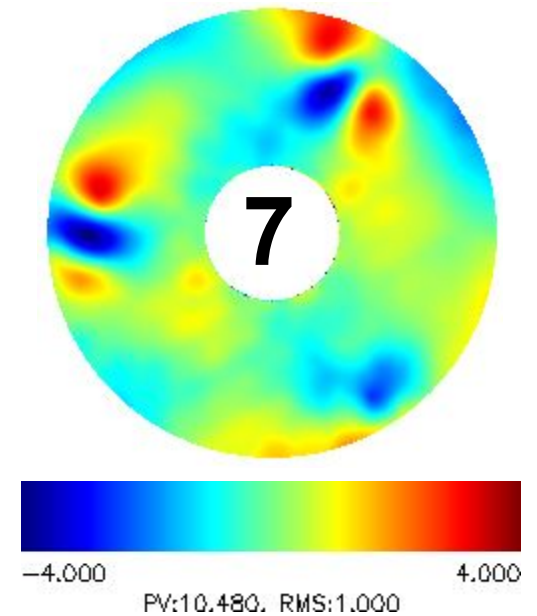
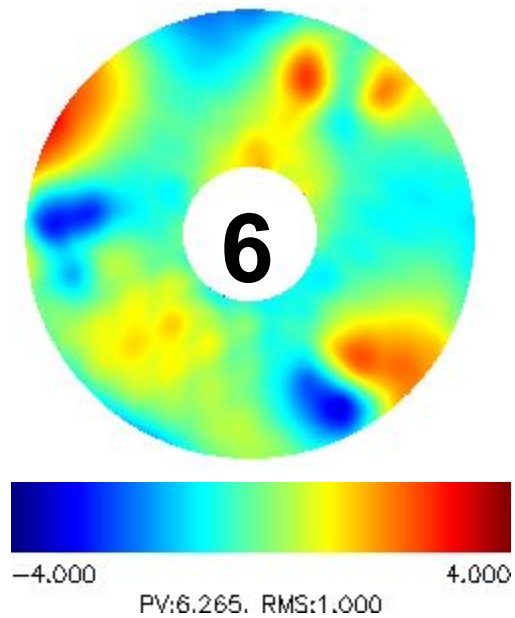
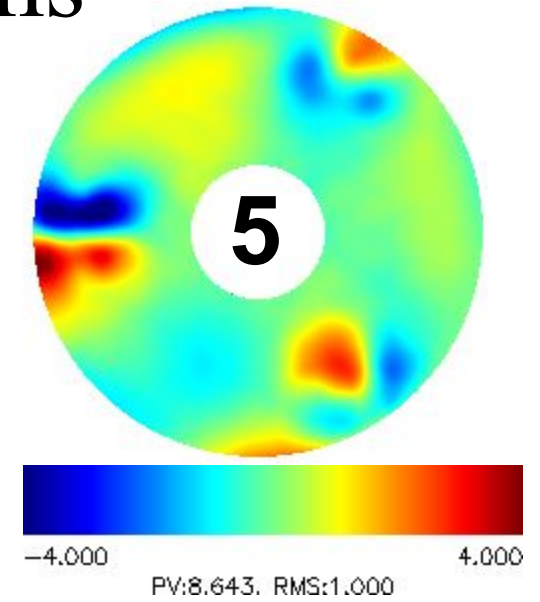
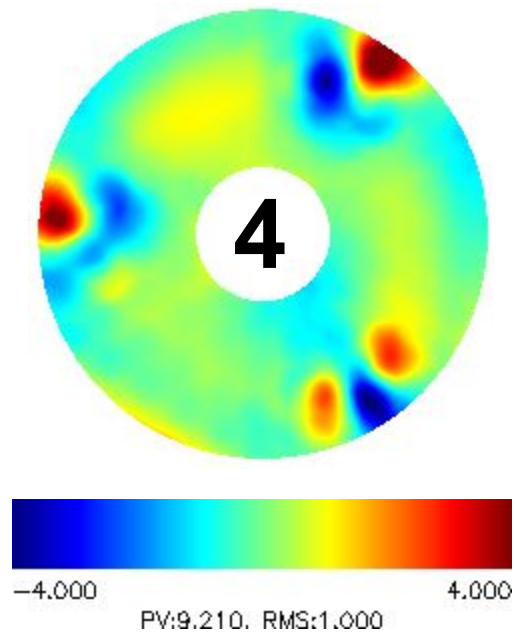
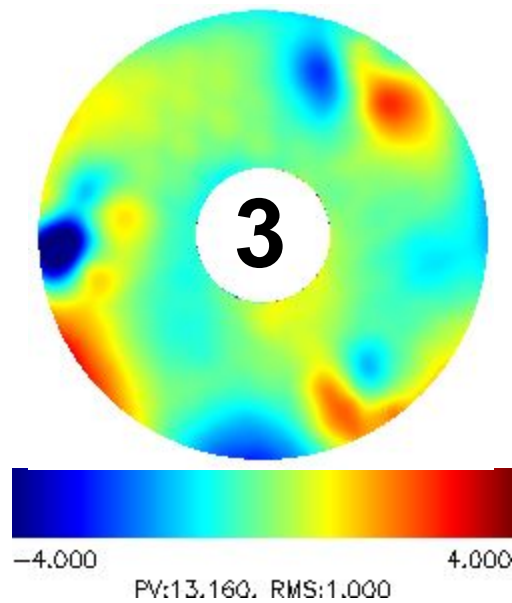


FEM Influence Function #2



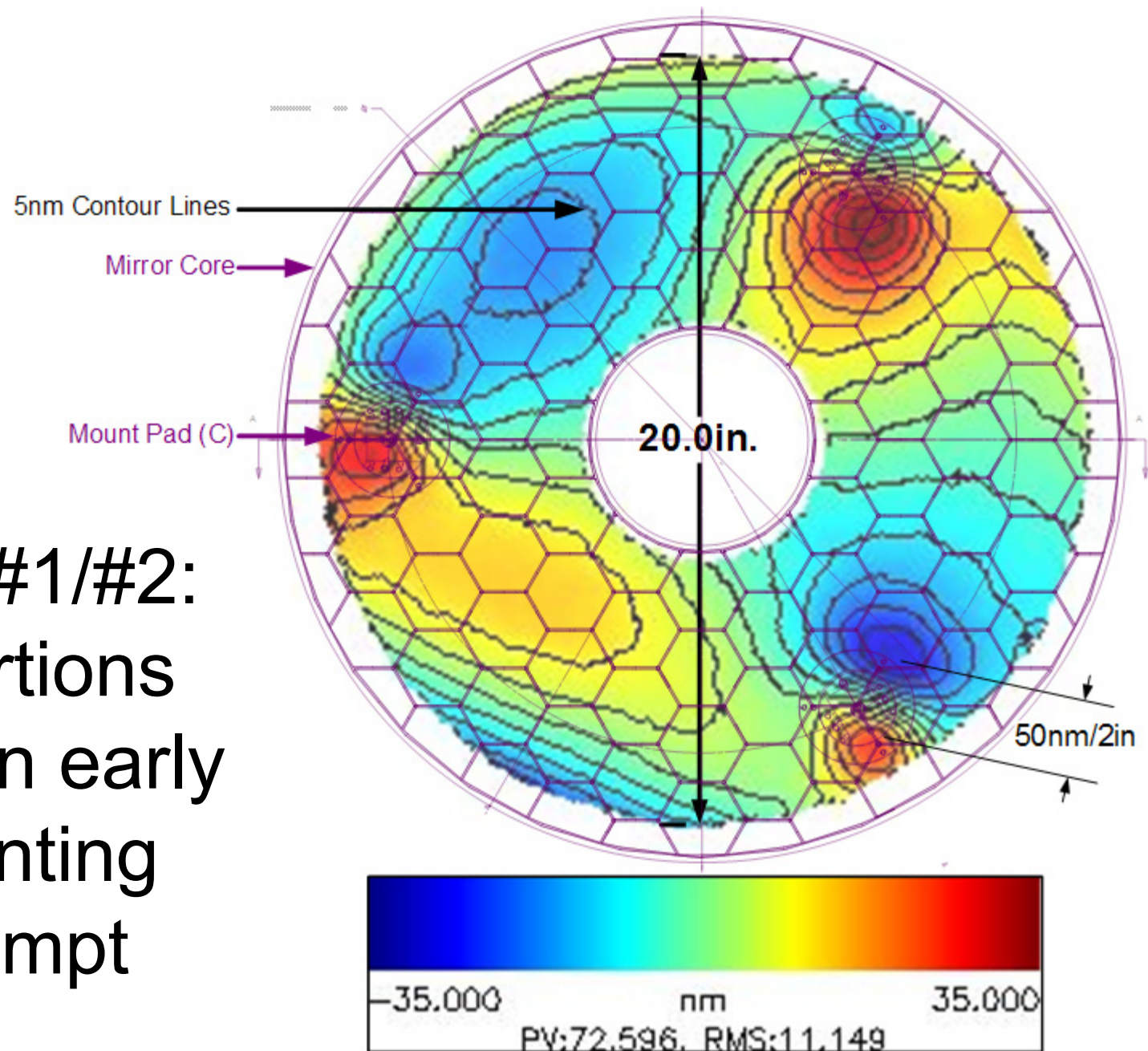
# FEM Basis Functions

## FEM #3-7



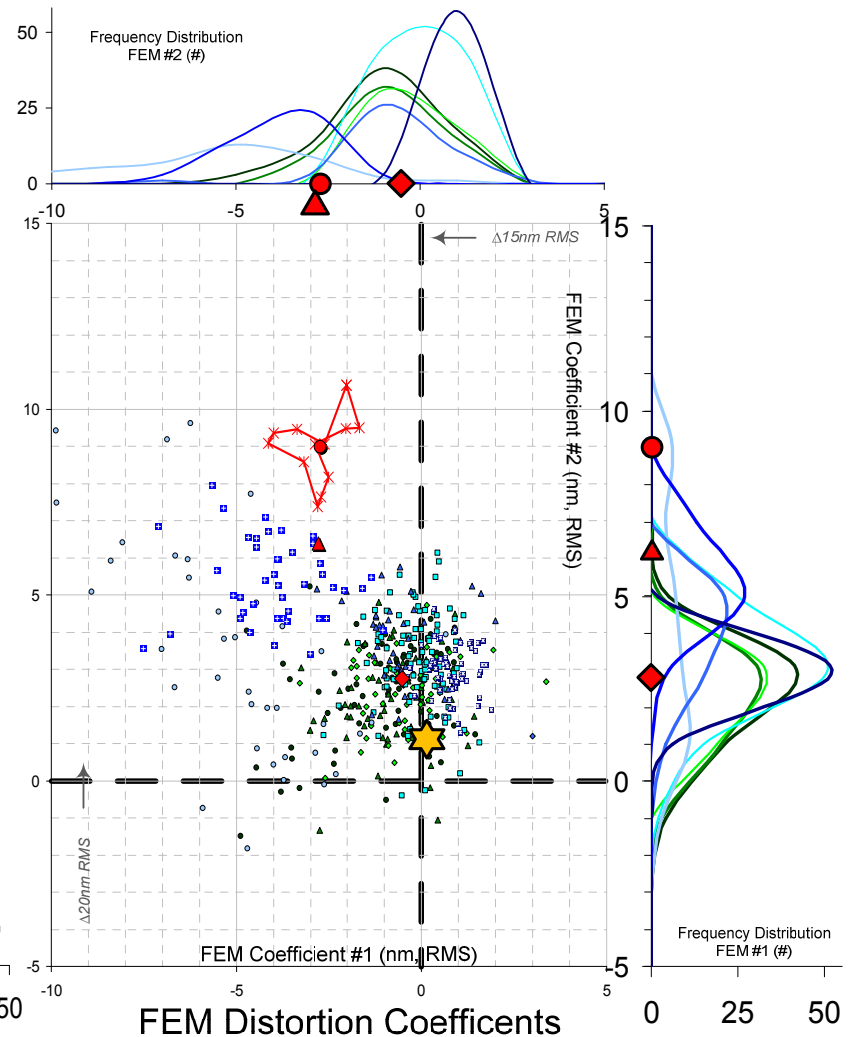
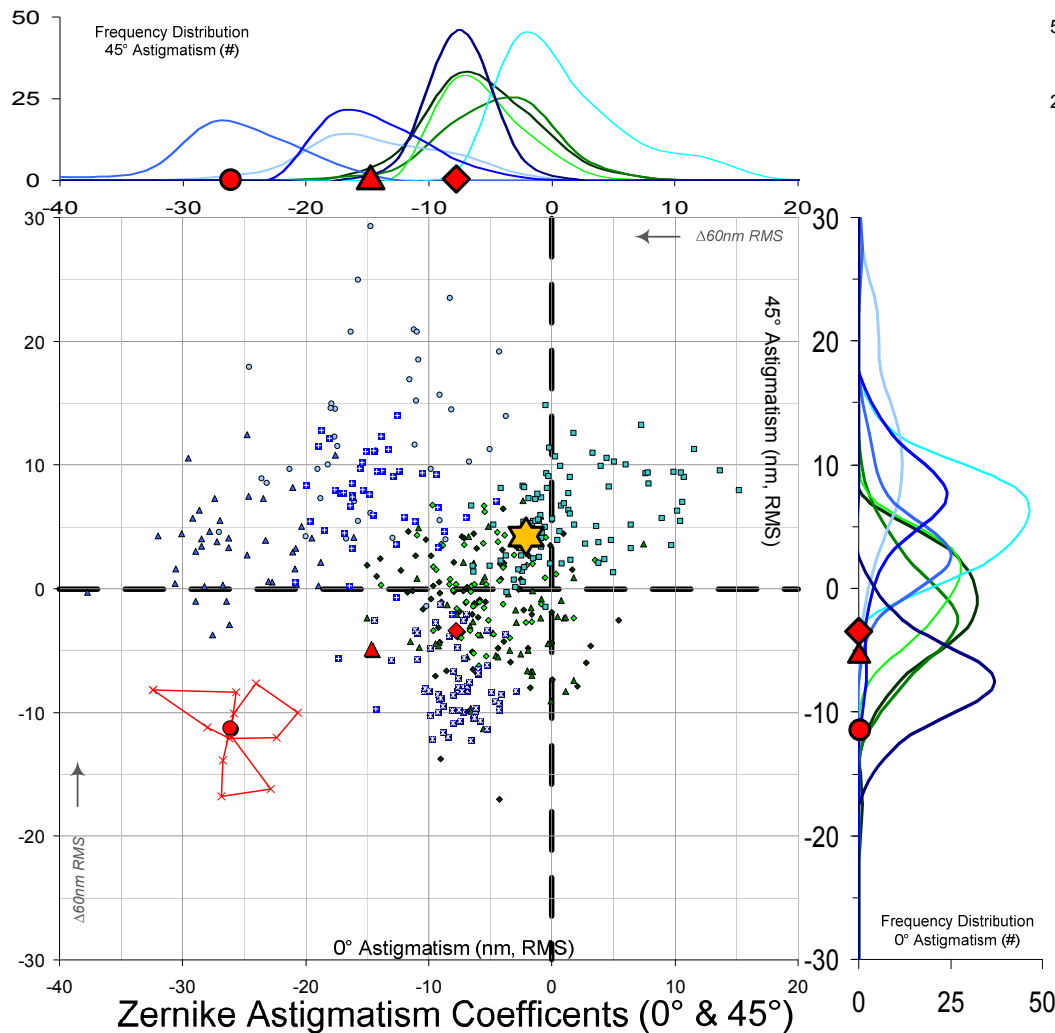


FEM #1/#2:  
distortions  
from an early  
mounting  
attempt

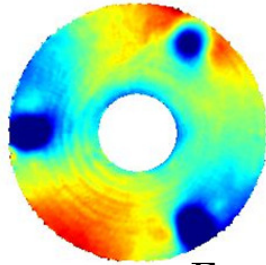




- ◆ Step 1 (loose)
- ▲ Step 2 (tighten)
- ◆ Step 3 (tighten)
- Step 4 (loosen)
- Step 5 (tighten)
- ▲ Step 6 (locked)
- Step 7 (remove support)
- Step 8 (unbolt)
- ✖ n-asphere set (12×30°)
- Average n-asphere set
- ▲ 3×4 n-asphere mount compensation
- ◆ Final mounted condition

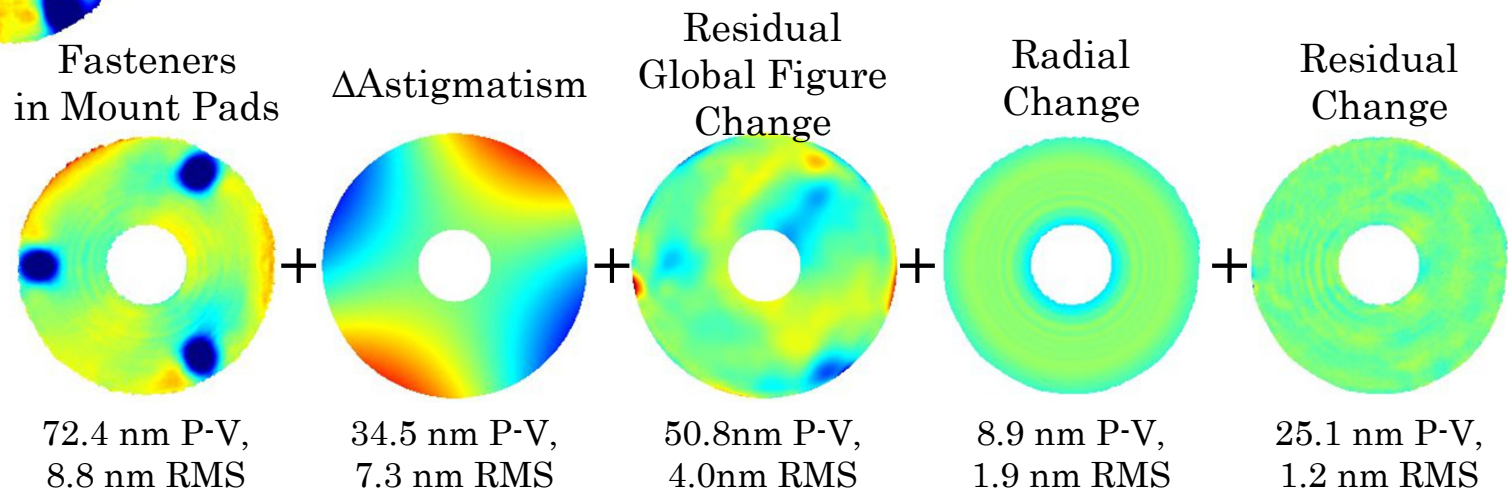


Total Change: 92.9 nm P-V,  
11.7 nm RMS

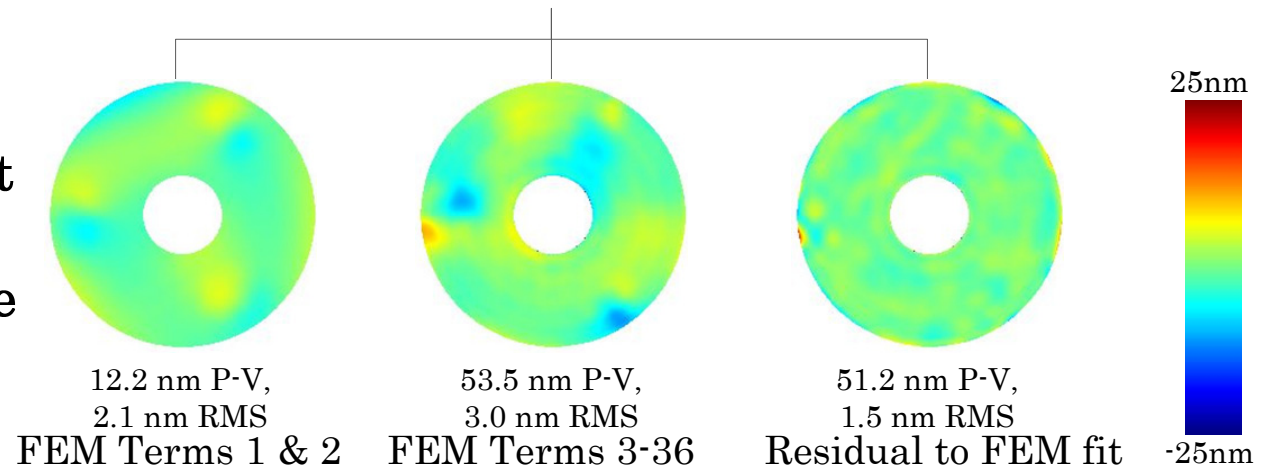


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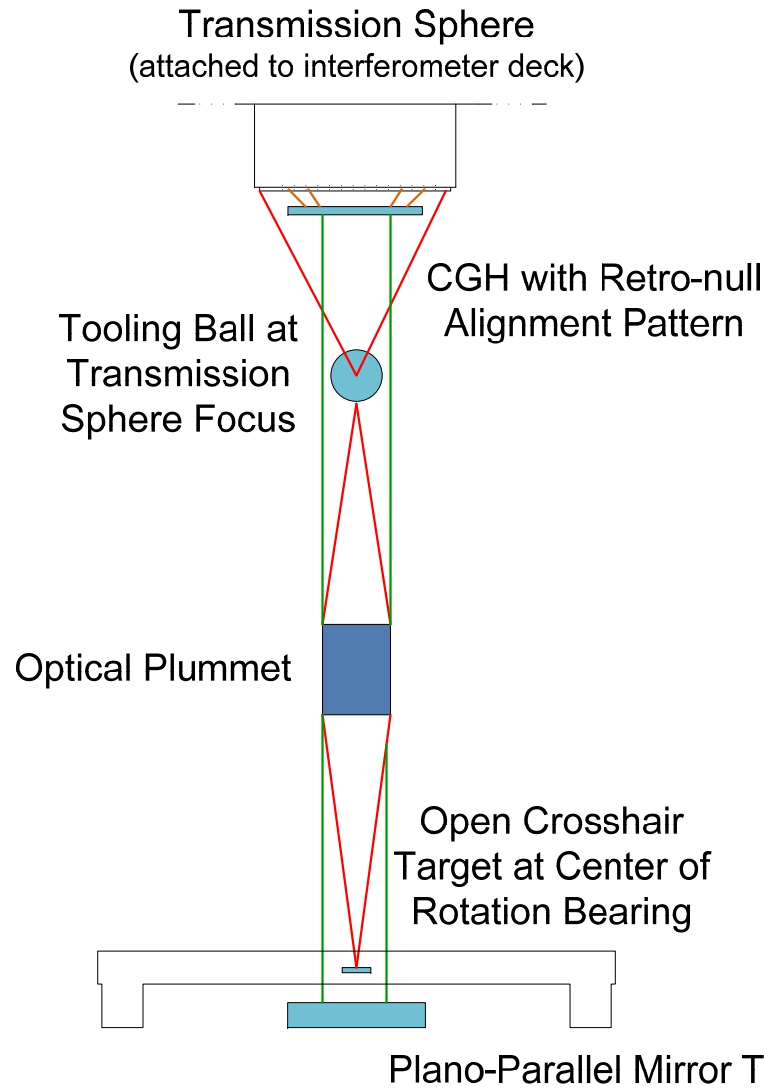
## Detailed Decomposition of Mirror Figure Changes through Mounting and Vibration Testing



FEM Basis Fit  
to Residual  
Figure Change



# Alignment of Tower



0. Tip/tilt interferometer deck so that laser output with no transmission element autoreflects off of plano-parallel.

1. Position optical plummet so that it is centered with the rotation bearing crosshair, and normal to the plano-parallel mirror on the table.

2. Center the tooling ball with the optical plummet.

3. With the CGH removed, move interferometer assembly until nulled on the tooling ball.

4. Install CGH and null CGH alignment pattern.

5. With laser aperture stopped, remove tooling ball and tip/tilt CGH until normal with plummet.

6. Open laser aperture and re-null CGH alignment pattern. Repeat steps 5 and 6 until CGH is both normal to the optical plummet and aligned with the interferometer.